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Network Inference And Graph Learning in Characterising Alzheimer's Disease

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Coventry University Centre for Computational Science and Mathematical Modelling

Network Inference And Graph Learning in Characterising Alzheimer's Disease



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Supervisor: Dr Min Wu

A thesis submitted in partial fulfilment of the University's requirements for the degree of Doctor of Philosophy

May 1, 2024

To Mum, Dad, Brother Daniel and my beloved Ivana.

Declaration

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Certificate of Ethical Approval

Applicant:

Project Title:

Dominik Klepl

Network inference and graph theory: Applications for Characterising Neurodegenerative Diseases from EEG

This is to certify that the above named applicant has completed the Coventry University Ethical Approval process and their project has been confirmed and approved as Medium Risk

Date of approval:09 Jun 2021Project Reference Number:P121994

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Abstract

Alzheimer's- disease- (AD),- the- predominant- cause- of- dementia,- presents- a- growingglobal-challenge-as-the-number-of-patients-continues-to-rise.- This-neurodegenerativecondition-is-characterised-by-disruptions-in-brain-function-and-a-progressive-decline-incognitive-abilities.- Research-shows-that-it-can-be-identified-before-the-onset-of-symptoms,- providing- an- opportunity- for- early- intervention.- However,- current- diagnosticapproaches- are-expensive- and-inaccessible,- highlighting-the-necessity- for-a-cheap- andfast-alternative.-

Electroencephalography-(EEG)-might-offer-a-viable-solution-to-this-need-due-toits-affordability- and-portability. Although-EEG-has-lower-spatial-resolution-thanfunctional-magnetic-resonance-imaging-(fMRI),-its-excellent-temporal-resolution-inmilliseconds-makes-it-a-suitable-candidate-for-early-detection.-

This thesis aims to contribute to the characterisation of AD from a graph perspective. This thesis uses graph theory to model EEG signals as graphs, capturing complex interactions between brain regions through functional connectivity (FC) to identify disruptions in brain networks and generate explainable predictions.

The first contribution introduces cross-bispectrum, a higher-order spectral analysis method, to reconstruct EEG-based FC graphs. This method can quantify both within frequency coupling and cross-frequency coupling. A novel multilayer graph modelling approach integrates information from both coupling types. The analysis reveals significant cross-frequency differences, particularly increased FC in AD cases' δ - θ coupling. Graph-theoretic analysis proves crucial in understanding the structure and function of cross-frequency brain networks, with vulnerability analysis providing insights into integration and segregation properties.

The second contribution explores various FC measures for creating graph-basedbiomarkers for AD-diagnosis using EEG. Graph-neural networks (GNNs) are employed to compare the performance of eight FC measures. The study demonstrates that GNNmodels outperform baseline models and that using FC measures to estimate brain graphs improves the overall performance of GNN. However, no single FC measure consistently outperforms others, highlighting the importance of considering multiple measures for a comprehensive analysis.

The third-contribution introduces a novel-Adaptive gated graph-convolutional-network-(AGGCN), providing explainable predictions for AD diagnosis. AGGCN-combines-convolution-based-node-feature-enhancement-with a correlation-based-power-spectral-density-similarity-measure. The gated graph-convolution dynamically-weighs the contribution of various-spatial-scales, enhancing the model's interpretability. The proposed AGGCN-achieves high accuracy under different conditions and generates consistent explanations of its predictions, offering valuable insights into AD-related alterations of brain-networks.

In-conclusion, this thesis advances our understanding of AD-by-leveraging EEG and graph theory. The novel contributions, including cross-bispectrum analysis, exploration of various FC measures, and the development of AGGCN, collectively enhance our ability to characterise and diagnose AD-from a graph perspective.

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List of Abbreviations

AD	Alzheimer's-disease-
HC	healthy-control-
\mathbf{NW}	network-neuroscience-
MCI	mild-cognitive-impairment-
\mathbf{EC}	eyes-closed-
EO	eyes-open-
GNN	graph-neural-network-
RNN	recurrent-neural-network-
NFP	node-feature-pre-processing-module-
\mathbf{FC}	functional-connectivity-
EEG	electroencephalography-
MEG	magnetoencephalography-
MRI	magnetic-resonance-imaging-
\mathbf{CT}	computerised-tomography-
BCI	brain-computer-interface-
fMRI	functional-magnetic-resonance-imaging-
\mathbf{PET}	positron-emission-tomography-
CBS	cross-bispectrum-
\mathbf{CS}	cross-spectrum-
\mathbf{PSD}	power-spectral-density-
\mathbf{CFC}	cross-frequency-coupling-
WFC	within-frequency-coupling-

AUC	area-under-curve-
\mathbf{ML}	machine-learning-
\mathbf{DL}	deep-learning-
\mathbf{SVM}	support-vector-machine-
KNN	k-nearest-neighbours-
\mathbf{SC}	structural-connectivity-
EC	effective-connectivity-
GRU	gated-recurrent-unit-
AGGCN	$adaptive \verb+gated-graph-convolutional-network-$
GCN	graph-convolutional-network-
CNN	convolutional-neural-network-
LSTM	long-short-term-memory-
MLP	multilayer-perceptron-
ND	node-degree-
NS	node-strength-
E_G	global-efficiency-
E_L	local-efficiency-
\mathbf{FFT}	fast-Fourier-transform-
\mathbf{BW}	betweenness-centrality-
CBW	coupling-betweenness-centrality-
v_G	global-vulnerability-
v_L	local-vulnerability-
PCC	Pearson's-correlation-coefficient-
СОН	coherence
iCOH	imaginary-part-of-coherency-
PLI	phase-lagged-index-
wPLI	weighted-phase-lagged-index-
PLV	phase-locking-value-

WCOH wavelet-coherence-

MI mutual-Information-

MST minimum-spanning-tree-

OMST orthogonal-MST-

ChebConv Chebyshev-graph-convolution-

DropEdge edge-dropout-layer-

AM adjacency-matrix-

ASAP adaptive-structure-aware-pooling-

 $GGCN \quad {\rm gated}\mbox{-}{\rm graph}\mbox{-}{\rm convolutional}\mbox{-}{\rm neural}\mbox{-}{\rm network}\mbox{-}$

MMSE Mini-Mental-State-Examination-

 ${\bf STGCN} \hspace{0.1 cm} {\rm spatio-temporal-graph-convolutional-network-}$

GAT graph-attention-network-

Chapter 1

Introduction

1.1 Background

Alzheimer's- disease- (AD)- is- the-leading- cause- of- dementia- among- older- individuals,posing-a-growing-challenge-to-healthcare-systems-and-economies.- There-are-approximately-47-million-patients-worldwide-diagnosed-with-AD, a-figure-projected-to-triple-by-2050-[82].- The-increase-of-patients-diagnosed-with-AD-is-likely-related-to-the-averageage-increasing-globally-because-the-prevalence-of-AD-increases-rapidly-with-age.- ADis-a-progressive-neurological-disorder-characterised-by-the-buildup-of-amyloid-plaquesand-neurofibrillary-tangles-[211,-259,-252].- This-pathology-leads-to-neuronal-cell-death,loss- of- neural-pathways- and- consecutively- widespread- disruptions- in- brain-function-[211].- Cognitively,-it-manifests-through-a-gradual-deterioration-in-memory,-executivefunction,-decision-making,- and-other-cognitive-abilities,-ultimately-leading-to-a-stagewherein- the-patients- cannot-function- independently- in- their-daily-lives- [88].- Theseissues-affect-the-families-of-AD-patients-in-significant-ways-as-well.-

Despite ongoing research, the exact causes of AD remain largely unknown; it is estimated that about 79% of the cases of late onset AD are hereditary and are often linked to specific genes [15], while only around 1% of early onset cases are familial [111]. Additionally, alterations in brain cortical activity have been observed preceding the onset of cognitive symptoms [67, 14], suggesting the potential for early detection. Although there is currently no cure for AD, an early diagnosis might be crucial to initialise procedures to mitigate the symptom severity and potentially delay or even prevent the progression to later AD stages.

However, the current process for diagnosing AD is expensive, time-consuming and may be inaccessible due to the need for specialised equipment and trained clinicians.

This process entails various neuroimaging scans such as magnetic resonance imaging (MRI), computerised tomography (CT), positron emission tomography (PET) and cerebrospinal fluid analysis, as well as a battery of cognitive tests assessing abilities such as short-term memory, attention and spatial orientation [64, 110, 13]. Therefore, there is an urgent need for a reliable, economical, portable and automated alternative diagnostic method. Despite the desirability of an automated method, it is crucial to provide accurate and easy-to-understand explanations so that experts can validate the automated predictions.

Electroencephalography- (EEG)- is- a-suitable- candidate- for- addressing- this- need.-EEG- is- a- non-invasive- neuroimaging- technique- that- measures- the- sum- of- electricalpotentials-generated-by-neuronal-populations-within-the-brain.- Specifically,-EEG-functions- by- placing-electrodes- on- the-subject's-scalp.- Compared- to- other- neuroimagingmethods-capable-of-capturing-brain-dynamics,-such-as-functional-magnetic-resonanceimaging-(fMRI)-and-magnetoencephalography-(MEG),-EEG-is-portable-and-relativelyaffordable.- However,-because-of-recording-at-the-scalp-level-with-a-limited-number-ofelectrodes,-the-spatial-resolution-of-EEG-is-low-compared-to-fMRI.- Thus,-signals-fromthe-brain-cortex-are-predominantly-detected.- On-the-other-hand,-EEG-has-excellenttemporal-resolution-at-the-scale-of-milliseconds-[14,-13].- While-EEG-can-be-measuredat-rest- and-during-a-task,- this-thesis-focuses-only-on-resting-state-EEG.- Recording-EEG-data-during-a-resting-state-presents-advantages-in-investigating-AD-patients-dueto-its-low-demand-for-active-engagement-and-non-intrusive-nature,-thereby-mitigatingstress-that-might-be-otherwise-induced-by-performing-a-task.-

Although-EEG-is-not-currently-used-in-a-clinical-setting-for-AD-diagnosis,-it-hasbeen-widely-used-for-studying-changes-induced-by-neurodegenerative-diseases-[13,-14]. There-is-evidence-of-alterations-of-brain-oscillatory-patterns-in-early-AD-when-compared-to-age-matched-healthy-control-(HC)-prior-to-observing-any-structural-changessuch-as-signal-slowing-and-complexity-reduction-[14,-67].-Additionally,-EEG-has-beensuccessfully-used-to-measure-brain-connectivity,-i.e.-relationships-between-pairs-of-brainregions.-As-the-pathology-of-AD-causes-widespread-disconnections-between-brain-areas,it-can-be-considered-a-network-disorder-(i.e.-graph).-Thus,-studying-the-connectivityfrom-a-graph-perspective-is-crucial-for-accurately-characterising-AD-[76,-36,-260].-

For these reasons, the research presented in this thesis focuses on examining the disruptions in connectivity induced by AD. Specifically, the aim is to examine novel ways to design a graph-based approach to characterise the complex changes in the brain-due to AD and utilise these characteristics to generate accurate and interpretable

predictions.

1.2 Motivation

It-is-well-known-that-the-brain-is-a-complex-network-of-neural-units-interacting-acrossmultiple-spatial-and-temporal-scales-[21].- The-patterns-of-brain-oscillations- acquiredfrom-multiple-EEG-electrodes-have-traditionally-been-analysed-in-isolation,-grandaveraged-across-electrodes-or-their-pairwise-interactions.- However,-using-such-an-approach,-it-is-not-possible-to-quantify-the-function-of-the-entire-brain-[23].- Networkneuroscience- (NW)-is-an-emerging-approach-in-neuroscience-which-aims-to-addressthis-issue.- Unlike-other-neuroscience-approaches,-NW-studies-the-brain-from-an-integrative-perspective-[27,-22].- This-means-that-NW-assumes-that-the-function-of-thebrain-is-distributed-and-cannot-be-studied-by-looking-at-single-units.- This-core-assumption-is-then-conceptualised-as-a-graph.- In-most-NW-literature,-the-graph-nodes-arebrain-areas,-and-edges-signify-some-relationship-exists-between-the-nodes-[27,-196,-40].-

Networks-on-various-scales-of-the-brain-can-be-defined-from-molecular-and-cellularlevels-up-to-macro-regions-of-the-brain-[23].- The-research-presented-in-this-thesis-is-positioned-at-the-far-end-of-this-dimension-as-EEG-provides-only-a-coarse-spatial-resolution,i.e.- electrical-potentials-measured-on-the-level-of-macro-regions-[204,-14].- Specifically,the-nodes-are-modelled-at-the-electrode-level-such-that-each-node-corresponds-to-an-EEG-electrode.-

The edges connecting brain regions can be defined in multiple ways. Structural connectivity (SC) edges represent the physical connections between regions retrieved frommethods such as MRI or CT [40, 22]. However, information about SC is unavailable in electrophysiological signals such as EEG. In contrast, edges modelled as functional connectivity (FC) and effective connectivity (EC) represent a statistical dependency and causal relationship between regions, respectively [27, 40, 22]. This thesis focuses on FC-based methods to reconstruct brain graphs from EEG recordings.

FC-measures-can-aim-to-quantify-various-types-of-dependencies-between-pairs-ofsignals. There-are-linear-and-nonlinear-approaches-[224], time-and-frequency-domainapproaches-[3], and phase-and amplitude approaches [35]. Additionally, FC-can-becomputed-on-full-frequency-signals-(approximately-between-0.5Hz and 100Hz)-or-specific-frequency-bands. Studies-show-that-AD-related-changes-can-be-observed-mainlyin- δ (0.5-4Hz), θ (4-7Hz)-and β (15-31Hz)-bands-[13]. Studies-have-shown-that-AD-affects-distributed-brain-networks, alters-FC-and-disrupts-information-processingacross-multiple-scales-[207,-150,-76,-128].-

Besides-this-type-of-within-frequency-coupling-(WFC), there is a growing amountof-evidence-that-cross-frequency-coupling-(CFC)-serve-a-crucial-role-in-the-brain-[45,-42].- CFC-quantifies-FC-between-signals-with-different-frequencies.- It-is-hypothesisedthat-CFC-plays-a-role-in-synchronising-local- and-global-processes- and-relates-to-theinformation-integration-across-distributed-systems-[135].- Specifically, various-types-of-CFC-have-been-detected-in-the-brain-[126], such-as-amplitude-to-amplitude-[126,-73,-39,-135], phase-to-phase-[126,-42,-251,-135]-and-phase-to-amplitude-[126,-59,-257,-135].-However,-CFC-has-been-predominantly-studied-to-measure-pairwise-interactions.- Acomprehensive- analysis- of-CFC- from- a-graph-perspective- that-would-elucidate- theroles- of-different-frequency-components- is-thus-required.- CFC- brain-graphs-mightbe- effectively-modelled-using-multilayer-graphs-where- each-frequency-component- isrepresented-by-a-layer- and-with-inter-layer-edges-encoding-CFC-interactions.- This-isone- of- the-aims- of- this- thesis.- Additionally,- the- utility- of-accounting-for-nonlinearinteractions-in-addition-to-linear-is-examined-in-this-thesis.-

After-a-brain-graph-is-reconstructed-from-EEG, the next-challenge-is-to-design-an-effective-model-to-deliver-accurate-predictions-about-the-graphs. Feature-based-machinelearning-(ML)-is-one-of-the-available-approaches. Graph-theory-can-be-leveraged-to-engineer-features-describing-various-brain-graph-properties-manually-[40]. Such-featurescan-be-nodal, i.e. defined-for-each-node-of-a-graph, or-global, i.e. an-index-describingthe-graph-as-a-whole-[3,-27]. Nodal-features-are-commonly-used-to-identify-influentialnodes-in-the-graph. In-the-context-of-AD, node-degree-[197], and-clustering-coefficient-[273,-172,-52,-84]-have-been-successfully-used-to-determine-brain-regions-important-forcharacterisation-and-prediction-of-AD. While-ML-models-can-be-efficient-and-offer-relatively-simple-interpretability, the need-for-manual-feature-engineering-poses-a-cruciallimitation-of-such-an-approach. Feature-engineering-requires-expert-domain-knowledgeand-is-generally-time-consuming-[50].-

Deep-learning-(DL)-models-offer-an-alternative-approach-with-automatic-featureextraction,-although-they-require-the-selection-of-a-large-number-of-hyperparameterscompared-to-ML.- However,-most-traditional-DL-architectures-are-ill-suited-for-graphstructured-inputs-[37].- Models-such-as-multilayer-perceptrons-(MLPs),-convolutionalneural-networks- (CNNs),- and- recurrent- neural- networks- (RNNs)- were- designed- for-Euclidian-inputs- such- as- time- series- and- images.- Graph- neural- networks- (GNNs)have-been-proposed-to-address-this-limitation- and-offer- an-efficient-extension- of-theconvolutional-mechanism-of-CNN-to-graphs-[312].- However,-the-applications-of-GNN- for-EEG-tasks-are-relatively-limited-without-a-clear-set-of-guidelines-for-designing-suchmodels.- Thus,-another-aim-of-this-thesis-is-to-systematically-review-this-emerging-subfield-of-NW- and-propose-categorisation-of-the-various-approaches-experimented-within-the-literature.-

As-discussed-above, various-FC-measures-are-utilised-in-the-literature. However, selecting-an-appropriate-measure-of-FC-for-subsequent-graph-analysis-and-classification-remains-ambiguous. To-our-knowledge, this-is-true-for-both-ML-and-DL-approaches. This-thesis-aims-to-fill-this-gap-by-proposing-an-empirical-evaluation-of-the-effect-an-FC-measure-has-on-the-performance-of-various-ML-and-DL-models, including-GNNs-in-the-AD-diagnosis-task.

A-crucial-area-for-improvement-of-the-modelling-approaches-mentioned-previouslyis-their-explicit-lack-of-explainability, i.e.- it-is-usually-possible-to-generate-some-explanations-via-post-hoc-analysis.- For-a-model-to-be-successfully-deployed-in-a-real-worldclinical-setting, it-is-vital-to-produce-consistent-and-detailed-explanations-of-its-predictions-that-medical-experts-can-validate.- For-AD-prediction-task,-such-explanationsneed- to-be-generated-for-multiple-spatial-scales-as-AD-related-disruptions- are-wellknown-to-present-on-both-local-and-global-levels-[6].- GNNs-are-an-ideal-architecturefor-such-a-purpose-due-to-the-inherent-nature-of-the-graph-convolutional-mechanismof-graph-convolutional-network-(GCN)-family-of-GNNs-[312,-285].- Briefly,-GCNs-learnvia-recursive-information-aggregation-across-gradually-increasing-receptive-fields.- Therecursive-property- of-GCNs-might-be-leveraged-to-quantify-patterns-across-variousspatial-levels,-going-from-highly-localised-to-coarse-grained-whole-brain-levels.-

Unlike-other-DL-models, the-input-to-GNNs-forms-the-computational-graph-simultaneously, i.e. graph-structure-is-leveraged-both-for-learning-and-information-propagation-[285].- Whether-the-input-graph-structure-is-the-optimal-computational-graphhas-been-a-central-point-of-interest-in-GNN-literature-[31].- A-popular-approach-hasbeen-to-decouple-the-computational-graph-from-the-input-with-methods-such-as-graphrewiring-[256,-137],- graph-lifting- to-higher- dimensional- topological-spaces- [31]- andtransformer-based-methods-[152,-292].- However,-preserving-the-FC-based-graph-structure-is-essential-for-brain-graph-prediction-tasks-to-retain-the-ability-to-generate-modelpredictions,-which-would-be-lost-if-the-computational-graph-is-fully-decoupled-fromthe-input.- This-thesis-explores-a-hybrid-strategy-where-the-model-learns-the-graphstructure.- This-offers-two-advantages:- (1)- the-dilemma-of-FC-measure-selection-iseffectively-circumvented,- and- (2)- the-model- is-free-to-adapt- the-graph-structure-tostrike-a-balance-between-producing-an-optimal-computational-graph- and-recoveringthe underlying brain-graph-structure.-

1.3 Aims and Objectives

Generally-speaking, the main-aim-of-this-research-thesis-is-to-model-high-dimensional-EEG-signals-from-a-graph-perspective-in-order-to-quantify-the-changes-in-the-brainconnectivity-caused-by-neurodegenerative-diseases-and-to-develop-novel-biomarkers-fordiagnosis-and-characterisation-of-neurodegenerative-diseases.- Such-results-can-potentially-improve-the-diagnostic-process-of-AD-due-to-the-accessibility, ease-of-use-and-lowcost-of-EEG.- This-main-objective-is-concisely-captured-within-the-following-researchquestion:-

How can reconstructed complex brain graphs from EEG signals be used for diagnosing and characterising neurodegenerative diseases?

In-order-to-provide-a-detailed-answer-to-the-research-question,-multiple-objectiveswere-identified,-highlighting-the-key-elements-and-potential-for-novel-contributions-ofthis-research-project.- The-objectives-listed-below-aim-to-research-the-brain-structureand-function-changes-induced-by-neurodegenerative-disease.- This-aim-is-not-explicitlyformulated-in-the-objectives-to-avoid-repetition.- Although-there-are-other-types-ofneurodegenerative-diseases,-this-research-project-is-going-to-focus-on-AD-as-this-diseaseaffects-the-largest-portion-of-the-human-population.-

- 1.- Assess-the-predictive-power-of-nonlinear-and-cross-frequency-brain-connectivitycompared-to-linear-and-within-frequency-alternatives.-
- 2.- Develop-methods-for-analysing-cross-frequency-coupling-from-a-graph-perspectiveusing-a-multilayer-graph-analysis-framework.-
- 3.- Investigate-the-use-of-graph-representation-learning-algorithms-and-graph-neural-networks-to-study-neurodegenerative-diseases-and-facilitate-the-diagnosticprocess.-
 - (a)- Systematically-review-graph-neural-networks-for-EEG-classification-in-orderto-facilitate-a-current-overview-of-the-field-and-aid-in-innovation.-
 - (b)- Examine-the-usability-of-common-functional-connectivity-methods-to-constructing-input-EEG-brain-graphs-to-graph-neural-networks.-

- 4.- Assess-the-potential-of-graph-neural-networks-for-automatically-reconstructingbrain-graph-structures.-
- 5.- Develop-graph-neural-network-architecture-for-explainable-prediction-of-neurodegenerative-diseases.-

1.4 Overview of the Thesis

This-thesis-is-organised-into-seven-chapters-and-covers-the-following-content:-

- Chapter 2 examines-prior-research-connected-to-this-thesis.-It-begins-by-exploring-different-methods-for-reconstructing-brain-graphs-from-EEG.-It-then-delvesinto-understanding-established-changes-in-AD,-focusing-on-graph-level-alterations.-Lastly,-it-critically-assesses-the-utilisation-of-GNNs-in-analysing-EEG.- Overall,this-chapter-pinpoints-several-research-gaps-this-thesis-intends-to-address.-
- Chapter 3 describes-the-details-of-the-EEG-dataset-that-is-subsequently-utilisedin-chapters-4,-5-and-6.-
- Chapter 4 presents-work-on-utilising-the-higher-order-nonlinear-bispectrum-toreconstruct-multilayer-brain-graphs-incorporating-information-about-both-WFCand-CFC-interactions.-It-evaluates-the-benefits-of-this-approach-against-a-singlelayer-linear-alternative-in-terms-of-statistical-characterisation-and-ML-based-prediction-of-AD.-
- Chapter 5 presents the practical assessment of the influences of different FCmeasure on the performance of multiple ML and DL algorithms in AD diagnosistask.
- Chapter 6 introduces-adaptive-gated-graph-convolutional-network-(AGGCN), anovel-GNN-architecture-designed-for-AD-classification.-Unlike-traditional-graphbased-approaches-dependent-on-specific-FC-measures, this-architecture-employs-adata-driven-approach-for-reconstructing-brain-graphs.-Demonstrating-outstanding-performance-in-contrast-to-several-state-of-the-art-methods, it-generates-diverse-prediction-explanations-at-graph, node, and edge-levels.-
- Chapter 7 summarises-the-presented-contributions-and-outlines-potential-futureresearch-directions.-

1.5 Contributions and Research Outputs

This-thesis-introduces-original-contributions-focused-on-utilising-machine-learning,-deep-learning,-and-graph-theory-methods-to-characterise-AD-from-graph-perspective.- This-research-aims-to-contribute-to-developing-a-data-driven-framework-for-analysing-and-understanding-neurodegenerative-diseases.-

1.- Chapter 2 reviews- previous- research- on- graph- approach- to- reconstruct- andclassify-brain-graphs-of- AD- cases- from- EEG-signals.- The-main-contribution-ofthis-chapter-is-a-survey-of-applications-of-GNNs-for-EEG-classification.-

Based-on-parts-of-this-work,-a-review-paper-has-been-published:-

- Dominik-Klepl, Min-Wu, and Fei-He. Graph-Neural-Network-Based-EEG-Classification: A-Survey. *IEEE Transactions on Neural Systems and Rehabilitation Engineering*, 32:493–503, 2024. ISSN-1558-0210. doi: 10.1109/TN-SRE.2024.3355750-
- 2.- Chapter 4 introduces-novel-multilayer-graph-analysis-to-elucidate-the-roles-ofvarious-brain-rhythms-in-enabling-information-integration-and-segregation-withinthe-brain-and-how-these-roles-are-disrupted-due-to-AD.- This-information-is-thenused-for-ML-based-prediction-of-AD.-

Based-on-this-work,-a-journal-paper-and-a-conference-paper-have-been-published:-

- Dominik-Klepl, Fei-He, Min-Wu, Daniel-J. Blackburn, and Ptolemaios-G. Sarrigiannis. Cross-Frequency-Multilayer-Network-Analysis-with-Bispectrum-based-Functional-Connectivity: A-Study of Alzheimer's Disease. Neuro-science, 521:77–88, June 2023. ISSN 0306-4522. doi: 10.1016/j.neuroscience. 2023.04.008-
- Dominik-Klepl, Fei-He, Wu-Min, Daniel-Blackburn, and Ptolemaios-Sarrigiannis. Bispectrum-based-Cross-frequency-Functional-Connectivity: Classification of Alzheimer's disease. In 2022 44th Annual International Conference of the IEEE Engineering in Medicine & Biology Society (EMBC), pages 305–308, July 2022. doi: 10.1109/EMBC48229.2022.9871366-
- 3.- Chapter 5 reports-the-effect-of-commonly-used-FC-measures-on-the-performanceof-ML-and-DL-models-in-AD-classification-task.- The-main-focus-is-on-GNNs.-

Based-on-this-work,-a-journal-paper-has-been-published:-

- Dominik-Klepl, Fei-He, Min-Wu, Daniel-J.-Blackburn, and Ptolemaios-Sarrigiannis. EEG-Based-Graph-Neural-Network-Classification-of-Alzheimer's-Disease: An-Empirical-Evaluation-of-Functional-Connectivity-Methods. *IEEE Transactions on Neural Systems and Rehabilitation Engineering*, 30:2651–2660, 2022. ISSN-1558-0210. doi: 10.1109/TNSRE.2022.3204913-
- 4.- Chapter 6 introduces-a-novel-GNN-architecture-with-a-learnable-graph-structure, thus-avoiding-the-issue-of-FC-measure-selection.- The-focus-is-on-acquiringexplainable-predictions.-

Based-on-this-work,-a-journal-paper-has-been-published:-

Dominik-Klepl, Fei-He, Min-Wu, Daniel-J. Blackburn, and Ptolemaios-Sarrigiannis. Adaptive-Gated-Graph-Convolutional-Network-for-Explainable-Diagnosis-of-Alzheimer's-Disease-Using-EEG-Data. *IEEE Transactions on Neural Systems and Rehabilitation Engineering*, 31:3978–3987, 2023. ISSN-1558-0210. doi: 10.1109/TNSRE.2023.3321634-

Moreover,-additional-research-outputs-have-been-published-during-this-PhD-project:-

• Dominik-Klepl, Fei-He, Min-Wu, Matteo-De-Marco, Daniel-J. Blackburn, and Ptolemaios-G. Sarrigiannis. Characterising-Alzheimer's-Disease-With-EEG-Based-Energy-Landscape-Analysis. *IEEE Journal of Biomedical and Health Informatics*, 26(3):992–1000, March-2022. ISSN-2168-2208. doi: 10.1109/JBHI.202-1.3105397-

• Sivasharmini-Ganeshamoorthy, Laura-Roden, Dominik-Klepl, and Fei-He.-Gene-Regulatory-Network-Inference-through-Link-Prediction-using-Graph-Neural-Network.- In-2022 IEEE Signal Processing in Medicine and Biology Symposium (SPMB), pages-1-5, December-2022.- doi:-10.1109/SPMB55497.2022.10014835-

Chapter 2

Literature Review

Although-EEG-is-currently-not-used-as-part-of-the-diagnostic-process-of-neurodegenerative-diseases-such-as-AD,-its-potential-for-characterisation-and-diagnosis-has-recentlygained-attention-in-research-[19].- In-contrast-to-other-neuroimaging-methods-such-as-CT,-fMRI-and-PET,-EEG-offers-an-excellent-temporal-resolution-(on-the-scale-of-milliseconds)-but-suffers-from-relatively-low-spatial-resolution.- An-alternative-to-EEG-is-MEG,-which-maintains-a-comparable-temporal-resolution-and-allows-for-higher-spatial-resolution.- However,-EEG-is-considerably-cheaper-and-more-portable-than-MEG,making-it-an-ideal-candidate-for-developing-an-economical-and-accessible-tool-for-thediagnosis-of-AD.-

EEG-records-the-gross-sum-of-electrical-potentials-generated-by-neural-assembliesin-cortical-and-sub-cortical-areas-[204]. However, the positioning of EEG-electrodeson-a-subject's-scalp-will-likely-emphasise-the-contribution-of-cortical-regions-to-thesignals-measured-by-EEG. EEG-signals-are-typically-further-decomposed-into-severalfrequency-bands-corresponding-to-different-brain-rhythms. Namely-these-are- δ , θ , α , β and γ bands. Different-processes-in-the-brain-generate-each-frequency-band. Generally, high-frequencies-are-related-to-local-communication, while-low-frequenciessupport-communication-between-distant-regions-[266,-231].

Various-alterations-of-these-brain-rhythms-have-been-reported-in-AD-using-electrodelevel-methods-[114,-9,-139,-221,-222,-227,-200]. This-category-of-EEG-analysis-typicallyquantifies-the-alterations-on-a-single-electrode-level-without-considering-pairwise-interactions. These-patterns-of-brain-oscillatory-rhythms-are-reviewed-in-section-2.1.

Network-neuroscience-extends-the-analysis-of-brain-oscillations-to-quantify-interactions-between-brain-regions.-Such-interactions-can-be-reconstructed-from-neuroimagingdata-using-connectivity-analysis.-Specifically,-three-types-of-connectivity-can-be-typically-reconstructed: functional (FC), structural (SC) and effective (EC). FC-measuresstatistical dependency between pairs of signals indicating functional interaction and is the main focus of this thesis [231]. SC-quantifies the physical connection between neuronal populations and brain regions. However, EEG signals do not contain any information about brain structure; thus, SC-is not applicable. Finally, EC, considered a subcategory of FC, measures the causality or flow of information between regions.

Upon-selecting-an-appropriate-connectivity-measure,-a-brain-graph-can-be-reconstructed-from-EEG-by-computing-the-connectivity-between-all-pairwise-combinationsof-available-electrodes.-In-section-2.2,-a-typical-pipeline-for-reconstructing-brain-graphsfrom-EEG-is-reviewed-with-a-focus-on-common-FC-measures,-brain-graph-preprocessingand-graph-measures.-

Then, graph-level-patterns-related-to-AD-are-reviewed-in-section-2.3-together-withvarious-ML-and-DL-methods-for-utilising-graph-information-for-automated-diagnosisof-AD.- Among-these-classification-methods, GNNs-emerge-as-a-powerful-method-forlearning-on-graph-structured-objects-such-as-EEG-based-brain-graphs.- Thus, GNNsmodels-proposed-for-various-EEG-classification-tasks-are-reviewed-in-section-2.4.-

2.1 Brain Oscillation Changes in Alzheimer's disease

This-section-reviews-the-findings-on-brain-oscillation-changes-induced-by-AD.-Brain-oscillations-influence-the-timing-of-individual-neuronal-firing-on-a-microscopic-level-whilecoordinating- the-interaction- among- widely- dispersed- cortical- networks- on- a-macroscopic-scale-[302].- Signals-recorded-by-EEG-can-then-be-characterised-in-the-time-orfrequency-domains-to-study-the-oscillatory-activity.-

Identification of oscillations in EEG measurements is typically computed across different EEG channels, i.e. electrodes, either in isolation or by obtaining a grand-averaged signal of the whole brain or a particular region of interest. These oscillatory patterns are typically analysed in frequency bands, thus allowing the study of the processes linked to low-frequency and high-frequency oscillations in isolation. Five canonical frequency bands are defined for EEG signals: $\delta (0.5-4Hz)$, $\theta (4-7Hz)$, $\alpha (7-15Hz)$ and $\beta (15-31Hz)$. It has been shown that each band supports various cognitive functions, although some functions do not fit the canonical definition of frequency bands.

Generally, low-frequency oscillations enable long-range global neural communication, while high-frequency oscillations support local communication [231, 266]. Forinstance, δ rhythm becomes dominant during sleep and θ oscillations in the frontal region are linked to inhibitory regulation of other regions, memory and executive function [117]. α band is related to memory and temporal attention [105], β is linked to motor planning, imagery and execution [199], and γ is related to conscious information processing [232] and active memory [109].

Healthy- ageing- is- characterised- by- progressive- changes- in- brain- wave- frequency, power, and distribution-during-rest-[121].- In-particular, healthy- ageing-is- associated-with-an-increase-of-power-in- δ and θ bands-[222]-and-slowing-down-of-dominant-activity-of- α band-[121].- Cognitive-decline-related-to-neurodegeneration-further-enhances-the-alterations- of- brain- oscillatory- activity- [193].- The-hallmark- EEG-based- biomarker-of-AD- is- the-slowing-down-of-brain-signals.- This- is-manifested- by- the-reduction-of-the-power-of-high-frequency-rhythms- and- an-increase- in-the-power-of-low-frequency-components-[114,-9,-139,-221,-222,-227].-

A-global- δ power-increase-has-been-observed-in-AD-[49,-11,-46]-whereas- θ power-increase-is-limited-to-central-and-occipital-regions-[47,-140]. Reduced- α power-has-been-observed-in-occipital, parietal- and-temporal-regions-[11,-179,-157,-140]. Similarly, reduced- β power-has-been-detected-in-central, frontal-and-occipital-regions-[140]. Findings-related-to- γ band-changes, such-as-power-and-synchronisation, are-considered-controversial-due-to-their-inconsistency-[101], with-some-studies-reporting-a-decrease-[148,-239]. In-contrast, others-report-an-increase-of- γ [20,-275,-221]. Interestingly, an-increase-in- γ CFC-in-AD-has-been-suggested-to-be-linked-with-a-compensatory-mechanism-for-the-increased-need-for-resources-due-to-network-disruptions-[275].

Slowing-down-of-EEG-signals-has-also-been-shown-to-be-a-potential-indicator-ofconversion-from-mild-cognitive-impairment-(MCI)-stage-to-AD-[102].-The-ratio-of- θ and- γ correlates-with-AD-conversion-and-decreased-memory-test-scores-[219,-192].-Changesin-power-also-correlate-with-several-biomarkers-of-AD-and-cortical-neurodegeneration.-There-is-a-correlation-between-cerebrospinal-fluid-based-biomarkers-such-as-A β ,-p-tauand-t-tau,- and-global-power- of- δ ,- θ ,- α and- β frequency-bands-[233].- Studies-alsoreport-a-link-between-volumetric-neurodegeneration-[10,-193],-with-occipital- α powercorrelating-with-occipital-grey-matter-density-[12,-87].-

Based-on-these-oscillatory-patterns-of-AD-cases,-multiple-attempts-to-design-MLand-DL-based-classification-models-have-been-published.- support-vector-machine-(SVM)-classifier-has-been-trained-on-time-frequency-domain-[188]-and-wavelet-transform-features-extracted-to-distinguish-between-AD-and-HC-cases-[154].-Next,-multiplestudies-on-using-artificial-neural-networks-have-been-published.-

Raw-EEG-signal-can-be-used-as-an-input-to-a-neural-network-to-classify-AD-[62].-In-[7],-the-EEG-signal-from-a-single-EEG-electrode-is-transformed-into-a-visibility-graphand-classified-using-a-neural-network.- Alternatively,-a-neural-network-can-be-trained-onfeatures-derived-from-wavelet-transform-and-short-time-Fourier-transform-[218].- Someapproaches- have- been- developed- to- transform- EEG- signals- from- multiple- electrodesinto- images- to- leverage- the- image-classification- advantages- of- CNNs.- power-spectraldensity-(PSD)-vectors-across-all-electrodes-are-computed-and-stacked-to-form-an-inputmatrix,-i.e.- image,- and-fed-to- a- CNN- [118].- In- [115],- wavelet-transform-matrices- ofmultiple-electrodes-are-used-as-tiles-to-create-an-input-image-to-a-CNN-by-arrangingthe-tiles-according-to-the-spatial-positions-of-corresponding-electrodes.-

A-significant-limitation-of-these-classification-approaches-is-the-lack-of-incorporatinginformation-about-relationships-between-EEG-electrodes.- Network-based-(i.e.- graphbased)- approaches- seek- to- address- this- limitation- by- using- connectivity- methods- tomodel-these-interactions.-

2.2 Graph-based EEG Analysis

Graph-based-approaches-for-modelling-EEG-signals-aim-to-utilise-the-information-fromall-available-electrodes-by-considering-the-complex-pairwise-interactions.- This-sectionreviews-the-core-steps-in-the-pipeline-of-graph-based-approaches.- First,-the-methodsfor-reconstructing-brain-graph-structure-from-EEG,-i.e.- FC-measures,-are-reviewed.-Then,-the-methods-for-graph-preprocessing-are-reviewed.- Finally,-we-review-the-mostused-graph-metrics-for-characterising-brain-graphs.-

2.2.1 Graph Inference via functional connectivity

There-is-no-consensus-on-how-the-edges-of-a-brain-graph,-i.e.- connectivity,-should-beinferred-from-EEG.- In-the-case-of-EEG,-this-connectivity-is-referred-to-as-FC-as-theedges-capture-merely-information-about-statistical-dependency-between-nodes-[201].-This-is-in-contrast-to-structural-connectivity,-which-models-the-physical-connectionsbetween-brain-regions,-e.g.- white-matter-fibres-[23].- Although-FC-does-not-indicate-aphysical-connection-between-brain-regions,-it-still-describes-an-interesting-property-ofthe-brain-as-it-has-been-shown-that-synchronised-EEG-oscillations-of-two-distant-brain-

	Linear-	Nonlinear-	Time-Domain-	Frequency-Domain-	Phase-	Amplitude-	Cross-frequency-
Pearson's-correlation-coefficient-(PCC)-	1		1				
Coherence-(COH)-	1			✓	1		
Wavelet-coherence-(WCOH)-	1	1		✓	1		
Partial-Coherence-	1			✓	1		
Amplitude-envelope-correlation-(AEC)-	1					1	✓
Imaginary-part-of-coherency-(iCOH)-	1			✓	1		
Phase-lagged-index-(PLI)-	1	1		✓	1		
Weighted-phase-lagged-index-(wPLI)-	1	1		✓	1		
Mutual-Information-(MI)-	1	1	1	✓			
Transfer-Entropy-	1	1	1				
n:m-Phase-synchronisation-	1	1		✓	1		
Phase-locking-value-(PLV)-		1			1		1
Mean-Vector-Length-	1	1			1	1	1
Modulation-Index-	1	1			1	1	\checkmark
Cross-bispectrum-(CBS)-	1	1		✓	1	1	1

Table 2.1: Categorisation of methods for estimating FC

regions-indicate-a-functional-interaction-[231].-

FC-can-be-divided-into-two-categories:-directed-and-undirected-[27,-24].- Directed-FC-is-referred-to-as-effective-connectivity-and-models-the-causal-effects-that-nodes-haveon-each-other.- On-the-other-hand,-undirected-FC-models-the-dependencies-but-not-thedirectionality-of-information-flow.- This-review-focuses-on-undirected-measures-of-FC.-

The simplest method for estimating FC-is Pearson's correlation and is often used with different types of neuroimaging [220, -33] including characterising AD-[276]. However, EEG signals are typically non-stationary and exhibit complex nonlinear interactions; thus, correlation is not a well-suited method for use with EEG as it captures only linear relationships and assumes stationarity. Thus, other methods are commonly employed to estimate FC, which consider the interactions' complexity. The various FC methods are listed in Table 2.1. The FC methods are categorised based on whether they measure linear or nonlinear dependencies, whether they are computed in the time domain or frequency domain, which property of EEG signal they measure, and whether cross-frequency coupling can be measured.

Although-the-brain-signals-are-nonlinear,-many-linear-methods-based-on-correlationare-a-popular-choice-for-FC-estimation.- An-extension-of-correlation-to-frequency-domainis- coherence,- measuring- phase- synchronisation- of- two- signals- [4,-69,-248].- Similarly,correlation-is-extended-to-measure-relationships-between-amplitudes-of-the-signals,-i.e.envelope-correlation- [60].- Typically,- these- methods- rely- on- the- Hilbert- transform- toextract-the-instantaneous-phase- and-amplitude- of-the-EEG-signal.-

The limitations of coherence can be resolved by using wavelet transform to obtain wavelet coherence, which is sensitive to nonlinear relationships in addition to linear [127]. However, the inferred FC can be a result of an indirect relationship, e.g. two signals are related via a third signal, partial coherence attempts to resolve this issue by removing-linear-effects-of-all-other-signals-[18].- The-imaginary-part-of-coherence-canalso-be-used-as-it-removes-zero-lag-dependencies-and-thus-is-well-suited-for-sensor-level-EEG-FC,-which-can-suffer-from-volume-conduction,-i.e.- spatial-information-leakagebetween-adjacent-EEG-electrodes-[203].-

Similar to coherence, the phase lag index family of FC methods aims to measure phase synchronisation [241], which utilises asymmetries of the probability distribution of differences between phases of two signals and thus can capture nonlinear relationships. Weighted phase lag index incorporates the imaginary part of coherence by using it-to-weight the phase lags [265], resulting in more robust FC estimates with respect to noise. An interpretation might be difficult as it mixes information about the magnitude and consistency of the phase.

The last common family of methods to infer FC are based on information theory:mutual information [129] and transfer entropy [189]. Mutual information estimates FC as the amount of information about one signal explained by another signal and vice versa, utilising their marginal and joint probability distributions. It has been shown that mutual information can capture both linear and nonlinear dependencies [129,-119].

However, all of the FC-methods introduced above share one major limitation: they rely on splitting EEG signals into frequency bands, which are subsequently analysed in isolation. We refer to these types of FC as WFC as the inferred interactions can occur only between signals within the same frequency band. Recently, there has been increasing evidence that brain signals become entangled across frequency bands, giving rise CFC [125]. CFC is hypothesised to be the underlying mechanism of interaction of local and global processes [135], thus facilitating the integration of information, which is one of the essential properties of the brain. Hence, accounting for WFC and CFC is critical when studying brain networks but has been largely ignored in FC and NWliterature.

Both-WFC-and-CFC-are-generally-quantified-as-coupling-between-two-componentsof-EEG-signals, such-as-phase-to-phase, amplitude-to-amplitude, and-phase-to-amplitude. Other-coupling-types-were-documented-but-poorly-understood-and-thus-omittedin-this-review, e.g. phase-frequency-[125]-and-amplitude-frequency-[282]. Most-of-thefollowing-measures-are-not-FC-measures-per-se-but-can-be-easily-adopted-as-such.

Amplitude-amplitude-coupling-is-most-commonly-studied-using-amplitude-envelopecorrelation-described-above-[39,-74]-and-is-usually-observed-between-high-frequencyrhythms.-n:m-phase-synchronisation-is-used-for-quantifying-phase-phase-coupling-[268,-226,-58]-and-is-the-only-CFC-measure-that-has,-to-the-best-of-our-knowledge,-beenused-as-FC-measure-[42].-

Phase-amplitude-coupling-refers-to-a-coupling-where-the-phase-of-a-low-frequencysignal-is-coupled-with-the-amplitude-of-a-high-frequency-signal- and-is-possibly-themost-studied-type-of-CFC-as-it-has-been-demonstrated-to-occur-frequently-both-inhuman- and- animal-brains- [194,-258].- Specifically,- $\theta - \gamma$ phase-amplitude-couplingplays- a-crucial-role- in-multiple-cognitive-processes- such- as-perception,- learning- orcomputation- [125,-44,-45].- Multiple-phase-amplitude-coupling-measures-are-reportedin-the-literature,-such-as-mean-vector-length,-phase-locking-value-and-modulation-index-[116].-

2.2.2 Graph Pre-processing

In order to reconstruct the brain graph structure from EEG, a chosen FC measure is computed for all pairwise combinations of available EEG channels. Since FC(x, y) = FC(y, x), given N channels, this results in a fully connected graph with $\frac{N(N-1)}{2}$ edges. However, using a fully connected graph for further analysis can pose several issues: (1) false positive edges and (2) graph measures calculating unweighted shortest paths are invalid.

The former can stem from multiple reasons, such as signal-noise, volume conduction or spurious coupling. These issues can be controlled by appropriate signal preprocessing, selecting a robust FC measure and using false positive corrections such as surrogate testing. The latter can be addressed only by transforming the fully connected graph to a sparse version of itself, i.e. discarding a certain number of edges. The choice of graph preprocessing method is crucial, especially for unweighted graph analysis, i.e. edges do not have a strength, as it might alter the graph structure significantly. Some studies omit the graph preprocessing step and analyse the fully connected graphs obtained by chosen FC measure [306, 186]. Despite the limitations described previously, an advantage of this method is obtaining the same number of edges for all graphs, thus making group comparisons unbiased.

A simple-graph-filtering-method-is-choosing-a-specific-threshold-value-of-connectivityand-removing-any-edges-that-are-below-this-threshold-[273,-262,-172,-225].- Such-amethod-requires-a-normalised-FC-measure-to-establish-a-meaningful-threshold-value.-However,-the-resulting-graphs-can-have-varying-densities,-i.e.-the-number-of-edges,-andbecome-disconnected-such-that-a-node-cannot-be-reached-from-all-other-nodes.- Thus,comparisons-of-such-graphs-might-be-difficult-and-biased.- Many studies opt instead for a data-driven graph preprocessing method. Edgedensity thresholding is a popular and straightforward approach [5, 271, 123, 236, 190, 294, 122, 42]. This approach establishes a certain edge density level for each graph by keeping the top x% strongest edges. It is, however, challenging to determine the optimal edge density value. Typically, the analysis is repeated with multiple edge densities to prove that the results are independent of the edge density value. Alternatively, the median FC value can be used [295]. A drawback of the edge density threshold is that the actual minimum FC value will differ between graphs. Additionally, this method does not prevent graph disconnection, especially at low edge densities. The number of edges remains fixed across all graphs, provided they have the same number of nodes, thus making comparisons unbiased.

The orthogonal-MST-(OMST)-method-has-been-proposed-to-solve-the-limited-number-of-edges-of-MST-[78,-79]. OMST-is-an-iterative-extension-of-MST. The first-iterationequals-an-MST, and the selected-edges-are-removed-from-the candidate-set-of-edges. The MST-algorithm-is-then-run-again, repeating-the-step-until-the desired-numberof-iterations-is-achieved. Thus, I iterations-of-OMST-yield-a-graph-with-I(N - 1)edges. OMST-thus-combined-the-advantages-of-MST-and-edge-density-methods, i.e.guarantee-of-a-connected-graph-and-fixed-number-of-edges.

2.2.3 Graph Measures

There-are-various-ways-to-quantify-the-properties-of-a-graph.- This-subsection-reviewsthe-measures-based-on-graph-theory-commonly-used-in-brain-graph-analyses.- Graphmeasures-can-be-divided-into-node-level-and-graph-level.- Node-level-measures-can-becomputed-individually-for-each-node,-thus-allowing-one-to-evaluate-the-importance-ofeach-node-in-the-context-of-the-entire-graph.- In-contrast,-graph-level-measures-characterise-the-graph-as-a-whole-by-a-single-value.- Besides-graph-theory-based-measures,-onecan-analyse-and-compare-graphs-by-summarising-the-adjacency-matrix-via-descriptivestatistics-or-performing-edge-wise-comparisons.-Such-approaches-are,-however,-infeasible-with-large-graphs-as-the-number-of-comparisons-grows-too-large.-

Standard-node-level-measures-used-in-brain-graph-literature-are-node-degree-(ND),node-strength-(NS),-clustering-coefficient-and-betweenness-centrality.-ND-is-defined-asthe-sum-of-edges-of-a-given-node,-thus-giving-a-rudimentary-measure-of-node-centralitysince-a-more-connected-node-implies-more-information-flows-through-it-[165].-NS-is-theweighted-extension-of-ND,-i.e.- the-sum-of-edge-weights-of-a-given-node,-and-having-asimilar-interpretation-[106,-84].-

The clustering coefficient measures the tendency of a node to form clusters with other nodes [273, -172, -52, -84]. The clustering coefficient of node *i* is computed as follows:-

$$C_i = \frac{1}{\mathrm{ND}_i(\mathrm{ND}_i - 1)} \sum_{jk} \mathbf{A}_{ij} \mathbf{A}_{jk} \mathbf{A}_{ki}, \qquad (2.1)$$

where **A** is the adjacency matrix. The average clustering coefficient can be used to assess the degree of information segregation of a graph, a crucial property of the brain [223].

Finally, betweenness centrality (BW) is a measure of node importance in terms of the influence the node has on information flowing through the graph [122, -42]. BW of node *i* is computed as follows

$$BW(i) = \sum_{i \neq j \neq k} \frac{d_{jk}(i)}{d_{jk}},$$
(2.2)

where g_{jk} is the total number of shortest paths between nodes j and k, and d_{jk})(i) is the total number of d_{jk} passing through node i.

Commonly-used-graph-level-measures-are-average-path-length,-local-efficiency- (E_L) ,-global-efficiency- (E_G) - and-small-worldness.- Average-path-length-quantifies- the-efficiency-of-information-transport-throughout-the-graph-[273,-262,-156].- It-is-defined-as-the-average-length-of-all-possible-paths-between-all-pairs-of-nodes.-

 E_G measures-the-information-integration-across-the-entire-graph-[273,-172,-5,-186,-93].-It-is-computed-as-

$$E_G(G) = \frac{1}{N(N-1)} \sum_{i \neq j \in G} \frac{1}{d(ij)},$$
(2.3)

where N is the number of nodes in network G and d(ij) is the shortest path length

between-nodes-i and j.

 E_L measures-the-information-segregation-in-the-graph-[273,-5,-123,-42]-and-is-computed-as-follows:-

$$E_L(G) = \frac{1}{N} \sum_i E_G(G_i), \qquad (2.4)$$

where G_i is the subgraph containing node *i* and its neighbours.

A-small-world-graph-is-a-graph-with-high-clustering-and-short-distances-betweennodes, i.e., neighbouring-nodes-tend-to-connect-with-similar-nodes, and-each-node-canbe-reached-via-a-relatively-short-path-from-any-other-node. Small-worldness-measureshow-close-to-a-small-world-graph-the-given-graph-is [273, 180, 42].

A-particular-case-of-graph-measures-are-measures-of-vulnerability.- These-measurescompute-the-change-of-a-graph-level-measure-after-a-node-is-removed.- In-other-words,vulnerability-measures-quantify-the-importance-of-the-removed-node-to-facilitate-thegiven-property-of-a-graph.- For-example,-characteristic-path-length-vulnerability-hasbeen-previously-used-to-characterise-brain-graphs-[273].-

Additional-measures- can- be- employed- to- characterise- a- graph- structure,- such- asvarious- graph- complexity- measures- and- alternative- node- centrality- measures.- However,- the- graph- measures- described- in- this- section- are- the- most- commonly- used- tocharacterise-brain-graphs.-

2.3 Graph-based Alzheimer's disease patterns

This-section-reviews-AD-disruptions-from-a-graph-perspective.-First,-global-changes-in-FC-are-reviewed.-Next,-AD-disruptions-expressed-as-global-level-graph-measures-are-examined.-Then,-we-examine-the-regional-changes-in-brain-graphs-of-AD-cases.-The-changes-related-to-conversion-from-MCI-stage-to-AD-are-also-reviewed.-Finally,-graph-MLclassification-approaches-are-summarised.-

2.3.1 Global changes in functional connectivity

As discussed in Section 2.1, brain oscillatory changes due to AD are observed as a decrease in high-frequency activity and an increase in low-frequency activity. A similar pattern can be observed in the global average FC strength of AD brain graphs. Average FC strength is reduced in the α frequency band [71, 165, 238, 273, 286, 297] and β frequency band [71, 165, 238, 273, 286]. Moreover, the network structure in α of AD

cases has been reported to disintegrate under eyes open (EO)-[65]. A whole-scalp hypoconnectivity of long-range connections independent of a frequency band has also been reported [236]. In contrast, average FC-strength in θ is increased in AD cases [297].

Interestingly, it has been demonstrated that α connectivity, measured by AEC, increases after AD patients have been administered medication to reduce cognitive symptoms [34]. This suggests a plausibility of using FC based approaches for monitoring and evaluation of AD treatments.

There-is-also-some-evidence-that-whole-scalp-CFC-is-disrupted-in-AD-brain-graphs-[42,-79].- Mean-phase-phase-CFC-is-negatively-correlated-with-mean-WFC-in-AD-[42].-However,-a-detailed-examination-of-combined-WFC-and-WFC-brain-graphs-is-necessaryto-characterise-the-more-complex-AD-related-disruptions.-

2.3.2 Changes in Global-level Graph Metrics

The most studied properties of brain graphs are related to information integration across the entire graph and information segregation, i.e., the presence of specialised and localised information processing units. E_G is one of the measures of information integration. Decrease of E_G values has been reported in AD brain graphs [297, 5, 186, 93]. Moreover, this decreased information integration in α band correlates with verbal fluency test scores [52]. Average path length further supports decreased integration in AD graphs. Its inverse is related to E_G . Thus, an increase in average path length observed in AD graphs translates to lower information integration [186, 156]. An increase in average path length has also been observed in CFC multi-layer graphs where each frequency band is represented as a separate layer [42].

Findings-related-to-information-segregation-in-AD-brain-graphs-are-not-as-clear.-However,-the-evidence-seems-to-accumulate-in-favour-of-a-decrease-[5,-93,-296,-186,-156,-52,-2]-rather-than-an-increase-[123].-Both- E_L and-the-clustering-coefficient-can-be-used-to-quantify-the-segregation-of-a-graph.-One-study-reports-an-increase-of- E_L [123].-In-contrast,-multiple-studies-using-various-FC-measures-to-reconstruct-brain-graphs-report-reduction-of- E_L [5,-93,-296].-Characterisation-of-information-segregation-in-AD-measured-with-clustering-coefficient-is-more-consistent-with-all-studies-indicating-decreased-values-[186,-156,-52,-296,-2].-Specifically,-reduced-average-clustering-coefficient-can-be-found-in- α [52,-296,-2]-and- β [2]-frequency-bands.-Furthermore,-this-decrease-in- α clustering-coefficient-correlates-with-Mini-Mental-State-Examination-(MMSE)-score-[93]-and-score-of-verbal-fluency-[52].- AD-brain-graphs-have-also-been-shown-to-have-reduced-modularity-[123], whichmight-be-in-conflict-with-the-clustering-coefficient-findings. Lower-average-node-degreehas-also-been-reported-in-AD-graphs-[93]. Overall, it-seems-that-AD-graphs-are-furtherfrom-optimal-small-world-graphs, with-multiple-studies-reporting-reduced-small-worldindexes-[240, -261, -273, -295, -156]. This-pattern-seems-to-reverse, however, when CFCinformation-is-included-in-the-reconstructed-graph-[42].

AD-graphs-have-also-been-reported-to-be-more-homogeneous-[295],-less-robust-[66],and-more-vulnerable-than-their-HC-counterparts-[261,-273,-2,-5].-Increased-vulnerabilityof-AD-graphs-in- α and- β frequency-bands-has-been-demonstrated-by-quantifying-theeffect-of-node-removal-on- E_G values-[5].- However,-the-differences-in-vulnerability-of-CFC-graphs-remain-unclear.-

2.3.3 Regional Changes of Brain Graphs

Multiple localised graph disruptions in AD have been reported. An overall loss of network organisation has been observed in parietal and occipital areas [297]. Similarly, the average wPLI strength is reduced in α and β bands in occipital and orbitofrontal regions [165].

Coherence- between- hemispheres- in- these- frequency- bands- is- reduced- as- well- infrontal, -temporal-and-parietal-lobes-[91,-90,-147,-310]-which-reflects-the-general-loss-oflong-distance-connectivity- in- AD- [237].- Intrahemispheric-coherence- is-also- disruptedbetween-central-and-occipital-regions-in- δ band-[147,-310].- The-strength-of-edges-withinthe-frontal-lobe- and- between-left-frontal- and-right-occipital-regions- have- been-shownto-be-strong-predictors-of-AD-[236].- Additionally,-the-information-flow-from-posteriorto-anterior-regions-is-reduced-in-AD-[85].- In-contrast,-central-to-posterior-informationflow-is-increased-in-AD-

2.3.4 Graph Biomarkers of Alzheimer's Disease Progression

A-few-studies-propose-methods-to-automatically-classify-MCI-cases-that-will,-over-time,convert-to-AD-[212,-288,-185].- A-whole-scalp-decrease-of-functional-dissimilarity-(canbe-considered-an-inverse-of-FC)-in- δ and- θ frequency-bands-have-been-identified-aspredictors-of-MCI-AD-conversion-[185].-

Region-specific predictors of MCI-AD conversion have been identified using MIin α frequency band across temporal, parietal and frontal lobes [288]. Furthermore, differences in the parahippocampal cortex have been suggested to be linked to the degradation-of-visual-memory-[288].-

Node-level-graph-metrics-also-reveal-various-AD-related-alterations. An informationhub-of-a-graph-located-in-the-frontal-lobe-is-damaged-in-AD- [236]. Reduced-hubstrength-in-the-central-area-has-also-been-observed-in-AD-when-performing-a-cognitivelydemanding-task-[65].

Furthermore, lower NDs and clustering coefficients across all frequency bands infrontal and orbitofrontal areas show further evidence of damaged hubs in these regions [165]. Reduced clustering coefficients have also been reported in δ - β CFC in parietal, occipital and temporal regions [43].

2.3.5 Graph ML for Alzheimer's Disease Diagnosis

Multiple-ML-classifiers-have-been-proposed-to-use-features-extracted-from-reconstructedbrain-graphs-to-diagnose-AD.- Classifiers-trained-using-graph-measures-are-a-popularchoice-in-the-literature-with-methods-such-as-SVM[225,-123,-295,-236,-1,-43,-43],-MLP-[225],-linear-discriminant-classifier-[5]-and-fuzzy-network-classifier-[296].-

Discriminatory-electrodes-have-been-identified-predominantly-in-parietal-and-occipital-regions-[225].- The-SVM-based-approach-has-even-been-extended-to-the-3-wayclassification-of-AD,-MCI,-and-HC-using-node-degree-features-[1].-

The predictive utility of multiplex brain graphs has also been tested. Multiplexgraphs are constructed such that a layer represents each frequency band, and interlayer edges are inserted to connect the same electrodes across layers. Using such graph construction method, SVM has been trained with multiplex clustering coefficient as features [43].

Finally, one study has demonstrated the importance of linear and nonlinear FCgraphs. Comparisons of k-nearest-neighbour classifiers trained using linear and mixed (linear and nonlinear) FC values show that mixed FC performs significantly better [306]. In this section, GNN-based methods have been omitted since those methods require a detailed review to elucidate how such methods should be utilised for ADclassification.

2.4 Graph Neural Networks for EEG Classification

¹GNNs-emerge-as-a-powerful-tool-for-modelling-EEG-data-[167]-within-the-NW-framework.- GNNs-are-specifically-designed-to-operate-on-graph-structured-data.- They-caneffectively-leverage-the-spatial-structure-within-EEG-data-to-extract-features,-uncoverpatterns,- and- make-predictions- based- on- complex- electrode- interactions.- Designing-GNN-models-for-EEG-classification-will-likely-improve-classification-tasks-and-potentially-uncover-new-insights-in-neuroscience.-

Motivated by the potential of GNNs and an increasing number of recent papers proposing GNN for various EEG classification tasks, there is an urgent need for a comprehensive review of GNN models for EEG classification. The main aims of this section include:

- Identifying-emerging-trends-of-GNN-models-tailored-for-EEG-classification.-
- Reviewing- popular- graph- convolutional- layers- and- their- applicability- to- EEG- data.-
- Providing-a-unified-overview-of-node-feature-and-brain-graph-structure-definitionsin-the-context-of-EEG-analysis.-
- Examining-techniques-for-transforming-sets-of-node-feature-embeddings-into-asingle-graph-embedding-for-graph-classification-tasks.-

This review will provide a comprehensive and in-depth analysis of the application of GNN-models for EEG classification by addressing these essential aspects. The findings and insights gained from this review will identify promising future research directions.

2.4.1 Overview of Graph Neural Networks

Graphs-are-widely-used-to-capture-complex-relationships-and-dependencies-in-variousdomains,- such-as- social- networks,- biological- networks,- and- knowledge- graphs.- Theproblem-of-graph-classification,- which-aims-to-assign-a-label-to-an-entire-graph,- hasgained-attention-in-recent-years.- GNNs-offer-a-promising-solution-to-this-problem-byextending-the-concept-of-convolution-from-Euclidean-inputs-to-graph-structured-data.-

¹The content presented in this section has been published in Dominik Klepl, Min Wu, and Fei He. Graph Neural Network-Based EEG Classification: A Survey. *IEEE Transactions on Neural Systems* and Rehabilitation Engineering, 32:493–503, 2024. ISSN 1558-0210. doi: 10.1109/TNSRE.2024.3355750

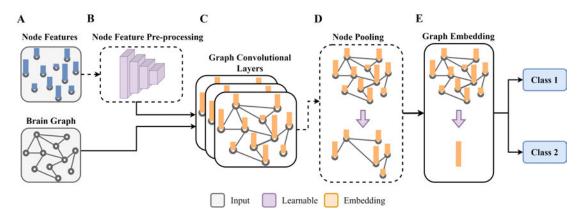


Figure 2.1: The general architecture of a graph neural network model for classification of EEG. (A) The input to the model consists of node features and a possibly learnable brain graph structure. (B) Optionally, the node features can undergo preprocessing via a neural network. (C) Next, the node features are passed to a block of graph convolutional layers, where node embeddings are learned. (D) Then, a node pooling module can be utilised to coarsen the graph. Node pooling may contain learnable parameters as well. (E) Finally, the node embeddings form a graph embedding, which can be used to predict the outcome.

GNNs-have-been-successfully-applied-in-a-wide-range-of-fields, such-as-biology [167], bioinformatics-[304], network-neuroscience-[26], chemistry-[280, 216], drug-design-and-discovery-[287, 243], natural-language-processing-[184, 283], recommendation-systems-[95, 284], traffic-prediction-[134, 182]-and-finance-[274].

In-graph-classification-problems, the input-is-a-set-of-graphs, each-with its own-set-ofnodes, edges, and node-features. Let G = (V, E, H) denote a featured-graph, where V represents the set-of-nodes, E represents the set-of-edges-connecting-the-nodes, and H represents the $V \times D$ matrix of D-dimensional-node-features. In the case-of-EEG, the EEG-channels are the nodes, and edges represent structural or functional connectivity between pairs of nodes. Each graph G is associated with a label y, indicating its class. The goal-is-to-learn a function $f(G) \to y$ that can predict the class-label y given an input-graph G. A general structure of a GNN-model for EEG classification is presented in Figure 2.1.

Multiple-types-of-GNNs-have-been-well-introduced-in-[285,-312].- In-this-survey,-webriefly-introduce-the-two-main-branches-of-GNNs,-namely,-spatial-and-spectral-GNNs-(Figure-2.2).- Other-types-of-GNNs,-such-as-attention-GNNs-GAT-[264],-recurrent-GNNs-[228],- and-graph-transformers-[230],- can-be-viewed-as-special-cases-of-spatial-GNNs,- and-thus-we-will-not-provide-detailed-discussion-in-this-survey.- Both-spatialand spectral-GNNs aim to extend the convolution mechanism to graph data. For a detailed review of their similarities and differences, see [55].

Spatial-GNNs-aggregate-information-from-neighbouring-nodes, similar-to-traditionalconvolution-applied-to-image-data-aggregating-information-from-adjacent-pixels. - Stacking-multiple-spatial-GNN-layers-leads-to-information-aggregation-from-various-scalesgoing-from-local-to-global-patterns-being-captured-in-early-and-later-layers, respectively.-In-contrast, spectral-GNNs-perform-information-aggregation-in-the-graph-frequency-domain, with-low-frequency- and-high-frequency- components- capturing- global- and-localpatterns, respectively.- However, both-approaches-learn-to-capture-local- and- globalpatterns-within-the-graph, i.e. - high-and-low-frequency-information-in-the-spectral-domain.- The-advantage-of-spectral-GNNs-is-their-connection-to-graph-signal-processing, allowing-for-interpretation-from-the-perspective-of-graph-filters.- However, spectral-GNNs-do-not-generalise-well-to-large-graphs-since-they-depend-on-the-eigendecomposition-of-graph-Laplacian.- In-contrast, spatial-GNNs-can-be-applied-to-large-graphssince-they-perform-only-local-message-passing.- On-the-other-hand, spatial-GNNs-maybe-challenging-to-interpret-and-prone-to-overfitting-because-of-over-smoothing, whereembeddings-of-all-nodes-become-similar.-

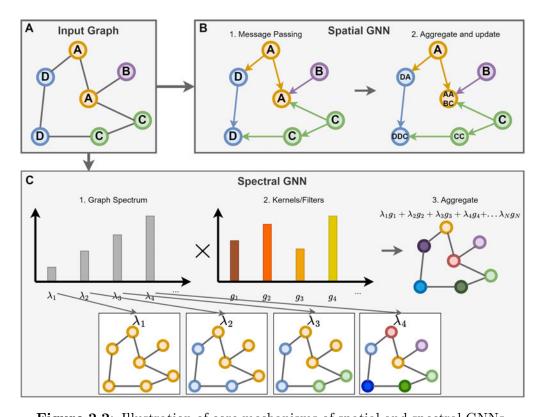


Figure 2.2: Illustration of core mechanisms of spatial and spectral GNNs. A) An undirected featured graph is given as an example input graph with node features. B) Spatial GNNs operate in the graph domain using message passing to update node embeddings. 1) Messages, i.e. transformed node features, are sent along edges. For simplicity, only one direction of the flow of messages is shown. 2) The collected messages at each node are aggregated using a permutation-invariant function and are fused with the original node embedding to form an updated node embedding. Thus, one spatial GNN layer results in node embeddings containing information about the 1-hop neighbourhood of a given node. Thus, L layers are required for node embeddings to access the information from the L-hop neighbourhood. C) In contrast, spectral GNNs operate in the graph spectral domain. 1) Node features are treated as signals on top of a graph and are deconstructed into graph frequencies given by the eigendecomposition of the graph Laplacian. Graph frequency can be interpreted as a variation of the signal. 2) The contribution of each graph frequency is weighted by the set of learnable kernels G, i.e. graph filters. 3) Node embeddings are obtained by aggregating the filtered graph frequencies and projecting them back to the spatial graph domain. Thus, full spectral GNNs can access information from N-hop neighbourhoods where N is the number of nodes of a given graph. However, in practice, approximations such as Chebyshev graph convolution (ChebConv) restrict this to the chosen hop size.

Spatial GNNs

Spatial-GNNs-directly-operate-on-the-graph-structure-via-the-adjacency-matrix-operator.-Given-a-set-of-nodes-and-associated-features, spatial-GNNs-perform-neighbourhoodaggregation-to-derive-node-embeddings.-This-process-is-referred-to-as-message-passing.-Intuitively,-nodes-connected-by-edges-should-have-similar-node-embeddings,-i.e.- localnode-similarity.- Message-passing-implements-this-idea-by-updating-node-embeddingswith-aggregated-information-collected-from-the-node's-neighbourhood.- Formally,-thenode-update-equation-in- l^{th} layer-of-spatial-GNN-with-L layers-is-defined-as-follows:-

$$h_i^{(l+1)} = \sigma \left(W_1^{(l)} h_i^{(l)} + \sum_{j \in \mathcal{N}(v_i)} W_2^{(l)} h_j^{(l)} e_{ji} \right), \qquad (2.5)$$

where h_i is the node embedding vector, or when l = 1, this is the input node feature vector. σ is the activation function, \sum is the aggregation function, $\mathcal{N}(v_i)$ is the neighbourhood of node $v_i, W \in \mathbb{R}^{d_1 \times d_2}$ is a learnable parameter matrix projecting node embeddings from input dimension d_1 to hidden dimension d_2 and e_{ji} is the edge weight $(e_{ji} = 1 \text{ for unweighted graphs})$.

A-single-spatial-GNN-layer-aggregates-information-from-the-1-hop-neighbourhood. Thus, to increase the reception-field of the model, L spatial-GNN-layers can be stacked to aggregate information from up to L-hop-neighbourhoods. A-disadvantage of spatial-GNNs- is the difficulty of training deep models with many layers. With an increasing-number of layers, the node embeddings become increasingly smooth, i.e. variance among embeddings of all nodes decreases. This happens when the messages already contain aggregated information from the whole graph; continual passing of such saturated messages leads to oversmoothing, i.e., all node embeddings becoming essentially identical.

Spectral GNNs

Spectral-GNNs-can-also-be-applied-to-EEG-classification-tasks-by-leveraging-the-spectral-domain-analysis-of-graph-structured-data. The-EEG-graph-is-transformed-into-thespectral-domain-using-the-Graph-Fourier-Transform-(GFT)-and-Graph-Signal-Processing-(GSP)-techniques. For-a-detailed-review-of-spectral-GNN-methods, please-refer-to-[30].

The graph spectrum is defined as the eigendecomposition of the graph Laplacian matrix. The GFT is then defined as $\hat{\mathbf{H}} = \mathbf{U}^T \mathbf{H}$, its inverse as $\mathbf{H} = \mathbf{U} \hat{\mathbf{H}}$, where \mathbf{U}

is the orthonormal matrix of eigenvectors of the graph Laplacian \mathbf{L} and $\mathbf{H} \in \mathbf{R}^{N \times D}$ is the matrix of node feature vectors with N and D being the number of nodes and dimensionality of node features, respectively. The graph Laplacian is defined as $\mathbf{L} = \mathbf{D} - \mathbf{A}$, but often the normalized version is preferred: $\hat{\mathbf{L}} = \mathbf{I} - \mathbf{D}^{-1/2} \mathbf{A} \mathbf{D}^{-1/2}$ (\mathbf{A} and \mathbf{D} are the adjacency and degree matrices, respectively).

Spectral-GNN-is-then-typically-defined-as-the-convolution-(*)-of-a-signal-defined-on-graph-**H** and-a-spatial-kernel-g in-the-spectral-domain,-thus-becoming-an-element-wise-multiplication- (\odot) :-

$$\mathbf{H} * g = \mathbf{U} \left(\left(\mathbf{U}^T \mathbf{H} \right) \odot \left(\mathbf{U}^T g \right) \right).$$
(2.6)

Generally, $\mathbf{U}^T g$ is defined as a learnable diagonal matrix $\mathbf{G} = -diag(g_1, ..., g_V)$ spectral-filter [30].

However, the full-spectral-graph-convolution-can-be-computationally-expensive. A-popular-approximation-is-the-ChebConv-[75], which-performs-localised-spectral-filtering-on-the-graph. The node-embedding-update-equation-of-a-ChebConv-is-defined-as:-

$$H * g \approx \sum_{i=1}^{K} \Theta_i T_i(\hat{\mathbf{L}}'), \qquad (2.7)^2$$

where $\Theta \in \mathbb{R}^{K \times d \times d}$ are learnable parameters, $T_i(\hat{\mathbf{L}}') = 2T_{i-1}(\hat{\mathbf{L}}') - T_{i-2}(\hat{\mathbf{L}}')$, $T_1(\hat{\mathbf{L}}') = T_{i-1}(\hat{\mathbf{L}}') - T_{i-2}(\hat{\mathbf{L}}')$, $T_1(\hat{\mathbf{L}}') = T_{i-1}(\hat{\mathbf{L}}')$, $T_1(\hat{\mathbf{L}}') =$

However, spectral-GNNs-are-limited-to-input-graphs-with-a-fixed-number-of-nodes. This-is-because-of-the-explicit-use-of-the-graph-Laplacian. This-is-in-contrast-to-spatial-GNNs, which-do-not-rely-on-explicitly-materialising-the-adjacency-matrix.

2.4.2 Survey Results

This-survey-is-based-on-a-review-of-63-articles.- These-articles-were-selected-by-titleand-abstract-screening-from-a-search-on-Google-Scholar-and-ScienceDirect-queriedon-November-1st,-2022.- The-search-query-for-collecting-the-articles-was-definedas:- ("Graph-neural-network"-OR-"Graph-convolutional-network")-AND-("Electroencephalography"-OR-"EEG").-Both-peer-reviewed-articles-and-preprints-were-searchedand-utilised.- All-types-of-EEG-classification-tasks-were-included.- We-summarise-thevarious-types-of-EEG-classification-tasks-identified-in-the-surveyed-papers-in-Fig-2.3.-The-most-common-classification-tasks-are-emotion-recognition,-epilepsy-diagnosis-and-

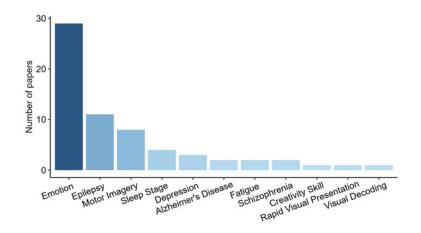


Figure 2.3: Classification tasks presented in the current EEG-GNN literature.

detection-and-motor-imagery.- However, the type of classification task should have a relatively minor effect on the GNN architecture design.- Thus, we do not analyse and discuss this in detail.- Instead, we survey the various GNN-based methods for EEG classification, intending to systematically categorise the types of GNN modules and identify emerging trends in this field independent of the specific classification task.

In the remaining portion of this section, we report the categories of comparisons we identified in the surveyed papers. These are based on the different modules of GNN-based models. Specifically, these are:

- Definition-of-brain-graph-structure-
- Type-of-node-features-
- Type-of-graph-convolutional-layer-
- Node-feature-preprocessing-
- Node-pooling-mechanisms-
- Formation-of-graph-embedding-from-the-set-of-node-embeddings-

2.4.3 Definition of Brain Graph Structure

The first part of the input to a GNN model is the brain graph structure inferred from the EEG data itself (Figure 2.1A). We summarise the methods for defining the

brain-graphs-in-Table-2.2.- These-methods-can-be-generally-categorised-as-learnable-or-pre-defined.-

An-alternative-categorisation-of-the-brain-graph-structures-is-the-functional-and-the-"structural"-connectivity.-Generally,-SC-graphs-are-pre-defined,-whereas-FC-graphs-canbe-both-pre-defined-and-learnable.-SC-in-the-classical-sense-of-physical-connectionsbetween-brain-regions-is-not-possible-to-obtain-using-EEG-signals-since-these-arerecorded-at-the-scalp-surface.-Instead,-we-use-the-term-to-describe-methods-thatconstruct-brain-graphs-based-on-the-physical-distance-between-EEG-electrodes.-Incontrast,-FC-refers-to-pairwise-statistical-relationships-between-EEG-signals.-

SC-graph-is-pre-defined-such-that-electrodes-are-connected-by-an-edge-in-the-following-way:-

$$e_{ij} = \begin{cases} 1 \text{-} \operatorname{or} \cdot 1/d_{ij}, & \text{if} \cdot d_{ij} \leq t \\ 0, & \text{otherwise} \end{cases},$$
(2.8)

where e_{ij} is the edge weight connecting nodes i and j, d_{ij} is a measure of distance between EEG electrodes, and t is a manually defined threshold controlling the graph sparsity.

Such an approach offers several advantages. First, the SC graph is insensitive to any noise effects of EEG recording since it is independent of the actual signals. Second, all data samples share an identical graph structure, provided the same EEG montage was utilised during the recording. This offers explainability advantages when combined with spectral GNN since the graph frequency components defined by the eigenvectors of graph Laplacian are fixed. On the other hand, the SC graph is limited to short-range relationships. Thus, it might not accurately represent the underlying brain network. Some papers propose to overcome this limitation by manually inserting global [83, -80, -308, -300, -54] or inter-hemispheric edges [311, -161, -289].

In-contrast, an-FC-graph-can-be-obtained-from-either-classical-FC-measures-(FC-measure-in-Table-2.2-or-learnable-methods-(e.g.-feature-concatenation/distance-and-attention-methods-in-Table-2.2). We-refer-to-all-of-these-methods-as-FC-because-they-all-measure-the-degree-of-interaction-between-two-nodes, thus-falling-within-the-traditional-definition-of-FC. Unlike-SC, the-FC-graph-is-unique-for-each-data-sample-and-can-contain-both-short- and-long-range-edges. On-the-other-hand, since-it-is-derived-directly-from-EEG-signals, it-might-be-noise-sensitive.

Learnable-FC-based-on-node-feature-distance-or-feature-concatenation-are-generally-

Method	Learnable-	Pre- defined-	Papers-
Distance-between- electrode-positions-	×	1	[311,-177,-77,-214,-249,-291,-242,-83,- 289,-124,-80,-308,-300,-130,-210,- 131,-54,-164,-133]-
Functional- connectivity-measure-	×	1	[178,-177,-155,-48,-28,-214,-8,-305,- 249,-53,-166,-99,-138,-272,-112,-113,- 124,-149,-130,-250,-270,-173,-16,-86,- 108,-131,-246,-142,-229]-
Manually-defined-	×	1	[311,-161,-83,-289,-308,-300,-54]-
Shared-learnable- mask-	1	×	[311,-160,-8,-166,-244,-303,-174,-290,- 16,-164]-
Feature-similarity-	1	X	[162,-161,-166,-80,-290,-164,-181]-
Feature-distance-	1	X	[132,-281,-301,-133]-
Transformer-style- attention-	1	×	[313,-170]-
Concatenation- attention-	1	×	[168,-173]-
Dense-projection-	1	X	[234,-235,-176]-
LSTM-based-	1	X	[81]-
Multiple/Combined- graph-definitions-	-	-	[250,-177,-48,-161,-214,-8,-166,-235,- 83,-289,-308,-290,-300,-130,-250,- 173,-16,-131,-54,-164,-133]-

Table 2.2: Overview of methods for obtaining the brain graph structure.

computed-as:-

$$e_{ij} = \theta_1(|h_i - h_j|) \text{ and }$$

$$(2.9)$$

$$e_{ij} = \theta_2(h_i \parallel h_j), \tag{2.10}$$

respectively, where $\theta_1(\cdot)$ -and $\theta_2(\cdot)$ -are-neural-networks-with-input-output-dimensions-of- \mathbb{R} : $d \to 1$ -and \mathbb{R} : $2 \times d \to 1$, respectively; $|\cdot|$ denotes-absolute-value; || denotes-concate-nation-and h_i is the node-feature/embedding-of-node-*i*. We discuss the attention-based-graphs-and-the-types-of-graph-convolutional-layers-in-Section-2.4.5-and-thus-skip-these-methods-in-this-section.

Special-cases of brain-graph-definition-are-the-shared-mask-methods. These-methodsdefined-a-matrix-of-learnable-parameters-with-the-same-shape-as-the-adjacency-matrixof-the-input-graphs-that-acts-as-a-mask/filter-by-multiplying-it-with-the-adjacencymatrix. This-learnable-matrix-is-a-part-of-the-model. Thus, the-same-mask-is-applied-

Method-	Time-	Frequency	Graph-	Depende
Method	domain-	domain-	domain-	Papers-
Differential-entropy-	1	×	×	[311,-162,-162,-161,-291,- 53,-166,-132,-281,-234,- 235,-83,-244,-272,-301,- 303,-124,-149,-308,-290,- 173,-313,-16,-170]-
Raw-signal- Fourier-Transform-	√ X	×	×	[77,-155,-48,-171,-8,- 307,-242,-166,-168,-112,- 113,-174,-80,-210,-250,- 270,-81,-86,-108,-54,- 164,-181,-133,-229]- [160,-240,-61].
	^	~	^	[160,-249,-61]-
Power-Spectral- Density/Band- Power-	×	1	×	[214,-303,-124,-149,-308,- 300,-130,-131,-246,-142]-
Graph-theory- metrics-	×	×	1	[178,-99]-
Descriptive- statistics-	1	×	×	[177,-300,-131]-

 Table 2.3: Overview of methods in defining the input node features

to-all-input-graphs. However, -a-shared-mask-limits-the-size-of-the-input-graphs, -i.e.the-number-of-nodes-must-remain-fixed-so-that-the-adjacency-matrix-can-be-multipliedwith-the-shared-mask.-

In-the-current-stage, the-preferred-method-for-brain-graph-classification-tasks-remains-unclear. Some-authors-attempt-to-avoid-this-issue-by-combining-multiple-methods. However, we instead-suggest-that-the-researchers-carefully-consider-each-of-thepresented-methods-in-the-context-of-the-given-classification-task, as-each-method-posesits-unique-set-of-strengths-and-weaknesses.

2.4.4 Node Feature Definitions

The second part of the input to a GNN-model is the node feature matrix (Figure 2.1A). We summarise the various definitions of node features in Table 2.3. We categorise these definitions based on which domain they are computed, i.e. time, frequency and graph domains.

The time-domain-methods are the most commonly used in the current literature. In particular, these are the differential entropy (DE) and raw signal methods. The

Method-	Trained- separately-	Papers-
1D-CNN-		[77,-162,-307,-168,-83,- 210,-81,-181]-
Feature-wise-attention- weighting-	×	[99]-
bidirectional-LSTM-	1	[112]-
Temporal-CNN-	×	[174,-80,-181]-
WaveletCNN-	×	[174]-
SincCNN-	×	[210]-
MLP-	×	[246]-
CNN-Feature-Extractor-	1	[133]-

Table 2.4: Overview of node feature pre-processing before GNN layers.

popularity-of-DE-is-given-by-the-fact-that-many-of-the-open-EEG-datasets-includethis-feature,-such-as-the-SEED-[309]-emotion-recognition-dataset.- DE-describes-thecomplexity-of-a-continuous-variable-and-is-defined-as:-

$$DE(X) = -\int_X f(x) log(f(x)) dx \qquad (2.11)$$

where X is a random continuous variable and f(x) is the probability density function.

Many-papers define the node feature as the raw EEG signal. However, the raw signal can be too long for a GNN-to-process effectively. Thus, it is often coupled with node feature preprocessing module and spatio-temporal GNNs (See 2.4.4 and 2.4.5 respectively) to either reduce the dimensionality or to extract the temporal patterns contained within the signal effectively. An alternative to the raw signal node feature is descriptive statistics, such as mean, median or standard deviation.

Frequency-domain-node-features-are-usually-defined-as-the-Fourier-frequency-components-obtained-by-the-Fourier-transform-or-the-power-spectral-density.- These-methods-attempt-to-quantify-the-strength-of-various-frequency-components-within-the-EEGsignal.- An-advantage-of-these-representations-is-their-relatively-low-dimensionalitycompared-to-the-raw-signal-described-previously.-

Finally, graph-theoretical-features-can-be-utilised-to-describe-the-nodes, e.g. meannode-weight-[178]- and- betweenness- centrality-[99,-178]. A-severe-limitation-of-thismethod-is-that-the-graph-structure-needs-to-be-defined-prior-to-node-feature-extraction.-Thus, this-node-feature-type-is-incompatible-with-learnable-brain-graph-methods.-

Node Feature Preprocessing

An optional next step after node features construction is some kind of node feature pre-processing module (NFP) (Figure 2.1B). We summarise the NFPs types in Table 2.4.

Most-of-the-NFPs-are-integrated-within-the-GNN-architecture,-thus-allowing-themodel-to-be-trained-in-an-end-to-end-manner.- The-exceptions-are-methods-that-utilisea-pre-trained-feature-extraction-neural-network-implemented-as-a-bidirectional-longshort-term-memory-(LSTM)-[112]-or-a-CNN-[133].-

The surveyed NFPs are all based on a neural network. In most cases, these are variants of a CNN and MLP. These modules aim to (1) reduce the dimensionality of the node features and (2) enhance the node features, including potentially suppressing noise or redundant information.

2.4.5 Type of Graph Convolutional Layer

A-core-part-of-a-GNN-model-are-the-GCN-layers-(Figure-2.1C).-We-summarise-theutilised-types-of-GCNs-in-Table-2.5.-We-further-categorise-them-based-on-the-type-of-GNN-as-introduced-in-Section-2.4.1,-i.e.- spatial,-spectral.- Additionally,-we-add-thetemporal-category,-which-is-not-a-type-of-standalone-GCN-layer-but-must-be-combinedwith-spatial-or-spectral-GCN.-

Interestingly, ChebConv-is-used-in-the-majority-of-the-surveyed-papers-(countingboth-ChebConv-and-spectral-spatio-temporal-GNN-in-Table-2.5). Since-EEG-typicallyuses-128-electrodes-in-high-density-montages, the-size-of-the-brain-graphs-is-relativelysmall.- In-such-cases, even- a-full-spectral-GNN-would-not-be-too-computationallyexpensive-for-EEG-classification.- Therefore, why-many-authors-opt-for-the-ChebConvapproximation-of-spectral-GNN-remains-unclear.- We-speculate-that-the-influenceof-classical-signal-processing-tools-in-EEG-analysis-might-also-serve-as-a-sufficientargument-for-using-spectral-GNNs-for-EEG-classification.-

On the other hand, the other half of the surveyed papers experiment with a wide range of spatial GNNs. The (simplified) GCN is a popular method amongst these, which is equivalent to a 1st-order ChebConv (K = -1). A special case of spatial GNN is the graph attention network (GAT). GAT allows adjusting the graph by re-weighting the edges using an attention mechanism. Generally, the attention mechanism for com-

Method-	Spatial-	Spectral-	Temporal-	Papers-
Graph-Isomorphism- Network-	1	×	X	[178,-77,-250]-
(Simplified)-Graph- Convolution-Network-	1	×	×	[311,-305,-307,-166,-83,- 244,-272,-289,-80,-300,-86,- 131,-142]-
Chebyshev-Graph- Convolution-	X	1	×	[155,-48,-214,-8,-291,-53,- 138,-301,-112,-303,-113,- 124,-149,-308,-130,-270,- 81,-16,-170,-246]-
Graph-Attention- Network-	1	×	×	[160,-99,-168,-210,-313,- 108,-54,-181]-
Diffusion-recurrent- gated-	X	1	×	[249]-
Spatio-temporal- GNN-(Spectral)-	×	1	1	[242,-61,-173,-229,-132,- 281]-
Spatio-temporal- GNN-(Spatial)-	\checkmark	×	1	[171,-164]-
Powers-of-Adjacency- Matrix-GNN-	1	×	×	[234,-235]-
GraphSAGE- Spectral-GNN-	√ X	×	X X	[77, -61]- [162, -161]-
B-Spline-Kernel- GCN-	✓	×	×	[177]-
Residual-GCN- Multibranch-	1	×	×	[174]- $[168, -301, -290, -300, -270, -$
architectures-	-	-	-	164]-

 Table 2.5: Overview of graph convolutional layers.

puting-the-new-softmax-normalised-edge-weight- e_{ij} is-defined-as-follows:-

$$e_{i,j} = \frac{\exp\left(\sigma\left(\mathbf{w}^{\top}[\mathbf{W}h_i \| \mathbf{W}h_j]\right)\right)}{\sum_{k \in \mathcal{N}(i)} \exp\left(\sigma\left(\mathbf{w}^{\top}[\mathbf{W}h_i \| \mathbf{W}h_k]\right)\right)},$$
(2.12)

where w and W are the learnable parameters of the model, σ is an activation function, h is the node feature vector/embedding, and N(i) is the set of nodes connected to node i. The resulting edge weights can then be passed to Equation 2.5.

Next, the spatio-temporal GNNs were tested for EEG classification in several instances. A spatio-temporal block consists of one GCN layer and one 1D-CNN applied temporally. This structure allows the model to extract both spatial (i.e. graph) and

Method-	Learnable-	Papers-
TopK-	1	[48,-54]-
Hierarchical-tree-pooling-	1	[178]-
SortPool-	1	[77]-
EdgePool-	1	[77]-
SAGPool-	1	[77,-289]-
Set2Set-	1	[77]-
Manual-Clustering-	×	[234, -235]-
Graclus-Clustering-	×	[113,-270]-

Table 2.6: Overview of node pooling mechanisms.

temporal patterns. There are both spatial and spectral variants of spatio-temporal GNN, and there is no indication as to which one should be preferred as no comparative study exists to date.

Finally, several papers adopt multi-branch architectures. These methods utilise multiple GCN-layers applied in-parallel-to-allow-the-model-to-focus-on-various aspects (also-views) of the input graph. An example of such a model utilises two-branch GNN to learn from both FC- and SC-based brain graph structure [164]. Alternatively, the individual frequency bands of EEG signals can be used to construct various graph views [246].

2.4.6 Node Pooling Mechanisms

In-some-instances, reducing-the-number-of-nodes-in-the-graph-might-be-desirable. Thiscan-be-achieved-with-a-node-pooling-module-(Figure-2.1D). We-summarise-the-nodepooling-modules-utilised-in-the-surveyed-papers-in-Table-2.6.

There-are-both-learnable-and-non-learnable-node-pooling-modules-in-the-literature.-Please-see-the-corresponding-papers-for-a-detailed-description-of-these-methods-(Table-2.6).- Node-pooling-modules-remain-a-relatively-unexplored-topic-in-the-EEG-GNNclassification-models.- Node-pooling-can-(1)-remove-redundant-nodes,-(2)-reduce-thesize-of-the-graph-embedding-in-a-setting-where-the-concatenation-of-node-embeddingsforms-it,-and-(3)-aid-in-the-explainability-of-the-model-by-identifying-node-importancewith-respect-to-the-classification-task.-

Method-	Learnable-	Papers-
Sum-readout-	×	[178,-311,-16]-
Average-readout-	×	[214,-166,-289,-61,-131,-54,-246]-
Maximum-readout-	×	[307,-289,-112,-54,-142]-
Concatenate-node- embeddings-	×	[177,-162,-155,-48,-161,-305,-234,-235,-138,- 168,-303,-113,-124,-174,-80,-308,-290,-300,- 130,-210,-270,-173,-313,-81,-133,-229]-
CNN-like-		
Average/Maximum ⁻	×	[171,-86]-
Pooling-		
SortPool-	1	[28]-
Attention-weighted-	1	[160, -301, -164]-
CNN-	1	[8,-242,-149]-
LSTM-	1	[291,-170]-
Capsule-Network-	1	[99]-
Transformer-	1	[244]-
Bidirectional-LSTM-	✓	[168,-86,-108]-

 Table 2.7:
 Overview of methods for the formation of graph embedding

 from a set of node embeddings

2.4.7 From Node Embeddings to Graph Embedding

The output of the graph convolutions is a set of learned node embeddings. Node embeddings in this form are suitable for tasks such as node classification and link prediction. However, for graph classification, the set of node features needs to be transformed into a unified graph representation (Figure 2.1E). We summarise the methods for this transformation in Table 2.7.

The-most-straightforward-method-to-form-a-graph-embedding-is-to-simply-concatenate-the-node-features. This-approach-poses-a-few-limitations. First, the resultinggraph-embedding-grows-with-the-number-of-nodes. Thus, the classification-layer-requires-a-large-number-of-parameters. Second, all-input-graphs-must-have-the-samenumber-of-nodes, limiting-the-model's-generalisation-to-other-datasets. Finally, suchan-approach-is-likely-to-include-redundant-or-duplicated-information-in-the-graphembedding-since-GNN-produces-node-embeddings-by-aggregating-information-fromneighbouring-nodes.-

A-readout-function-is-one-of-the-methods-to-form-a-graph-embedding-that-addressesthese-issues.- A-readout-forms-the-embedding-by-passing-the-node-features-through-apermutation-invariant-function.- A-general-definition-of-a-readout-to-obtain-graphembedding-of-a-graph- G_i from-a-set-of-V node-embeddings- $H = [h_1, ..., h_V]$ -is-given-by:-

$$G_i = \sum_{k=1}^{V} h_k, \qquad (2.13)$$

where \sum can be any permutation-invariant function. In the surveyed papers, these functions were sum, average and maximum. A few papers also experiment with attention-weighted sum to attenuate the role of unimportant nodes within the graph embedding [160]. An interesting alternative is to apply CNN-style average or maximum pooling node-wise [171].

Alternatively, researchers explored various neural network models to obtain graphembeddings, such as CNN-[8, 242, 149], (bi-)LSTM-[291, 170, 168, 86, 108], Transformer-[244] and capsule networks [99]. Additionally, graph-pooling methods, such as DiffPool-[293], SAGPool-[159], iPool-[97], TAP-[96] and HierCorrPool-[279] can be used for this purpose.

2.4.8 Discussion of EEG-GNN Approaches

Despite-most-of-the-surveyed-papers-being-relatively-recent, - a-wide-range-of-GNNbased-methods-have-already-been-proposed-to-classify-EEG-signals-in-a-diverse-set-oftasks, - such-as-emotion-recognition, - brain-computer-interfaces, - and - psychological- andneurodegenerative-disorders- and-diseases- (Fig-2.3). - This-recent-rise-in-popularity-of-GNN-models-for-EEG-might-be-attributed-to-(1)-the-development-of-new-GNN-methodsand-(2)-advances-in-network-neuroscience-inspired-an-extension-of-this-framework-todeep-learning. - GNNs-offer-unique-advantages-over-other-deep-learning-methods. - Thisis-mainly-the-possibility-of-modelling-multivariate-time-series-and-interactions-amongthem-with-a-single-GNN-model, -which-is-not-possible-with-CNN-or-recurrent-networks. Additionally, - patterns-learned-by-GNNs- can-readily-be-interpreted-in-the-context-ofnetwork-neuroscience, -thus-enabling-a-wide-range-of-avenues-for-model-explainability.

This-survey-categorises-the-proposed-GNN-models-in-terms-of-their-inputs-and-modules.-Specifically,-these-are-brain-graph-structure,-node-features-and-their-preprocessing,-GCN-layers,-node-pooling-mechanisms,-and-the-formation-of-graph-embeddings.-This-categorisation-allows-us-to-provide-a-quick-and-simple-overview-of-the-differentmethods-presented-in-the-EEG-GNN-literature,-appreciate-the-current-state-of-the-artin-this-field-and-identify-promising-future-directions.-

Limitations of Surveyed Papers

Surprisingly, we have identified the least variety and innovation in the category of GCN-layers (Table 2.5). A significant proportion of the surveyed papers utilise either ChebConv or "vanilla" spatial GCN. This might be due to the relative novelty of the EEG-GNN field, and thus, many papers explore other areas of model design, such as node features and brain graph definitions. A few papers seem to successfully experiment with more complex types of GCN-layers [177, 174, 249] and multi-branch architectures [168, 301, 290, 300, 270, 164].

A-major-limitation-of-most-surveyed-papers-is-the-lack-of-generalisability-to-externaldatasets- that-might-use-a-different-number-of-EEG-signals. This-is-caused-by-(1)the-use-of-ChebConv-and-(2)-forming-graph-embedding-by-node-feature-concatenation-[177,-162,-155,-48,-161,-305,-234,-235,-138,-168,-303,-113,-124,-174,-80,-308,-290,-300,-130,-210,-270,-173,-313,-81,-133,-229].-(1)-can-be-addressed-by-utilising-spatial-GCN-layers-assuggested-above,-and-(2)-can-be-solved-by-using-a-readout-function-or-a-suitable-nodepooling-mechanism,-which-coarsens-the-graph-to-a-fixed-number-of-nodes.- Additionally,there-is-a-general-lack-of-transfer-learning-experiments-for-EEG-GNN-models,-whichmight-be-a-promising-direction-for-future-research.-

Finally, we have identified an interesting gap in EEG-GNN research: the lack of utilising frequency band information in a more complex way. A few papers train separate models for each frequency band in isolation [178, 311, 177]. Alternatively, they propose concatenating the graph embeddings generated from the frequency band GNN branches [161, 234, 242].

Future Directions

Several-promising-directions- can- be-identified- in- the-rapidly- evolving-landscape- of-EEG-GNN-research.- First,- a- comprehensive- comparison- of- the-various- GCN-layers-(e.g.- spatial-GNN,- ChebConv,- GAT- and- graph- transformer)- with- respect- to- theirinfluence- on-classification- performance- should- be- carried- out- to- address- this- crucialdesign-question-systematically.-

Second, enhancing-the-generalisability-of-models-by-addressing-issues-related-to-thevarying-number-of-EEG-signals/electrodes-and-exploring-transfer-learning-approachescan-open-new-avenues-for-research.- For-instance, pre-trained-GNN-models-on-cheap-toobtain-large-datasets, such-as-open-databases-for-emotion-recognition-or-brain-computerinterface-(BCI)-applications, would-allow-the-application-of-complex-GNN-architecturesto-problems-with-limited-data-availability-due-to-the-high-costs-or-small-populations-(e.g.-clinical-data,-rare-diseases-and-disorders).-Focusing-on-these-issues-would-likelyimprove-the-generalisability-of-the-models-when-evaluated-on-a-diverse-set-of-EEGdatasets-and-different-classification-tasks.-

Lastly, the rich-frequency-information of EEG signals should be explored more. For instance, we suggest a plausible utility of integrating CFC approaches into EEG-GNN models. There is growing evidence in the literature concerning the advanced brain functions (e.g. learning, memory) enabled by CFC [135]. Thus, integrating findings from neuroscience research into the EEG-GNN design promises both performance and explainability gains.

2.5 Chapter Summary

This- chapter- reviews- disruptions- of- brain- activity- in- AD- cases- and- discusses- themethodology-for-graph-based-analysis-of-EEG.- These-reviews-highlight-the-need-forgraph-based-approaches-to-characterise-and-accurately-distinguish-AD-using-EEG-multivariate-signals.- Furthermore,-this-thesis-examines-findings-on-AD-from-oscillatory-andgraph-perspectives-to-relate-to-the-explainability-capabilities-of-the-research-presentedin-this-thesis.-

Graph-based-methods-for-EEG-analysis-are-reviewed. First, we focus on brain-graphinference, graph-preprocessing, and standard-graph-theoretical-measures-to-characterisevarious-properties-of-the-brain, such-as-region-importance, information-integration, and segregation. Then, the AD-disruptions-related-to-FC- and graph-approach-aresummarised. The main-research gap-identified-is-the-need-for-closer-examination-of-CFC-from-a-graph-perspective.

Finally, GNN-architectures for EEG classification are reviewed. The surveyed papers were categorised based on model inputs and modules, including brain-graph structure inference, definitions of node features, types of GCN-layers, node pooling mechanisms, and generation of graph embeddings. Several limitations and areas for improvement were identified. There is a lack of variety and innovation in GCN-layers, with many-papers utilising ChebConv or "simple" spatial GCN without clear justification. Integration of CFC information and evaluation of methods for brain graph inference are identified as gaps in the literature to enhance the performance and explainability of GNNs.

Chapter 3

Data

This-chapter-introduces-the-EEG-dataset-used-in-Chapters-4,-5-and-6.-

EEG-recordings-were-collected-from-20-AD-patients-and-20-HC-participants-youngerthan-70-years.- A-detailed-description-of-the-experimental-design-and-confirmation-ofthe-diagnosis-is-provided-in-[29].- All-the-AD-participants-were-recruited-from-the-Sheffield-Teaching-Hospital-memory-clinic.- AD-participants-were-diagnosed-betweenone-month- and-two-years-before-data-collection.- All-of-them-were-in-the-mild-tomoderate-stage-of-the-disease-at-the-time-of-recording,-with-an-average-MMSE-score-of-20.1-(sd-=-4).- High-resolution-structural-MRI-scans-of-all-AD-patients-were-acquiredto-eliminate-alternative-causes-of-dementia.-

Age- and- gender-matched- HC- participants- with- normal- neuropsychological- testsand- structural- MRI- scans- were- recruited.- This- study- was- approved- by- the- Yorkshire- and- The- Humber- (Leeds- West)- Research- Ethics- Committee- (reference- number-14/YH/1070).- All-participants-gave-their-informed-written-consent.-

All- patients- underwent- examination- via- high-resolution- structural- MRI- scans- toeliminate- major- underlying- causes- that- could- explain- their-clinical- symptoms. - Noneexhibited-significant-small-vessel-ischemic-disease, -as-evidenced-by-FLAIR-MRI-scans.

Each-participant-provided-consent-for-a-3-Tesla-MRI-scanning-procedure-using-a-Philips-Ingenia-scanner, encompassing-structural-and-resting-state-functional-scans.-Additional-scans, including-diffusion, T2-weighted, and FLAIR-acquisitions, confirmed-the-absence-of-exclusion-criteria.-MRI-assessments-were-conducted-on-average-79-days-prior-to-their-inclusion-in-the-study.-The-purpose-of-the-structural-and-functional-neuroimaging-was-solely-to-characterize-brain-structure-and-function-in-these-patients, ensuring-they-were-representative-of-the-clinical-population-under-investigation.-

Anatomical-T1-weighted-images-were-acquired-with-the-following-parameters:-voxel-

size of $0.94 \times 0.94 \times 1.00$ mm, field of view of 256 mm, matrix size of $256 \times 256 \times 124$, repetition time of 8.2 s, echo delay time of 3.8 ms, and flip angle of 8° . Following a series of dummy scans to achieve electromagnetic equilibrium, a T2*-weighted scanwas conducted to assess cerebral hemodynamics at rest. This scan comprised 120-volumes, each containing 35-axial slices acquired in ascending order. Participants were

instructed to keep their eyes closed throughout the scan. The scan parameters were set as follows: repetition time of 2.6 s, total acquisition time of 4-minutes and 30 seconds, echo delay time of 35 ms, flip angle of 90°, voxel dimensions of $2.4 \times 2.4 \times 4.0$ mm, and field of view of $230 \times 230 \times 140$ mm.

The cognitive function of AD-patients and HC-was evaluated using a comprehensive battery of neuropsychological tests designed to detect cognitive impairments typically associated with AD. These tests covered areas such as short and long term memory (verbal and non-verbal), abstract reasoning, attention and executive function, language comprehension, and fluency in naming, category, and letter retrieval.

EEG-data-were-acquired-using-an-XLTEK-128-channel-headbox,-Ag/AgCL-electrodes-with-a-sampling-frequency-of-2-kHz-using-a-modified-10-10-overlapping-a-10-20international-electrode-placement-system-with-a-referential-montage-with-a-linked-earlobe-reference.- The-recordings-lasted-30-minutes,-during-which-the-participants-wereinstructed-to-rest-and-not-think-about-anything-specific.- In-case-the-participants-showedsigns-of-drowsiness,-they-were-prompted.- Within-each-recording-were-five-minute-longepochs-during-which-the-participants-had-their-eyes-closed,-alternating-with-an-equalduration-of-eyes-open-epochs.-

All-the-recordings-were-reviewed-by-an-experienced-neurophysiologist-on-the-XL-TEK-review-station-with-time-locked-video-recordings-(Optima-Medical-LTD).-Foreach-participant,-three-12-second-long-artefact-free-epochs-were-isolated.- Finally,-thefollowing-23-bipolar-channels-were-created:- F8–F4,-F7–F3,-F4–C4,-F3–C3,-F4–FZ,-FZ–CZ,-F3–FZ,-T4–C4,-T3–C3,-C4–CZ,-C3–CZ,-CZ–PZ,-C4–P4,-C3–P3,-T4–T6,-T3–T5,-P4–PZ,-P3–PZ,-T6–O2,-T5–O1,-P4–O2,-P3–O1- and-O1–O2-[29].- Bipolarmontage-was-selected-to-limit-the-volume-conduction-effects-to-a-certain-extent.-

As-a-neurophysiologist-confirmed-the-EEG-signal-to-be-artefact-free,-we-did-not-further-clean-the-signals.-The-signals-are-filtered-using-a-band-pass-Butterworth-filter-to-a-range-of-0.5-Hz-and-45-Hz.-

The utilisation of a relatively small EEG dataset in the experiments described in this thesis was driven by the absence of larger, open access data of EEG for AD at the time of performing the experiments. While this dataset undoubtedly posed limitations

 $in \ terms \ of \ its \ scope \ and \ general is ability, \ it \ none the less \ provided \ a \ valuable \ foundation \ for \ initial \ exploration \ analysis.$

However, since then, an open-access dataset for EEG in AD has been released [191]. This presents an exciting opportunity to enhance the robustness of future research by incorporating such a dataset for external independent validation. By leveraging a more extensive and diverse dataset, researchers can strengthen the reliability and generalisability of their findings.

Chapter 4

Cross-Frequency Multilayer Graph Analysis with Bispectrum-based Functional Connectivity

4.1 Introduction

¹The main EEG characteristics associated with AD are the slowing of signals, and altered synchronisation [128, 98, 150, 68, 267, 13]. However, these characteristics are typically measured at a single channel or between channel pairs. In contrast, the graph based analysis considers all EEG channels and reveals AD characteristics such as reduced integration of information [136, 63], and loss of small worldness [247]. However, these characteristics are often analysed only within specific frequency bands.

This-chapter-aims-to-extend-the-FC-beyond-WFC, taking-the-CFC-[135]-into-account.- WFC-graphs-of-AD-were-analysed-previously-by-using-coherence-(linear)-[4]and-wavelet-coherence-(nonlinear)-[127].- Only-one-CFC-measure, i.e.- phase-synchronisation-index-(PSI), had-been-used-for-the-graph-analysis-of-CFC-graphs-in-AD-[42].-This-work-extended-the-findings-of-reduced-integration-and-loss-of-small-worldness-to-CFC-multilayer-graphs.- However, it-does-not-consider-the-roles-of-different-frequencycomponents-in-the-graphs.- The-multilayer-graph-framework-had-been-used-previouslyfor-brain-graph-analysis.- Loss-of-inter-frequency-hubs-in-AD-was-reported-using-MEG-

¹The content presented in this chapter has been published in Dominik Klepl, Fei He, Min Wu, Daniel J. Blackburn, and Ptolemaios G. Sarrigiannis. Cross-Frequency Multilayer Network Analysis with Bispectrum-based Functional Connectivity: A Study of Alzheimer's Disease. Neuroscience, 521: 77–88, June 2023. ISSN 0306-4522. doi: 10.1016/j.neuroscience.2023.04.008

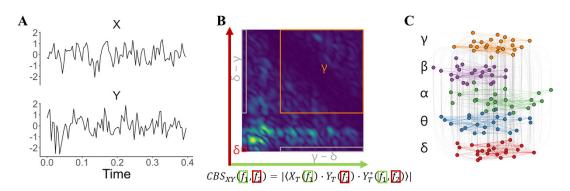


Figure 4.1: A conceptual schematic of implementing the proposed CBS multilayer graph analysis. (A) Each EEG signal is cleaned and scaled. (B) For each pair of EEG electrodes, a cross-bispectrum is estimated. The frequency bands coupling edge weights are given by the average value within the respective CBS window, e.g. δ - δ (red). Note that CBS estimates are directed, e.g. δ - $\gamma \neq \gamma$ - δ (both in grey). Thus, from each CBS, 25 edges are inferred. (C) Using the edge weights inferred from CBS, a multilayer graph is constructed with layers representing the frequency bands of EEG. Such a graph has both intra-layer and inter-layer edges, representing within-frequency and cross-frequency coupling, respectively.

multiplex-graphs[103,-298], where the inter-layer edges are inserted with fixed weight only between the same nodes across layers. Alterations in multilayer graph hubs have been reported in multimodal graphs in AD-[104], and fMRI frequency band graphs in schizophrenia [70]. Multilayer graphs integrating WFC and CFC have been used to analyse MEG data from healthy [254], and schizophrenic subjects [38]. Tewarie et al. [254] show that frequency band graph layers interact via CFC, share a certain amount of structure and operate at the edge of independence and interdependence. However, these studies analyse the layer relationships mainly as the correlation of their adjacency matrices or as differences in global average coupling strength.

Bispectrum- is- a- higher-order- spectral- analysis- and- quantifies- quadratic- couplingbetween-two-frequency-components- and-their-algebraic-sum- [107].- It-has-been-shownto- detect- amplitude- amplitude- and- phase-amplitude- CFC- in- addition- to- the- phasephase-coupling- [135,-151].- The- bispectral-coupling- also-indicates- an-increase-in- non-Gaussianity- [278].- Features- derived- from- bispectrum- were- proposed- as- biomarkersof-epilepsy- [183,-32],- Parkinson's- disease- [299],- autism- [206]- and- AD- [278,-275,-187].-Most- of- these- studies- compute- (cross-)- bispectra- of- only- a- few- channels- or- pairs- ofchannels.- Although- a- few- studies- used- bispectrum- to- compute- global- graphs- frommultiple- channels- [51],- these- analyses- do- not- use- graph- theory.- Instead,- each- nodeis-analysed-in-isolation-[275]-or-single-channel-bispectra-are-averaged-across-nodes-toderive-certain-global-properties-[187].-In-contrast,-this-study-computes-cross-bispectrabetween-all-pairs-of-EEG-channels-to-estimate-the-widely-distributed-FC-brain-graphsand-perform-graph-theoretical-analysis.-

In this chapter, the cross-bispectrum estimates of FC are computed. We aim to investigate the contribution of nonlinear WFC and CFC in differentiating between (AD) and HC in comparison to the equivalent linear WFC measured with cross-spectrum (CS) (Figure 4.1). We report a multilayer graph based analysis to elucidate the roles of the traditional EEG frequency bands and their CFC in the sensor-level EEG graphs of HC and AD. Moreover, we use the reconstructed brain graphs to classify AD using an SVM classifier.

4.2 Methods

4.2.1 EEG pre-processing

EEG-signals-were-confirmed-to-be-artifact-free. Thus, -no-additional-artefact-removalwas-undertaken. The signals-were-band-pass-filtered-to-be-between-0.1-and-100-Hzusing-a-zero-phase-5th order-Butterworth-filter; -50-Hz-relating-to-the-power-line-noisewas-removed-using-a-zero-phase-4th order-Butterworth-stop-band-filter, - and-the-datawere-down-sampled-to-250-Hz-using-an-order-8-Chebyshev-type-I-filter. Finally, - thesignals-were-normalised-(to-zero-mean-and-unit-standard-deviation).

4.2.2 Cross-spectrum and Cross-bispectrum

The spectrum S_X of a signal X is calculated via a smoothed periodogram. Fast-Fouriertransform (FFT)-is used to estimate the periodogram with Daniell smoothers. The periodogram is computed over 256-frequency bins (0.98-Hz-bandwidth). CS-at-frequencyf is then computed as: $CS_{XY}(f) = S_X(f) \cdot S_Y(f)$. An absolute value of CS-is calculated. A direct FFT-based method is used to estimate the absolute value of CBS:

$$CBS_{XY}(f_1, f_2) = |\langle X_T(f_1) \cdot Y_T(f_2) \cdot Y_T^*(f_1, f_2) \rangle|, \qquad (4.1)$$

where $\langle \cdot \rangle$ denotes averaging, $X_T(f)$ is an FFT of signal X over an interval T and Y_T^* is the complex conjugate. 256-point FFT is used. CBS is computed over 1-second-long windows with 50% overlap over the whole frequency range (0.5 - 100 Hz). The

window-size-and-overlap-were-chosen-empirically-to-balance-the-spectral-and-temporalresolutions.- The-estimated-CBS-is-then-smoothed-in-the-frequency-domain-using-the-Rao-Gabr-window-(size-5).-

CS-and-CBS-were-computed-for-all-pairs-of-EEG-channels. Five-frequency-bandsb are-considered: δ (0.5- 5Hz), θ (5- 8Hz), α (8- 16Hz), β (16- 32Hz) and γ (32- 100Hz).

The connectivity between channels X and Y and frequency bands b_X and b_Y is computed as:

$$FC_{XY}^{CS}(b) = \langle CS_{XY}(f \in b) \rangle, \tag{4.2}$$

$$FC_{XY}^{CBS}(b_X, b_Y) = \langle CBS_{XY}(f_1 \in b_X, f_2 \in b_Y) \rangle, \tag{4.3}$$

for CS-and-CBS, respectively, where $\langle . \rangle$ denotes averaging. This resulted in five WFC-(CS-and-CBS) and 20-CFC-(CBS-only) measures per-channel-pair. It is of note that the CBS-is directed.

In-order-to-ensure-the-reliability-of-the-estimated-connectivity,-surrogate-thresholding-was-used-[255].-For-each-pair-of-channels,-200-surrogate-signals-were-generatedusing-the-FFT-surrogate,-which-scrambles-the-phase-of-the-signal,-and-their-CS-and-CBS-are-computed.-The-95%-confidence-interval-of-surrogate-values-is-computed-andused-as-a-threshold.-Coupling-values-below-the-threshold-are-set-to-zero.-We-chosethis-approach-to-ensure-the-reliability-of-estimated-brain-graphs.-In-contrast,-Wang-etal.-[275]-used-no-such-thresholding-when-analysing-bicoherence-coupling.-Alternativeapproaches-exist-in-the-literature.-Chella-et-al.-[51]-take-advantage-of-the-asymmetricproperty-of-CBS-to-ensure-robustness-against-mixing-artefacts.-

We obtain a set of connectivity matrices for each EEG recording, i.e. $N \times N$ matrices (N = 23). For CS and CBS, there are five and 25 connectivity matrices, respectively. A-global (averaged per-subject) connectivity is computed for each 23 \times 23 matrix and compared between groups using a two-sample t-test if normally distributed and a Mann-Whitney test otherwise.

4.2.3 Graph Measures

To identify the important channels in the graph, we compute a coupling-specific NS-[17]-for each channel i and different types of frequency couplings c,

$$NS(i,c) = \sum_{j \in \Pi(i,c)} w_{ij}, \tag{4.4}$$

where $\Pi(i, c)$ -are-the-nodes-connected-to-channel-*i* via-edge-type-*c* and w_{ij} is-the-edgeweight, i.e. CS-or-CBS-connectivity-given-by-*ij*th-entry-of-the- $N \times N$ connectivitymatrix. This-measure-is-computed-for-both-CS-and-CBS, resulting-in-5-(5-frequencybands)-and-25-(5-× 5-frequency-bands)-values-per-channel, respectively.

In order to analyse the importance of the different frequency couplings within the global brain graph, we represent them as a multilayer graph. In this graph, nodes are located within layers representing the different frequency bands. WFC represents the edges between nodes within a single layer, i.e. intra-layer, and CFC represents the edges between nodes located in different layers, i.e. inter-layer. In this work, the CS graphs are not analysed as multilayer graphs since such graphs would have no inter-layer edges and thus would not be comparable directly with the CBS graphs. The following measures are computed only for CBS graphs. We obtain graphs with 23 nodes that are replicated over 5 layers ($L \in [\delta, \theta, \alpha, \beta, \gamma]$), resulting effectively in 115 nodes. There are 5 types of intra-layer edges, such as δ - δ , and 20 types of inter-layer edges, such as δ - θ or θ - δ .

We measure the importance of each type of frequency coupling within the multilayer graph by measuring the contribution of each edge to enable the efficient passing of information through the graph. For this purpose, we define coupling betweenness centrality (CBW) centrality based on an adjusted version of edge betweenness [100]:-

$$CBW(c) = \frac{1}{E} \sum_{i=1}^{E} BW(e), \qquad (4.5)$$

where E is the total number of edges of coupling type c and BW(e) is edge betweenness centrality given by:

$$BW(e) = \sum_{i \neq j} \frac{g_{ij}(e)}{g_{ij}}, \qquad (4.6)$$

where g_{ij} is the number of shortest paths between nodes i and j, and $g_{ij}(e)$ is the number of those paths that go through edge e. The shortest path is defined as a path with the least sum of w_{ij} . CBW quantifies the contribution of each coupling type to the information integration [245], i.e. the amount of information flow through edges. Note that the CBW of a weighted and unweighted version of the same graph results in different value of CBW. Therefore, we analyse both weighted and unweighted CBW.

CBW-assumes-that-the-essential-processes-within-the-graph-occur-along-the-shortestpaths.- However, there might be alternative paths with only minor-length differences, which-CBW-ignores. In-case-of-a-disruption-of-the-graph-structure, these-alternativepaths-might-enable-the-recovery-of-function-with-negligible-differences. We-quantifythis-as-the-vulnerability-of-the-graph-to-the-removal-of-one-type-of-frequency-coupling. The-vulnerability-is-measured-in-two-ways: the-loss-of-ability-to-integrate-information-[158]-and-the-loss-of-segregation.

The integration property of graph G, i.e. the ability of a graph to communicate information globally, is approximated with global efficiency (E_G) -given by:

$$E_G(G) = \frac{1}{N(N-1)} \sum_{i \neq j \in G} \frac{1}{d(ij)},$$
(4.7)

where N is the number of nodes in graph G and d(ij) is the shortest path length between nodes i and j. E_G is related to CBW. CBW measures the information flow on the more detailed edge level while E_G takes the node-level perspective.

$$E_L(G) = \frac{1}{N} \sum_{i \in G} E_G(G_i), \qquad (4.8)$$

where G_i is the neighbourhood of node i, i.e. subgraph of nodes directly connected to i, without node i itself.

In-order-to-measure-the-vulnerability-of-the-graph-and-its-dependence-on-differenttypes-of-frequency-coupling, E_G and E_L are-computed-for-the-full-graph. The-two-measures-are-then-re-computed-for-a-perturbed-graph-where-one-type-of-frequency-coupling-(i.e.- a-set-of-edges)-is-removed. The-change-in- E_G and E_L give-the-global-and-localvulnerability-measures- $V_G(G_c) = 1 - (E_G(G_c)/E_G(G))$ -and $V_L = 1 - (E_L(G_c)/E_L(G))$, where-G is-the-full-graph-and- G_c is-the-perturbed-graph-with-the-edges-of-couplingtype-c removed.

4.2.4 Graph Thresholding and Statistical Analysis

In order to filter out the unimportant edges that might result from a spurious coupling, the weighted multilayer graphs are thresholded through relative quantile based thresholding. Given a quantile Q, all edges with a weight lower than Q are removed from the graph. There are considerable differences between the weights of each frequency coupling type (e.g. mean of γ - β = 1.627 compared to the mean of α = 8.975); thus,

a separate threshold Q is used. As a result, the graphs retain Q% of the strongest edges. To ensure that the observed differences between the graphs are not due to the choice of threshold Q, all of the graph measures are computed over 20 threshold values $(Q \in [0, 0.95]$ in increments of 0.05), and only significant differences observed over at least ten thresholds are declared significant. The reported plots and numerical results are generated from such threshold levels of Q that the between group difference is maximised (i.e. largest effect size). However, the effect of choice of this thresholds. All p-values are corrected using the Benjamini–Hochberg false discovery rate method [25].

Additionally, to improve the reliability, we perform epoch-wise test-retest experiments. For each participant included in this study, there are three epochs. Thus, we repeat the full analysis reported in this chapter for each epoch separately. Consequently, only significant differences observed consistently across all three epochs are denoted as significant. An analysis of statistical power given our sample size was performed to identify the threshold effect size where 80% is reached (A.1).

Furthermore, we convert the CBS graph from directed to undirected by taking the mean weight for each pair of directed edges, thus collapsing them into a single edge. Such an approach is the most conservative since the potential effect of outliers is minimised compared to the alternative of taking the maximum weight.

NS-is-log-transformed-to-reduce-skewness.- We-do-not-threshold-the-graphs-for-NScomputation,- as-this-might-lead-to-isolated-nodes-with-no-edges.- We-test-whethernode-strengths-are-normally-distributed-separately-for-each-coupling-and-channel-witha-Shapiro-test.- Node-strengths-that-pass-the-test-are-then-compared-with-a-two-samplet-test,-and-those-that-do-not-pass-the-test-are-compared-with-a-Mann-Whitney-U-test.-

The multilayer graph measures such as CBW, global vulnerability (v_G) and local vulnerability (v_L) -aim to analyse the roles of frequency coupling types in terms of the graph's properties. However, whether such multilayer graphs should be weighted or unweighted is unclear. Thus, we examine the patterns in both weighted and unweighted multilayer graphs. The weighted graphs can be converted into unweighted graphs by setting the weights of all edges to 1. Additionally, the selected graph metrics, except for NS, assume edge weights represent the distance between weights. Since functional connectivity is a measure of similarity, we convert the edge weights to distance as follows,

$$\tilde{w_{ij}} = max(W) + min(W) - w_{ij} \tag{4.9}$$

, where \tilde{w}_{ij} is the transformed edge weight connecting nodes i and j, W is the edge

weight-distribution-of-the-graph-and- $max(\cdot)$ -and- $min(\cdot)$.

We test whether CBW, v_G and v_L of both weighted and unweighted graphs are normally distributed using the Shapiro-Wilk test for each coupling type separately. A two-sample t-test is used for normally distributed variables and Mann-Whitney U-for non-normally distributed variables to compare between groups. Furthermore, both weighted and unweighted CBW and v_G are log-transformed to reduce skewness.

4.2.5 Graph Classification

Finally, we train classifiers using the graph metrics to evaluate the predictive power of these biomarkers of AD. Three classifiers are trained using the CS, CBS, and combined features, respectively. In other words, the CS classifier is trained using NS, the CBS classifier uses the NS and multilayer graph metrics, and the combined classifier uses all of the previous. Additionally, these features are collected across all filtered graphs.

As this leads to a large feature space, we introduce an effect-size-based forward feature selection. The features are ordered by the absolute value of effect-size (Cohen's d [57]) and sequentially added to the feature vector, which is then used to train the classifier. The first 100 features are evaluated in this manner. Note that comparing the CS and CBS classifiers is likely unfair as the CS utilises considerably smaller and less complex features, as the NS is a relatively simple graph measure. Instead, the CS classifier should be viewed as a naive baseline.

SVM-classifier-with-radial-basis-kernel-is-used-as-the-classifier.- Moreover,-featuresare-scaled-to-zero-mean-and-unit-standard-deviation.- 10-fold-cross-validation-repeated-100-times-is-used-to-train-and-evaluate-the-classifier.-

Finally, we use the feature sets of CS and CBS classifiers that achieved the bestperformance and train a combined classifier. We hypothesise that the information captured by CS and CBS graphs is at least partially unique. Thus a classifier trained on the combined feature sets should outperform the classifiers trained on individual graphs, as it can leverage the information from both functional connectivity measures.

4.3 **Results and Discussion**

We denote a statistical test as significant only if it is consistently detected across at least ten-graph thresholds and in-all three epochs. Therefore, for simplicity, only results from epoch two are reported in the following sections, except for the classification results,

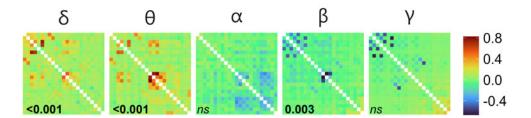


Figure 4.2: The difference between average connectivity matrices (AD – HC) measured with cross-spectrum in epoch 2. For visualisation purposes, the values were min-max normalised. Digits in black denote a *p*-value (FDR corrected) testing for the difference in global coupling (p < 0.05 in bold, in italics otherwise).

where-data-from-all-epochs-are-utilised.- Epoch-two-was-selected-randomly, which-doesnot-affect-the-reported-results-as-all-results-were-required-to-be-observed-across-all-threeepochs.- Moreover, -for-visualisation-purposes, -we-select-the-graph-threshold, -where-thestrongest-difference-is-observed-for-each-comparison-separately.-

The results and visualisations from epochs 1 and 3 are included in A.2 and A.4, respectively. The numerical results from epoch 2 are included in A.3.

4.3.1 Connectivity Matrices and Average Connectivity

Differences-in-averaged-connectivity-matrices-(Figure-4.2-and-4.3)-indicate-that-bothmethods-seem-to-detect-variations-in-the-topology-of-FC-graphs. The-results-of-statistical-tests-are-reported-in-A.3-(Tables-A.11-and-A.12). By-using-CS,-significantdifferences-in-the-average-connectivity-are-found-in- δ and- θ bands,-where-AD-caseshave-increased-connectivity. Additionally,-CS-reveals-a-decrease-in- β connectivity-of-AD-cases.

Using-CBS,-differences-can-be-observed-in-multiple-frequency-bands-and-their-couplings.-Increased-global-connectivity-is-observed-in-AD-cases-in- θ WFC-and- θ - δ ,- δ - θ and- δ - α CFC.- In-contrast,-decreased-global-connectivity-in-AD-cases-is-found-in- β WFC-and-alpha-beta,- α - γ ,- β - α ,- β - γ ,- γ - α and- γ - β CFC.- Overall,-AD-cases-show-increased-connectivity-in-low-frequency-components-and-their-CFC-interactions-and-decreased-connectivity-in-high-frequency-components.-

These findings are consistent with the literature reporting increased activity in δ and θ in AD [128, 150]. An increase in δ WFC and low-frequency CFC in AD was also reported using bicoherence [275]. Similarly, Maturana et al. [187] report increased bispectral power in AD in δ and θ and a decrease in α , β_1 and β_2 . They also report

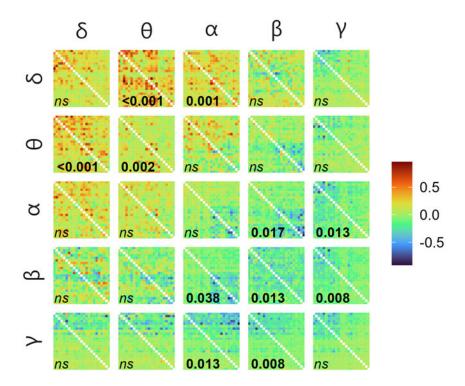


Figure 4.3: The difference between average connectivity matrices (AD – HC) measured with cross-bispectrum in epoch 2 with input frequency on the vertical facets and output frequency on the horizontal. For visualisation purposes, the values were min-max normalised. Digits in black denote a *p*-value (FDR corrected) testing for the difference in global coupling (p < 0.05 in bold, in italics otherwise).

lower-bispectral-entropy-in- δ and- θ suggesting-fewer-frequency-components-interactwith-these-frequency-bands.-In-contrast,-Cai-et-al.-[42]-report-the-opposite-differencesin-the-same-WFC-and-CFC-using-PSI,-i.e.-decrease-in- δ and- θ .-

Moreover, `the `visible `structure `distortion `within `multiple `frequency `bands `detected `by `both `CS `and `CBS `suggests `connections `to `the `disconnection `syndrome `and `disturbed `information `processing `in `AD.'

4.3.2 Coupling-wise Node Strength

In-order-to-statistically-test-the-differences-in-connectivity-measured-by-both-CS-and-CBS- and- to-localise- the- brain-regions- which- show- the- most- pronounced- differencesbetween-AD- and-HC,-NS-is-measured-for- each-channel- and-coupling-type-separately.-We-show-the-results-in-Figs.- 4.2- and -4.3-for-CS- and-CBS,-respectively.- The-details-ofthese-statistical-tests-are-reported-in-A.3-(Tables-A.13- and -A.14).-

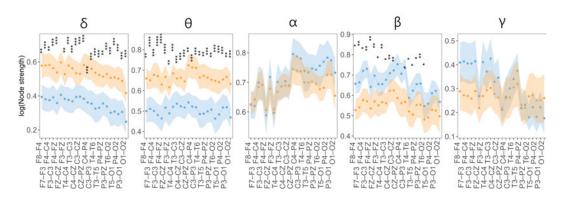


Figure 4.4: NS (min-max normalised) measured with CS of HC (blue) and AD (orange): mean with 95% confidence intervals. Significant differences observed across all epochs are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

The differences in WFC detected by CS and CBS (Figure 4.4 and diagonal elements in Figure 4.5) are generally similar. Both methods show increased θ NS in AD cases across most channels. Both CS and CBS show decreased β coupling. However, each detects these changes in different regions, i.e. CS across all channels except for occipital, while CBS only in central channels. Interestingly, CBS fails to capture the increased NS in AD cases that can be seen in CS. These differences show case the importance of assessing both-linear and nonlinear coupling in understanding the variations in AD brain graphs.

Multiple-differences-in-the-CFC- (off-diagonal-elements-in-Figure-4.5)-are-detected,highlighting- the- need- to- analyse- the- interactions- of- frequency- components- in- bothhealthy-and-AD-brain-graphs.- AD-cases-show-a-global-increase-in- δ - θ and- θ - δ ,-and-infrontal- and-temporal-areas-in- δ - α .- This-is-in-contrast-to-the-findings-in-Wang-et-al.-[275],-where-an-increase-of- δ - θ only-in-frontal-channels-is-reported.- They-also-reportan-increase-in-midline-parietal-occipital- θ - γ that-we-do-not-detect.- Furthermore,-weobserve-a-frontal,-occipital-and-temporal-decrease-in- α - β and- β - α ,-frontocentral-andfrontotemporal-decrease-in- α - γ and- β - γ ,- and-in-frontal,- frontocentral-and-occipitalchannels-in- γ - α in-AD-cases.-

Cai- et- al. [42] - report- comparable- differences- using- PSI,- but- in- contrast- to- ourresults,- they-show-mainly-decreased-NS-in-AD-cases. This-might-be-because-CBS-isinfluenced- by- the- amplitude,- while- PSI- is- a- pure- phase- coupling- measure. Fraga- etal. [92] - report- an-increase-of- the- δ - θ and - δ - β amplitude-amplitude-CFC- in-AD-caseswhich-is-similar-to-our-results. This-suggests-that-CBS-indeed-measures-some-mixture-

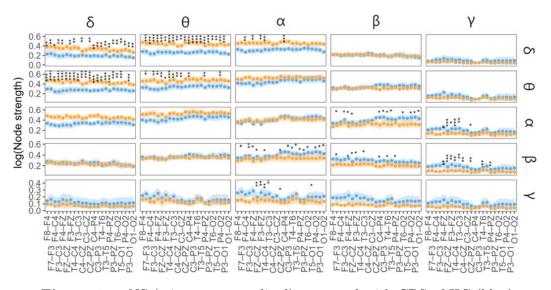


Figure 4.5: NS (min-max normalised) measured with CBS of HC (blue) and AD (orange): mean with 95% confidence intervals. The input frequency is on the vertical facets, and the output frequency is on the horizontal. Significant differences observed across all epochs are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "***", $p \leq 0.01$ "**", and $p \leq 0.05$ "*".

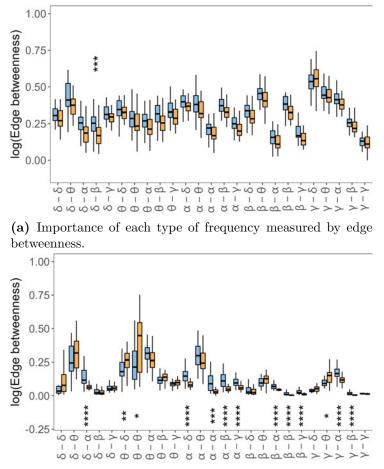
of-CFC-types-[135]-since-our-results-are-partially-in-line-both-with-phase-phase-and-amplitude-amplitude-CFC-studies.-

4.3.3 Multilayer Graph Analysis

In-order-to-elucidate-the-roles-of-the-frequency-bands-and-their-coupling, both-WFCand-CFC, we analyse the CBS-graphs-as-multilayer-graphs-with-five-layers-representingthe-traditional-frequency-bands-of-EEG. Moreover, both-the-weighted-and-unweightedversions-of-these-graphs-are-analysed.

First, weighted and unweighted CBW are used to assess the importance of each type of coupling for both local and global communications in the graph. Results of statistical tests comparing the unweighted CBW are reported in the appendix (Table A.15) and visualised in Figure 4.6a. Results of statistical tests comparing the weighted CBW are reported in the second tests comparing the communication of the second tests comparing the second tests comparing tests comparing the second tests comparing tests comparing the second tests comparing tests comparing tests comparing tests comparing the second tests comparing the second tests comparing tests comp

The unweighted CBW shows only a decrease in AD cases in the δ - β CFC (Fig 4.6a. In contrast, the weighted CBW shows multiple decreases in AD cases, specifically in α - α and β - β WFC and δ - α , α - δ , α - β , α - γ , β - α and β - γ CFC. As these decreases involve high-frequency components, we speculate that this finding is likely linked to



(b) Importance of each type of frequency coupling measured by weighted edge betweenness.

Figure 4.6: Significant differences observed between HC (blue) and AD (orange) in at least ten thresholded graphs and across all epochs are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "**", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

the characteristic slowing down of signals in AD, i.e. a decrease of high-frequency power [128, 98]. On the other hand, we observe an increase of weighted CBW of θ - θ WFC and θ - δ and γ - θ CFC in AD cases. Interestingly, previously, a decrease in γ - θ phase-amplitude coupling was reported to signify progression from mild cognitive impairment to AD [198]. However, our results indicate an opposite pattern.

Then, weighted and unweighted v_G are used to assess the vulnerability of information integration of the graph to the removal of a specific coupling type. Numerical results of comparing unweighted v_G are reported in the Appendix (Table A.16) and visualised in Figure 4.7a. Numerical results of comparing weighted v_G are reported.

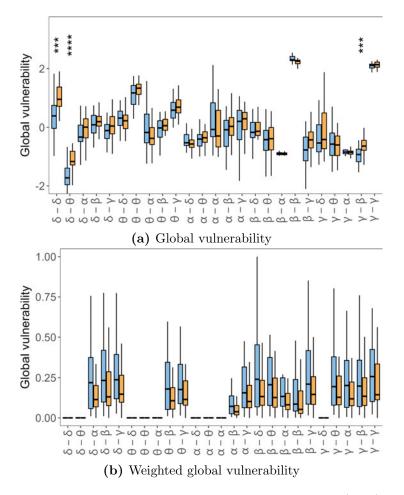


Figure 4.7: Significant differences observed between HC (blue) and AD (orange) in at least ten thresholded graphs and across all epochs are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "***", $p \leq 0.001$ "***", and $p \leq 0.05$ "*".

and-visualised-in-Appendix-(Table-A.19)-and-visualised-in-Figure-4.7b.-

The AD-brain-graphs-seem-more-vulnerable-to-removing-multiple-types-of-couplings.-Weighted- v_G fails-to-detect-any-reliable-differences.- We-speculate-this-might-be-causedby-edge-weight-differences-across-different-coupling-types,-thus-biasing-the-results.- v_G is-likely-more-sensitive-towards-such-an-issue,-as-it-is-a-global-measure-in-contrast-tothe-other-measures,-which-consider-predominantly-local-relationships.- A-significantincrease-in-unweighted- v_G in-AD-cases-is-observed-in- δ - δ WFC-and- δ - θ and- γ - β CFC.-Interestingly,-the-removal-of-WFC-generally-causes-a-larger-increase-in-vulnerabilitycompared-to-CFC-(except-for- α - α ,-suggesting-that-while-CFC-plays-a-crucial-role-inthe-brain-graphs,-WFC-seems-dominant-in-the-brain-graphs.-

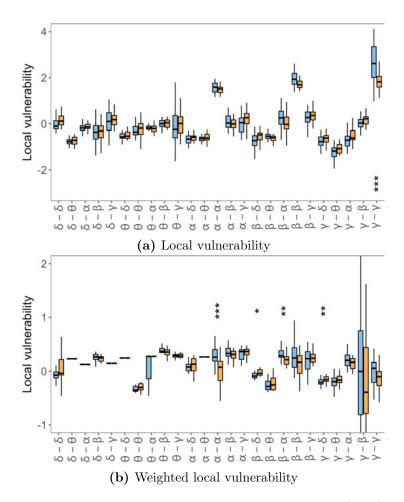


Figure 4.8: Significant differences observed between HC (blue) and AD (orange) in at least ten thresholded graphs and across all epochs are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "**", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

Finally, weighted and unweighted v_L are used to assess the vulnerability of segregation of the graph to the removal of a particular coupling type. Results of statisticaltests comparing unweighted v_L are reported in Appendix (Table A.17) and visualised in Figure 4.8a. Results of statistical tests comparing weighted v_L are reported in Appendix (Table A.20) and visualised in Figure 4.8b.

 γ - γ is-the-most-robustly-linked-to-segregation-measured-with-unweighted- v_L , whichfits-well-with-the-evidence-of-high-frequency-oscillations-being-related-to-local-processing-[41]. Moreover, this-coupling-is-significantly-more-vulnerable-in-weighted-graphs-of-HC-cases, which-is-likely-related-to-the-decreased- γ activity-in-AD-[128]. Likely-forsimilar-reasons, the removal-of- α - α WFC-and- β - α CFC-causes-a-significant-increase-of-

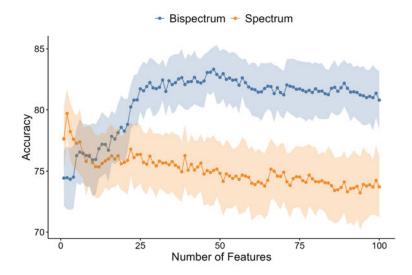


Figure 4.9: Average accuracy (points) with standard deviation (ribbons) of the classifiers trained with graph-theory features using a 10-fold stratified cross-validation repeated 100 times. Specifically, the features considered are NS for cross-spectrum (orange) and NS, CBW, v_G and v_L cross-bispectrum (blue) graphs. The features are sequentially added to the classifier based on their effect size.

weighted v_L in HC, suggesting the segregation function enabled by these high-frequency components is likely disrupted in AD. On the other hand, β - δ and γ - δ CFC removal cause a significant increase of weighted v_L in AD cases. This suggests that in AD cases, the high-frequency CFC takes over the role of enabling graph segregation as the high-frequency WFC is attenuated.

4.3.4 Classification Results

SVM-classifiers-were-trained-using-graph-features-extracted-from-CS-and-CBS-separately-to-measure-the-predictive-power-of-CS-and-CBS-based-graphs-and-evaluate-themultilayer-graph-features-(Figure-4.9).- A-detailed-performance-summary-of-the-bestmodels-is-reported-in-Table-4.1.-

All-CBS-based-models-outperform-the-CS-based-models,-suggesting-that-information-related-to-nonlinear-and-CFC-coupling-might-be-crucial-for-the-modelling-andclassification-of-AD.- However,-such-a-conclusion-might-be-biased-as-the-CS-basedmodels-are-trained-using-a-smaller-set-of-features,-i.e.- node-strengths.- Thus,-thecomparison-is-likely-unfair-and-should-be-interpreted-conservatively.-

The best-CS-based-model-reaches-its-highest-accuracy-of-79.71% (SD=1.94)-using-

Table 4.1: Performance of the best models trained using graph features identified via forward feature selection. The feature sets contain 2, 48 and 50 features for the spectrum, bispectrum and combined models, respectively.

Model-	Accuracy-	Sensitivity-	Specificity-
			74.62-%-(SD=4.48)-
Bispectrum-	83.32-%-(SD=1.83)-	86.62-%-(SD=2.95)-	80.71-%-(SD=3.9)-
Combined-	81.39-%-(SD=2.09)-	85.97-%-(SD=2.45)-	78.91-%-(SD=3.28)-

Table 4.2: Features included in the best cross-bispectrum-based classifier. For multilayer graph metrics, the graph thresholds are in parentheses. This is not necessary for the node strengths as these are obtained from the unthresholded graphs.

coupling-	Node-strength-	Multilayer-graph-metric-
α - β	C4P4,-CZPZ,-P3O1,-T5O1-	
β - α	C4P4,-P3O1-	weighted-CBW-(0.7)-
δ - α	F4C4-	weighted-CBW-(0.4,-0.45,-0.5,-0.55,-0.6)-
$\delta - \theta$	C3P3,-C4P4,-CZPZ,-FZCZ,-O1O2-	$v_G (0.55)^{-1}$
γ - α	F4FZ-	weighted-CBW-(0.4,-0.45,-0.5,-0.55,-0.6,-0.65,-0.7,-0.75,-0.8,-0.85)-
θ - δ	CZPZ, FZCZ, P4PZ	
$\theta - \theta$	F4C4-	
δ - δ		$v_G (0.65)$ -
α - δ		weighted CBW-(0,-0.05,-0.1,-0.15,-0.2,-0.25)-
α - γ		weighted-CBW-(0.5,-0.55,-0.6,-0.65,-0.7,-0.75,-0.8)-

only-two-features. These-features are the node strengths of channels-F4-C4 and C3-P3in the θ frequency-band WFC. In contrast, the CBS-based models require considerably more features to achieve the highest accuracy of 83.32% (SD=1.83) with 48 features (Table 4.2). Interestingly, the majority of these features are CFC. Furthermore, the weighted CBW-seems to provide the most information to the classifier from the multilayer graph measures introduced in this study, as it is included multiple times in the final feature set. Node strengths from all areas are utilised, but the central-parietal channels are selected repeatedly across multiple frequency couplings. It is worth noting that including the same features across different graph thresholds appears to improve the performance, despite likely strong correlations between such features. If only a single graph threshold was selected (i.e. based on the largest effect size), the accuracy drops by 2%-3%. Interestingly, both CS- and CBS-based models utilise the F4-C4 channel from the θ WFC, suggesting some shared information between these two functional connectivity methods.

Finally, we trained a combined model with the sets of best features concatenated from the CS- and CBS-based models, i.e. using 50 features. However, the accuracy of such a model is only 81.39% (SD=2.09), which is lower than the CBS-based model

suggesting-that-the-addition-of-CS-based-features-introduces-redundant-informationinto-the-model.-

4.4 Conclusions and Future Work

We-have-demonstrated-that-CBS-and-CS-detect-similar-differences-between-AD-and-HCgraphs,-but-CBS-has-an-advantage-over-CS-by-including-cross-frequency-and-nonlinearinteractions.- We-report-several-significant-differences-in-CFC-both-globally-and-ona-node-level,-suggesting-that-including-CFC-in-a-graph-theoretic-analysis-of-braingraphs-is-crucial-to-obtaining-a-more-detailed-insight-into-their-structure-and-function.-Furthermore,-we-show-that-multilayer-graph-analysis-provides-a-simple-yet-powerfulframework-for-representing-and-analysing-the-role-of-CFC-in-brain-graphs.- Using-thisframework,-we-present-a-novel-approach-to-elucidate-the-roles-of-different-frequencycomponents-of-EEG-signals.- Moreover,-we-show-that-both-CFC-and-WFC-CBS-basedgraphs-can-be-used-to-classify-AD-with-high-accuracy.-

CFC-has-been-suggested-to-be-related-to-modulatory-activity,-i.e. slow-band-modulating-the-activity-of-fast-oscillations.-However,-it-remains-unclear-why-low-frequency-CFC-would-be-increased-in-AD-and-requires-further-in-depth-study.-

Next, although (cross-) bispectrum was shown to be a powerful tool to detect various types of WFC and CFC, such as phase phase or phase amplitude, CBS seems to capture an unknown mixture of these types of couplings. Therefore, a combination of bispectrum with other types of CFC methods might be a plausible direction for future research.

Furthermore, by relying on traditional frequency bands to define the layers of the graphs, our framework might miss some CFC occurring on finer scales, e.g. interaction within one band. However, considering the CFC within only a few bands allows us to construct multilayer graphs with a relatively small number of layers. Thus, we argue that relying on the five bands is necessary to introduce the CFC into graph analysis without increasing the complexity significantly.

The presented multilayer graph analysis focused only on how dependent or vulnerable the graphs are on different types of frequency coupling to enable integration and segregation properties. Although these two properties are hypothesised to be crucial in brain graphs, their analysis is not sufficient to elucidate the functions the frequency couplings might enable across various spatio temporal scales in normal brains and how these functions disappear or change in AD. Thus, we suggest focusing on other graph theoretic-measures-beyond-integration-and-segregation-in-future-work.-

A-limitation-of-our-study-is-the-relatively-small-sample-size. This-leads-to-some-ofthe-observed-significant-differences-being-underpowered. Thus, the-small-differences-wereport-in-this-study-should-be-interpreted-more-conservatively. However, despite-thislimitation, we-identify-a-set-of-reliable-biomarkers-as-evidenced-by-the-classificationresults. In-future-research, it-might-also-be-important-and-interesting-to-explore-morecomplex-graph-based-features-that-would-capture-the-differences-between-AD-and-HCin-a-lower-dimensional-space-more-efficiently.

4.5 Chapter Summary

This-chapter-extends-the-FC-graph-analysis-beyond-WFC,-incorporating-CFC-information.- This-work-expands-on-previously-reported-graph-based-disruptions-of-braingraphs-of-AD-to-multilayer-graphs-containing-both-WFC-and-CFC-information.- Theframework-of-multilayer-graph-analysis-allows-us-to-consider-the-different-frequencycomponents'-roles-in-enabling-well-known-brain-graph-properties-such-as-informationintegration-and-information-segregation.-

Bispectrum-analysis-has-previously-been-used-to-quantify-EEG-interactions-on-a-pairwise-level.-In-contrast,-the-methodology-proposed-in-this-chapter-computes-cross-bispectra-between-all-pairs-of-EEG-channels-to-reconstruct-a-multilayer-brain-graph-with-a-layer-for-each-frequency-band.-In-such-a-graph,-intra-layer-and-inter-layer-edges-denote-WFC-and-CFC-interactions,-respectively.-

By-comparing-CBS-graphs-to-CS-graphs, the linear-counterpart of CBS, in terms of node-strength-and-classification-performance, the advantages of incorporating-nonlinear-and-CFC-information-were-demonstrated-showing-a-significantly-improved-prediction.

Statistical-analysis-of-CBS-based-graph-metrics-indicate-graph-variations-of-ADand-HC-cases.-AD-cases-show-increased-connectivity-in-low-frequency-components-andtheir-CFC-interactions-but-decreased-connectivity-in-high-frequency-components.-

We demonstrate that a graph-theoretic analysis of CFC brain graphs is crucial to obtain a more detailed insight into their structure and function. Vulnerability analysis reveals that different frequency couplings in AD graphs enable the information integration and segregation properties compared to HCs.

In-conclusion, the study-demonstrates the significance of CBS-in-capturing-nonlinear-and-CFC-interactions, providing-insights-into-AD-related-FC-alterations. Futureresearch-should-address-limitations-like-sample-size-and-explore-more-complex-graphbased-features-to-understand-AD-related-brain-graph-alterations-better.

Chapter 5

EEG-based Graph Neural Network Classification: An Empirical Evaluation of Functional Connectivity Methods

5.1 Introduction

¹In-this-chapter,-we-evaluate-a-number-of-commonly-used-methods-to-quantify-FC-from-EEG-data.-

GNN- extends- the-logic-of- convolution- operation- to- graphs- by- aggregating- information- from- connected-nodes- based- on- the- assumption- that- nodes- connected- by- anedge- are-similar.- However,- there- is- a-limited-number- of- GNN- applications- for- EEGbrain- graph- classification.- It- remains- unclear- which- method-should- be- used- to- inferthe- graph-structure-for- the- GNN- application.- A- fully-connected- graph- is- commonlyused- in- the- literature- [77].- However,- such- an- approach- does- not- leverage- any- information-encoded- by-FC- brain-graphs.- A-second-option-is-using-the-distances- betweenspatial-positions- of- EEG- electrodes- to- define- the- graph-structure- [77,-269].- Furthermore,-Demir-et-al.- [77]-utilise-distance-thresholding-and-k-nearest-neighbours-methodsto- filter-out-unimportant-edges.- Such-edge-filtering-can- be-important,- as-some-edges-

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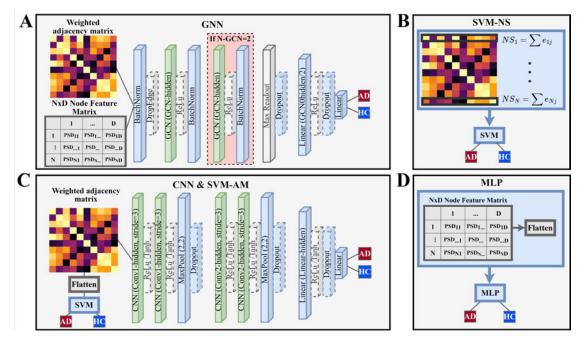


Figure 5.1: Overview of model architectures developed for classification of AD from EEG-FC-based graphs. (A) A GNN takes weighted featured brain graphs with N nodes represented by a weighted adjacency matrix and a node feature matrix ($\mathbb{R}^{N \times D}$, D = 100) where the node features consist of power spectral densities (PSD, 0 - 100Hz). The N-GCN hyper-parameter controls the number of graph convolutional layers. (B) SVM trained using the node strengths (i.e. the sum of edge weights of neighbouring nodes) as input features (SVM-NS). (C) CNN trained on the brain graphs represented by weighted adjacency matrices. Alternatively, the weighted adjacency matrix is flattened and used as input to a SVM (SVM-adjacency matrix (AM)). (D) Node feature matrix ($\mathbb{R}^{N \times D}$) with power spectral densities across all EEG channels is used to train a MLP.

might-be-redundant-or-even-introduce-additional-noise, thus-hindering-the-model-fromlearning-the-optimal-solution. Only-a-handful-of-studies-use-FC-measures, such-ascoherence-[269]-and-wPLI-[178]. Additionally, Liu-et-al. [178]-use-a-MST-algorithm-toproduce-sparse-brain-graphs. This-is-in-contrast-to-threshold-based-edge-filtering, as-MST-can-select-edges-with-various-edge-weights-and-ensure-that-the-resulting-graph-isconnected. Additionally, Zhong-et-al. [311]-utilise-a-learnable-mask-in-order-to-learnthe-optimal-graph-structure-for-a-specific-classification-task-without-relying-on-any-FCmeasure.

Other-graph-based-approaches-were-successfully-used-to-train-machine-learningclassifiers-to-diagnose-brain-disorders-using-EEG-automatically.- Manually-engineeredgraph-features,-such-as-node-strength-[202]-and-vectorised-adjacency-matrix-[197],- could-be-promising-graph-based-biomarkers-of-AD,-as-both-approaches-achieve-highclassification-accuracy.-Additionally,-there-were-some-attempts-to-utilise-deep-learning,-CNNs,-for-automatic-graph-based-feature-extraction.-Specifically,-CNN-was-trainedto-classify-AD-and-schizophrenia-using-adjacency-matrices,-which-are-image-like-representations-of-FC-graphs-[217].-However,-an-image-representation-of-a-graph-cannoteffectively-capture-all-the-properties,-as-a-graph-is-a-non-euclidean-object.-

In this chapter, we systematically evaluate the effects of using various FC methods to infer-EEG brain graphs in training GNN for the classification of AD patients. Two types of edge filtering are used to induce graph sparsity in order to improve the performance of GNN. To compare and evaluate the classification performance of various FC based GNNs, a GNN based baseline is trained using a fixed graph structure for all brain graphs, represented by the Euclidean distance between spatial positions of EEG sensors. Three additional baseline models are established: two SVM baselines trained on node strengths (SVM-NS) and vectorised adjacency matrix (SVM-vector), respectively, and a CNN trained on images of adjacency matrices. Figure 5.1 illustrates the model architectures employed for comparative study in this work.

5.2 Methods

5.2.1 EEG Pre-processing

First, a-zero-phase-5th order-Butterworth-filter-is-employed-to-remove-frequencies-below-0.1-Hz-and-above-100-Hz; a-zero-phase-4th order-Butterworth-stop-band-filter-is-used-to-remove-frequencies-between-49-and-51-Hz-related-to-power-noise. The EEG-data-were-then-down-sampled-to-250-Hz-using-an-8th order-Chebyshev-type-I-filter-and-scaled-to-zero-mean-and-unit-standard-deviation.

In order to increase the sample size and to demonstrate that the classification performance is epoch-independent, the 12-seconds-long epochs were split into 3-second-long non-overlapping segments. Thus, for each subject, there are 12-EEG segments. Finally, frequency bands are created from each EEG segment using a zero-phase 5th order Butterworth filter. Six frequency bands are considered: $\delta (0.5-4Hz)$, $\theta (4-7Hz)$, $\alpha (7-15Hz)$, $\beta (15-31Hz)$, $\gamma (31-100Hz)$ and full (0.5-100Hz).

5.2.2 Functional-Connectivity-based Brain Graph Inference

In-this-chapter,-we-selected-eight-commonly-used-methods-for-constructing-brain-graphsfrom-EEG-signals,-namely:- the-absolute-value-of-PCC,-spectral-COH,-iCOH,-PLI,wPLI,-PLV,-MI-and-AEC.-

We estimate FC brain-graphs for each EEG segment and frequency band separately. Thus, for each subject, we obtain 72 brain-graphs (12 segments × 6 frequency bands). A brain-graph G can be represented by an $N \times N$ adjacency matrix A where N = 23. As we consider only FC measures, all edges are undirected, and thus the number of inferred edges can be reduced from N^2 to $[N \times (N-1)/2]$. However, for simplicity, we keep the N^2 edges in the $N \times N$ adjacency matrix A. Thus, each entry of the adjacency matrix A_{xy}^{FC} represents the edge weight between nodes, i.e. the dependency of EEG signals $x \in \mathbb{R}^{\mathbb{T}}$ and $y \in \mathbb{R}^{\mathbb{T}}$ are measured by the connectivity measure FC where T is the signal length. All of the selected measures are normalised to [0, 1] where 0 indicates no coupling and 1 indicates a perfect coupling.

The adjacency-matrix-using-the absolute-values of Pearson's correlation coefficients between nodes x and y is given by:-

$$A_{xy}^{PCC} = \frac{\sum_{t} (x(t) - \bar{x})(y(t) - \bar{y})}{\sqrt{\sum_{t} (x(t) - \bar{x})^2} \sqrt{\sum_{t} (y(t) - \bar{y})^2}} , \qquad (5.1)$$

where x(t)-is-the-value-of-signal-x at-time-t, and \bar{x} -is-the-mean-of-x. The absolute-valueis-calculated as-we-are-only-interested in-the-coupling-magnitude. Next, the adjacencymatrix-of-COH-is-given-by:-

$$A_{xy}^{COH}(f) = \frac{|CS_{xy}(f)|^2}{CS_{xx}(f)CS_{yy}(f)},$$
(5.2)

where CS_{xy} and CS_{xx} are cross-spectral and auto-spectral densities respectively at frequency f. The coherence within a frequency band B is then calculated as the mean of $A_{xy}^{COH}(f)$ where $f \in B$.

The iCOH measures phase consistency similar to COH and accounts for volume conduction effects. The adjacency matrix using iCOH is computed as:-

$$A_{xy}^{iCOH}(f) = \frac{\Im(CS_{xy}(f))}{\sqrt{CS_{xx}(f)CS_{yy}(f)}},$$
(5.3)

where \Im denotes the imaginary component. The iCOH within a frequency band B is

then-calculated-as-the-mean-of- $A_{xy}^{iCOH}(f)$ -where- $f \in B$

The phase and amplitude of an EEG signal at time t can be calculated from the analytic representation z of signal x

$$z(t) = x(t) + \mathrm{i}\,\tilde{x}(t),\tag{5.4}$$

where is the imaginary component and $\tilde{x}(t)$ is the corresponding Hilbert transform. Then the phase and amplitude can be obtained from z(t) as

$$\phi(t) = \arctan\left(\frac{\tilde{x}(t)}{x(t)}\right), \qquad (5.5)$$

and-

$$amp(t) = \sqrt{[x(t)]^2 + [\tilde{x}(t)]^2}.$$
 (5.6)

PLI-quantifies-the-asymmetry-in-phase-distributions-of-two-signals-and-measuresonly-non-zero-phase-locking-[241].-The-adjacency-matrix-using-PLI-is-defined-as:-

$$A_{xy}^{PLI} = \frac{1}{T} \sum_{t=1}^{T} \operatorname{sign} \sin(\phi_x(t) - \phi_y(t)), \qquad (5.7)$$

where ϕ_x is obtained using Eq. 5.5. wPLI is an extension of PLI, which aims to remove the effects of amplitude and volume conduction by maximally weighting the ± 90 deg phase differences and thus omitting uniformly driven differences [265]. The adjacency matrix using wPLI is computed as

$$A_{xy}^{wPLI} = \frac{1}{T} \sum_{t=1}^{T} \frac{|\sin(\phi_x(t) - \phi_y(t))|}{\sin(\phi_x(t) - \phi_y(t))} .$$
(5.8)

PLV-is-another-approach-to-quantify-the-consistency-of-phase-differences-betweensignals,-and-its-associated-adjacency-matrix-is-computed-as-

$$A_{xy}^{PLV} = \frac{1}{T} \sum_{t=1}^{T} e^{-i(\phi_x(t) - \phi_y(t))} .$$
(5.9)

AEC-aims-to-quantify-the-coupling-based-on-the-amplitudes-of-the-signals.- The-adjacency-matrix-using-AEC-is-computed-with-Eq.- 5.1-where-x and-y are-the-amplitudesof-respective-signals-computed-using-Eq.- 5.6.-

MI-quantifies-the-amount-of-known-information-about-a-second-signal-after-observ-

ing-the-first-signal.- The-adjacency-matrix-using-MI-is-calculated-as:-

$$A_{xy}^{MI} = \sum_{x_i, y_j} P_{XY}(x_i, y_j) \log \left(\frac{P_{XY}(x_i, y_j)}{P_X(x_i) P_Y(y_j)} \right),$$
(5.10)

where P_{XY} and P_X are the joint and marginal probability distributions, respectively.

Edge Filtering Methods

It-is-worth-noting-that-we-did-not-use-any-corrections-for-false-positives. Thus, the truebrain-graph-structure-might-be-masked-by-noise-due-to-spurious-coupling. Traditionally,a-surrogate-threshold-might-be-used-to-control-such-spurious-edges. However, such-aprocedure-is-computationally-expensive, as-it-requires-re-computing-the-connectivitymeasure-on-multiple-random-surrogate-versions-of-the-original-signals, to-estimate-anull-surrogate-distribution. Instead, we-implement-two-edge-filtering-methods-to-selectonly-important-edges- and-thus-produce-sparse-graphs. Compared-to-the-surrogatethreshold-method, edge-filtering-is-a-fast- and-efficient, albeit-naive-method-to-dealwith-potentially-noisy-brain-graphs. We-also-utilise-the-fully-connected-graphs, i.e.without-any-edge-selection, in-the-classification-models-in-order-to-test-the-effect-ofedge-filtering.

The first edge-filtering method is an FC-strength-based top-k% filter ($k \in \{10, 20, 30\}$), which selects only the top-k% strongest edges of the given graph and removes the rest. This approach assumes that edge weight, i.e. the connectivity strength, is directly related to the importance of an edge. However, this assumption might not be valid.

A-minimum-spanning-tree-based-filter-(MST-k),-also-known-as-an-orthogonal-minimum-spanning-tree-[78],-addresses-this-concern-as-it-selects-a-mix-of-edge-weights-and-always-produces-a-connected-graph,-i.e.⁻ a-path-exists-among-all-nodes.⁻ Briefly,-the-MST-algorithm-[209]-aims-to-extract-a-backbone-of-a-graph-with-N nodes-by-selecting-N - 1-edges,-such-that-the-sum-of-weights-is-minimised.⁻ We-use-Prim's-algorithm-for-computing-MST-[209].⁻ In-the-case-of-brain-graphs,-a-stronger-edge-weight-implies-a-higher-degree-of-coupling;-thus,-we-use-an-inverted-MST-algorithm,-which-maximises-the-sum-of-weights-instead.⁻ When-k = -1,-MST-k-is-equal-to-a-single-iteration-of-the-MST-algorithm.⁻ For-k > 1,-the-edges-selected-by-the-previous-iterations-are-removed-from-the-graph,- and- the-MST-algorithm-is- re-run.⁻ Thus,- the-MST-k-filter-selects-k(N - 1)-edges.⁻

Hyper-parameter-	Values-	GNN-	SVM-NS-	SVM-AM-	CNN-	MLP-
Cost-	[0,1]-		✓	1		
Batch-size-	$\{16, -32, -64, -128, -256\}$	1			1	1
Learning-rate-	$\{0.0001, -0.001, -0.01, -0.1\}$	1			1	1
GCN_hidden-	${256,-516,-1024,-2048,-4096}$	1				
N_GCN-	$\{1,2\}$	1				
N_Linear-	$\{1,2,3,4,5\}$					1
Conv1_hidden-	$\{16, -32, -64, -128\}$				1	
Conv2_hidden-	$\{16, -32, -64, -128\}$				1	
Linear_hidden-	[32, -64, -96, -160, -256, -516]-				1	1
Activation-	${ReLU, -Tanh}$				1	1
edge-dropout- layer-(DropEdge)-	${True, False}$	1				
Dropout_p-	{0.1,-0.25,-0.5,-0.75,-0.8,- 0.9}	1			1	1
Frequency-band-	delta,-theta,-alpha,-beta,- gamma,-full-	1	1	1	1	
Edge-filter-	full, top-{10,20,30}, MST-{1,2,3}	1	1	1	1	
Gamma-	$\{0.8, -0.85, -0.9, -0.95\}$	✓			✓	1

Table 5.1: Possible values for hyper-parameters of GNN, SVM-NS, SVM-AM, CNN and MLP.

5.2.3 Graph Neural Network Classification

GNN-is-an-extension-of-an-artificial-neural-network-that-is-capable-of-learning-on-graphstructured-data.- Specifically,-we-implement-a-graph-convolutional-network-(GCN)-fora-graph-classification-task-(Figure-5.1A).-

The input-to-the-GCN-classifier-is-in-the-form-of-a-graph:- $G = \{N, E, F\}$, where N, E, and F are sets-of-nodes, edges-and-node-features, respectively. The nodes-are-fixed-in-our-case, as-this-is-the-number-of-EEG-electrodes. The set-of-edges-E is given-by-the-adjacency-matrix-A computed-by-the-FC-measures-introduced-in-the-previous-section. Finally, the node feature matrix F is an $N \times D$ matrix where each row encodes a D-dimensional-feature-for-the-corresponding-node. Specifically, PSD-is-computed-over-1-Hz-increments-in-an-interval-between-0-and-100-Hz, forming-a-100-dimensional-node-feature-vector-(i.e.-D=100).

GCN-is-based-on-the-message-passing-framework, which-assumes-that-neighbouringnodes-should-have-similar-node-features. Briefly, a-GCN-layer-updates-the-node-features-(i.e.-messages)-using-the-optionally-transformed-messages-collected-from-neighbouringnodes. On-a-node-level, a-single-GCN-layer-effectively-aggregates-information-fromthe-1-hop-neighbourhood-of-each-node. Thus, stacking-L GCN-layers-represents-aggregation-from-*L*-hop-neighbourhood.- Formally, the GCN-layer-is-implemented-on-a-node-level-as-follows-[195]:-

$$x_i^l = \Theta_1 x_i^{l-1} + \Theta_2 \max_{j \in G_i} e_{ij} x_j^{l-1},$$
(5.11)

where x_i^l is the node features of node i at the l^{th} layer, x_i^0 is the i^{th} row of the inputnode feature matrix F, and Θ is a learnable linear transformation, which maps the node features from shape [1, D]-to [1, -GCN-hidden]. G_i and e_{ij} are the neighbourhood of node i and the edge weight connecting nodes i and j given by the set of edges Erespectively. The GCN-hidden is a tunable hyper-parameter of the GCN architecture. A rectified-linear unit (ReLU) activation is applied to the output of GCN, and batch normalisation is performed [120]. We refer to the node wise outputs of GCN as node embeddings.

After-L GCN-layers-are-applied, the output-is-constructed-by-node-embeddings-inthe-form-of-a- $N \times H$ matrix, where-H is the hidden-size-given-by-GCN-hidden. In orderto-produce-a-graph-level-embedding, a-maximum-readout-layer-is-applied, resulting-inan-H-dimensional-graph-embedding-r for-each-graph-g.

$$r_g = \max_{i=1}^N x_i^L, \tag{5.12}$$

where x_i^L is the output of the L^{th} GCN-layer for the i^{th} node. Following the readout layer, two-linear-layers are applied to produce the final classification with output dimensions H/2 and 2 (number of classes), respectively. Two-linear-layers were used to allow for further refining of the graph embedding before outputting the predicted class probabilities.

Additionally, in order to improve the generalisability and reduce the risk of overfitting, dropout layers are utilised (5.1A). Briefly, the dropout layer randomly zeroes elements of the input tensor with p probability drawn from a binomial distribution, where p is a hyper-parameter. A dropout is applied to the graph embeddings, i.e. after the readout layer and after the first linear layer. Furthermore, an edge dropout is implemented, which randomly removes edges from the input graph. The inclusion of the edge dropout in the model is controlled by a hyper-parameter.

In-summary, the GNN-used-in-this-study-has-several-hyper-parameters, as shownin-Table 5.1, which control (1)-the model architecture, (2)-the form of input data, and (3)-the training process to prevent overfitting. In particular, (1)-is enabled bythe number of GCN-layers (N-GCN) and the inclusion of DropEdge; (2) is enabled by frequency band and edge filter; and finally, (3) is enabled by dropout probability (drop-p), learning rate, gamma and batch size.

5.2.4 Baseline Models

In order to enable a fair assessment of the advantages of using graph-based learning (i.e. the GNN), four baseline classifiers are trained and compared. These baseline models utilise the same graph-structured input data extracted using different FC measures, frequency bands and edge filters, and the same evaluation process. Thus, we argue this to be a fair comparison of models.

The three-selected baseline-models are based on previously used classifier strategies for learning on FC brain-graphs: SVM-trained on node strength (SVM-NS)-[202], SVM-trained on vectorised adjacency matrix (SVM-AM)-[197], and CNN-trained on image of adjacency matrix [217, 169]. Additionally, we train a MLP on the flattened node feature matrix that was previously used to train the GNN-models.

Support Vector Machine Baseline Models

The SVM-NS and SVM-AM are both trained using an SVM classifier. SVM has only one hyper-parameter, namely the cost, as shown in Table 5.1. Additionally, in order to select an appropriate kernel for SVM, we include two kinds of kernels as hyper-parameters: radial and polynomial (up to 3rd order). Both of the SVM based baseline models are trained on manually extracted features. All features are first normalised to zero mean and unit standard deviation.

The SVM-NS-is-trained-on-node-strengths (Figure 5.1B). Node-strength is definedas-the-sum-of-edge-weights-of-one-node-and-can-be-interpreted-as-a-measure-of-nodeimportance. Thus, each-brain-graph-is-represented-by-an-23-dimensional-feature-vector- $NS = (ns_1, ns_2, ..., ns_N)$, where N is the number-of-nodes (N =-23).

The SVM-AM-is-trained-on-vectorised-weighted-adjacency-matrices-(Figure 5.1D). As-we-use-only-undirected-FC-measures, the $N \times N$ adjacency-matrix-of-a-brain-graphis-symmetric. Thus, we-can-use-the-upper-triangular-matrix-only-and-flatten-it-to-forma-253-dimensional-feature-vector- $(N \times (N-1)/2)$. Principal-component-analysis-(PCA)is-optionally-employed-for-dimensionality-reduction-with-the-number-of-componentsselected, such-that-95%-of-the-variance-is-captured. A-hyper-parameter-controls-theinclusion-of-the-PCA-step.

Convolutional Neural Network

CNN-classifiers-are-trained-on-the-weighted-adjacency-matrices-of-the-brain-graphs. As-the-adjacency-matrix-is-a-square-matrix,-it-is-simple-to-convert-it-to-an-image-onwhich-a-CNN-can-be-trained.

The CNN-architecture-consists-of-two-convolutional-blocks-and-a-final-classifier,-asshown-in-Figure-5.1C.-Each-convolution-block-contains-two-convolutional-layers-(stride-=-3),-followed-by-a-maximum-pooling-layer-and-a-dropout-layer.- The-final-classifierconsists-of-two-linear-layers-with-a-dropout-between-them.- We-created-several-hyperparameters-to-control-the-CNN.- The-number-of-convolutional-filters-within-each-block-iscontrolled-by-the-Conv1-and-Conv2-hyper-parameters.- Similarly,-the-hidden-size-of-thelinear-layers-is-controlled-by-the-Linear-hidden-hyper-parameter.- Additionally,-thereare-hyper-parameters-controlling-the-dropout-probability,-the-choice-of-the-activationfunction-(ReLU-or-Tanh),-and-the-batch-size-as-shown-in-Table-5.1.-

Multilayer Perceptron

MLP-classifiers-are-trained-using-the-flattened-node-feature-matrix- $F \in \mathbb{R}^{N \times D}$, where D is the PSD-computed-over-the-range-1-100-Hz. Thus-the-entry- F_{ij} corresponds-to-PSD-of-the- i^{th} node-at-frequency-j. The-MLP-is-thus-trained-on-the-input-used-to-train-the-GNN-models, but-without-leveraging-the-topological-information-provided-by-the-FC-graph. The-MLP-architecture-is-controlled-by-the-following-hyper-parameters:-N-Linear-(number-of-layers), Linear-hidden-(hidden-size). Additionally, there are hyper-parameters-controlling-the-dropout-probability, the choice-of-the-activation-function-(ReLU-or-Tanh), and the batch-size as shown-in-Table-5.1.

5.2.5 Model Evaluation and Implementation

The EEG preprocessing, brain graph construction, and model evaluation are implemented in R-4.1.2 [213] using in-house scripts, and caret [153] for SVM training. The training of CNN and GNN classifiers is implemented using PyTorch 1.10 [205] and PyTorch Geometric 2.0.2 [89].

The models are trained and evaluated based on repeated 20-fold cross-validation (CV). A-5-times repeated CV-is-used in order to identify the best combination of hyperparameters for all models and FC measures. The folds used for CV are created, such that samples from the same subject are kept within a single fold in order to prevent information leakage. We use a smaller number of repetitions in order to reduce the computational-cost-of-training-CNN-and-GNN-models.-Hyper-parameter-values-are-selected-using-random-optimisation, where-the-values-of-all-hyper-parameters-are-selectedrandomly.- 200-iterations-of-random-optimisation-are-performed-for-each-combinationof-FC-measure-and-model-type.- The-hyper-parameters-of-all-three-model-types-andtheir-possible-values-are-summarised-in-Table-5.1.-

The best-performing models are selected using the area under the sensitivity specificity curve (AUC), i.e. one-model-per-each combination of FC-measure and model-type. In order to assess the stability of the selected models, 50 times repeated CV-is performed. The performance errors are computed using the maximum difference between the mean and 5th and 95th quantiles. This approach does not assume a normal distribution and results in conservative error estimates.

The CNN-and-GNN-models-are-trained-using-an-Adam-optimiser-with-an-exponential-learning-rate-decay-(controlled-by-the-gamma-hyper-parameter)-and-cross-entropyloss-function.- The-models-are-trained-for-300-epochs-with-an-early-stopping-after-15epochs-if-the-loss-stops-decreasing.-

5.3 Results

Brain-graphs-were-inferred-for-each-3-second-long-EEG-segment-by-using-several-commonly-used-FC-measures, which-aim-to-quantify-both-the-linear-and-nonlinear-couplingbetween-pairs-of-brain-signals. The-brain-graphs-were-then-used-as-an-input-to-trainthe-GNN-brain-graph-classifier. Moreover, four-baseline-models-were-trained-on-thesebrain-graphs-in-order-to-demonstrate-which-type-of-classifier-performs-the-best. AUCis-used-to-select-the-best-model.

Table-5.2-reports-the-AUC-values-and-the-95%-confidence-intervals-of-the-SVM-NS,-SMV-AM-and-CNN-baseline-models-and-GNN-across-the-8-FC-measures. Note-thatthe-MLP-baseline-is-not-included-here, since-it-does-not-utilise-the-FC-brain-graphs. Additionally, the performance of the baseline-GNN-using-Euclidean-distance-betweenspatial-positions-of-EEG-(GNN-euclid)-is-reported-in-Table-5.2-as-well. The hyperparameter-values-of-the-best-models-from-their-respective-categories-are-reported-in-Table-5.4. The averaged-sensitivity-specificity-curves-of-these-models-are-shown-in-Figure-5.2.

All-baseline-models-perform-worse-than-all-of-the-GNN-models-across-all-FC-measures-as-shown-in-Table-5.2.- Even-the-best-baseline-model,-MLP-(AUC=0.95),-achieveslower-performance-than-the-worst-GNN-model,-GNN-euclid-(AUC=0.978).-

Table 5.2: AUC of GNN, SVM-NS, SVM-AM and CNN models across different FC measures measured by 50-repeated 20-fold cross-validation. The 'euclid' entry refers to the baseline GNN model with a fixed graph structure based on the spatial distance of EEG electrodes.

FC-	GNN-	SVM-NS-	SVM-AM-	CNN-
AEC-	0.984 ± 0.002	0.75 ± 0.022 -	0.734 ± 0.01	0.886-±0.019-
COH-	0.982 ± 0.002	0.773 ± 0.007 -	0.784 ± 0.008	0.901 ± 0.014
PCC-	0.982 ± 0.003 -	0.764 ± 0.008 -	0.773 ± 0.008 -	0.887 ± 0.014
euclid-	0.978 ± 0.004	X	X	X
iCOH-	$0.984\ {\pm}0.002$	0.656 ± 0.017 -	0.648 ± 0.014	0.876 ± 0.01
MI	$0.981 - \pm 0.002$ -	$0.807\ {\pm}0.008$	0.779 ± 0.013 -	$0.924\ {\pm}0.015$
PLI	0.982 ± 0.005 -	$0.761 - \pm 0.057$ -	$0.603 - \pm 0.036$ -	0.893 ± 0.015
PLV-	0.982 ± 0.003 -	0.766 ± 0.008 -	$0.793\ {\pm}0.007$	0.9-±0.014-
wPLI-	0.984 ± 0.003	0.66 ± 0.069	0.637 ± 0.024	0.869 ± 0.016

Table 5.3: Detailed performance metrics of best-performing models (selected based on AUC) of each model type.

	AUC-	Accuracy-	Sensitivity-	Specificity-
GNN-(AEC)-	0.984-±0.002-	91.996%-±0.41-	97.366%-±0.941-	86.716%-±1.013-
GNN-euclid-	0.978 ± 0.004	91.147%-±1.278-	93.678%-±2.46-	88.658%-±3.497-
CNN-(MI)-	0.924 ± 0.015	84.689%-±2.233-	86.212%-±3.6-	83.192%-±4.613-
SVM-NS-(MI)-	0.807-±0.008-	73.924% - ± 0.852 -	73.494%-±0.926-	74.367%-±0.934-
SVM-AM-(PLV)-	0.793-±0.007-	72.929% - ± 0.6 -	72.123%-±0.673-	73.799%-±1.064-
MLP-	0.953 ± 0.007	84.97%-±1.93-	82.77%-±2.31-	87.13%-±2.88-

From-Table-5.2, we can also see that the GNN models trained using FC-based brain-graphs perform better than GNN-euclid, which was trained using a static graph structure.

Furthermore, we report the effect of frequency bands and edge filtering methods on the performance of the trained models in the supplementary materials. Figure S3 and tables S1-S3 report these effects of frequency bands. Figure S4 and Tables S4-S6 report these effects of edge filtering methods.

5.4 Discussion

We-trained-GNN-models-over-several-commonly-used-FC-measures. For-comparison, we-trained-four-baseline-models. The results-suggest-that-the-GNN-outperforms-all-baseline-models-across-all-FC-measures-(Table-5.2). Moreover, neural-network-based-models-(GNN, CNN-and-MLP), which perform-automatic-feature-extraction, perform-

decisively-better-than-the-classical-machine-learning-approaches-(SVM-AM-and-SVM-NS)-that-rely-on-manually-engineered-features.

We argue that the relatively low performance of the machine learning approaches is caused by the inability to remove noise contaminated information from the inputfeatures. This is likely exacerbated by the lack of false positives control during the brain graph inference, which would limit the number of edges caused by spurious coupling. We suggest that the neural network based models can solve this issue by using weight regularisation and dropout layers, designed to learn generalisable features insensitive to noise.

It-could-be-argued-that-the-GNN-models-perform-better-than-CNN-and-MLPbecause-they-are-trained-using-two-input-information-sources, i.e.-the-FC-weightedbrain-graph-and-the-node-feature-matrix-with-power-spectral-density.-This-is-a-uniqueproperty-of-GNN-as-it-can-aggregate-information-from-both-inputs.-Moreover, to-thebest-of-our-knowledge, GNN-is-the-only-model-architecture-that-can-process-these-twoinputs-simultaneously.-

The CNN and MLP baseline models offer an interesting comparison to the GNNsince each is trained using one of the two input information sources. The CNN and MLP baselines show the individual predictive power of the FC based brain graph and node feature matrix, respectively. The results suggest that the node feature matrix provides a slightly better source of information in the classification task (Table 5.3). However, GNN performs significantly better, and we argue that the comparison with the CNN and MLP baselines highlights the power of GNN in brain graph classification.

The relatively poor performance of CNN also demonstrates the shortcomings of treating the adjacency matrix of a brain graph as an image. Each pixel of an image has an equal number of neighbouring pixels, and the content of the image depends on the specific spatial ordering of its pixels. Therefore, convolution can be applied to patches of pixels to extract features automatically. This assumption is invalid for a graph where each node can be connected to an arbitrary number of neighbours and no meaningful ordering of nodes exists. In contrast, graph convolution generalises the convolution to solve this issue efficiently by utilising order invariant operations to aggregate information from neighbouring nodes.

Moreover, the hyper-parameter optimisation has identified a GNN-model with twograph convolutional layers as the optimal GNN architecture (Table 5.4). This means that the GNN aggregates information not only from the nodes connected by an edge directly (i.e., the 1-hop neighbours) but also from the 2-hop neighbours. This suggests the importance of global graph properties in diagnosing AD accurately, in addition to the local properties, which could likely be learned with a single layer. This is in line with the reported loss of small-world properties of AD brain graphs [247, -136, -277, -263].

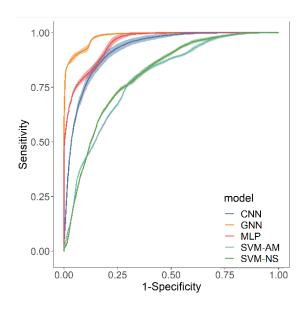


Figure 5.2: Averaged Sensitivity-Specificity curves of the best models of their respective categories with 95% confidence intervals (ribbon).

Next,- the- results- demonstrate- thatthe FC-based GNNs also outperform the GNN-euclid model, which utilises a static-graph-structure-(Table-5.2).- Thissuggests- that- it- is- preferable- to- utilise-FC-based-brain-graphs-rather-than-thedistance-based- static- graphs- previouslyused-for-EEG-GNN-tasks-[77,-269].-However,-it-seems-that-no-FC-measure-offersclearly-superior-performance-compared-tothe others. Thus, we suggest that futurestudies-need-to-carefully-consider-which-FC- measure- to- use- based- on- the- typeof-brain-coupling-they-might-wish-to-focus-on.- However,-we-do-not-claim-thatthe-brain-graphs-inferred-from-various-FCmeasures- are- necessarily- similar- from- a-

graph-theoretic-perspective.- This-is-supported-by-the-performance-differences-of-the-baseline-models-where-some-of-the-FC-measures,-such-as-MI,-perform-consistently-well.-

Surprisingly, the GNN-euclid-model-achieves-relatively-high-accuracy-despite-utilising-a-fixed-graph-structure-(Table-5.3). The Euclidean-brain-graph-structure-highlightsthe spatially-local-relationships-between-the EEG-channels. In contrast, long-rangeedges-have-only-a-low-weight. Therefore, we argue that the Euclidean-brain-graph-biases-the-GNN-model-to-learn-local-graph-features-predominantly. On the other-hand, the FC-based-brain-graphs-may-contain-both-local-and-long-range-relationships. Previous-research-suggests-that-AD-related-differences-are-observed-in-long-range-pathwaysand-global-graph-properties-[13,-247,-277]. In-our-opinion, the FC-based-GNNs-outperform-GNN-euclid-since-they-can-better-capture-both-the-local-and-global-differenceson-the-graph-level.

To investigate the differences between FC measures on the graph level further, we compute an average adjacency matrix for each FC measure across both groups and frequency bands (Figure S1). In Figure 5.3, we show these matrices for α and θ

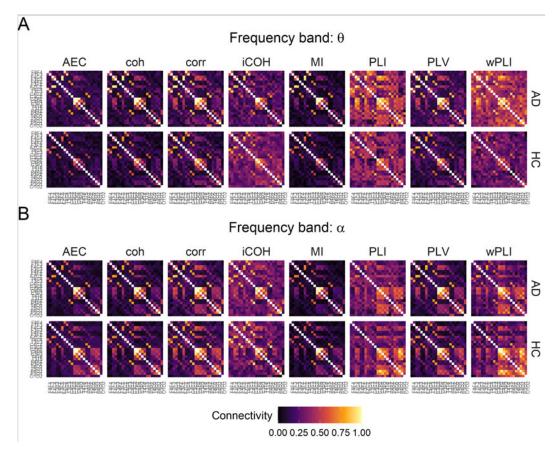


Figure 5.3: Averaged adjacency matrices of AD and HC cases measured with various functional connectivity measures in A) θ (best in CNN, SVM-NS and SVM-AM models), and B) α (best in GNN model) frequency bands.

frequency-bands-as-these-are-utilised-by-the-best-performing-models-(Table-5.4).- Thebrain-graphs-are-relatively-similar-across-the-FC-measures.- In-the- θ band,-increasedconnectivity-can-be-observed-in-AD-compared-to-HC.- In-contrast,- the-connectivityseems-to-be-decreased-in-AD-in-the- α band.- These-differences-are-well-documented-inthe-literature-[68,-267,-13].-

Interestingly, all-FC-measures-detect-a-well-defined-cluster-containing-mostly-parietal-and-occipital-EEG-channels.- The-strength-of-this-cluster-distinguishes-AD-from-HC-consistently-across-FC-measures.- We-speculate-that-this-cluster-contributes-mostof-the-predictive-information-for-the-classification-models.- However, since-the-GNNarchitecture-is-a-block-box-model, it-would-be-difficult-to-confirm-our-speculation.-

Next, the optimised model architectures suggest that using edge-filtering and filtering the EEG signal within a frequency band improve the model performance. A detailed report of differences between the edge-filtering methods and frequency bands

Hyper-parameter-	GNN-	SVM-NS-	SVM-AM-	CNN-	MLP-
FC-measure-	AEC-	MI-	PLV-	MI-	
Batch-size-	32-			64-	32-
Learning-rate-	0.001-			0.001-	0.01-
GCN_hidden-	1024-				
N_GCN-	2-				
N-Linear-					4-
Conv1_hidden-				128-	
Conv2_hidden-				64-	
Linear_hidden-				96-	4096-
Activation/Kernel-		Radial-	$Poly(1^{st})$	ReLU-	ReLU-
DropEdge-	TRUE-				
Drop_rate-	0.9-			0.1-	0.05-
Frequency-band-	alpha-	theta-	theta-	theta-	
Edge-filter-	Top- 20%-	MST-3-	full-	full-	
Gamma-	0.9-			0.9-	0.95-

Table 5.4: Hyper-parameter values of the best performing GNN, SVM-NS, SVM-AM, CNN and MLP measured by AUC.

across-the-FC-measures-and-model-types-is-included-in-the-supplements-(Figures-S3-S4and-Tables-S1-S6).- Briefly,-the-best-GNN-model-utilises-the- α frequency-band,-and-CNN,-SVM-AM-and-SVM-NS-utilise-the- θ frequency-band-(Table-5.4),-suggesting-thatfrequency-centred-brain-graphs-should-be-preferred-over-the-full-frequency-range-braingraphs.- The-selection-of-these-frequency-bands-is-not-surprising,-as-they-are-both-wellknown-to-be-altered-in-patients-with-AD-[68,-267,-13].- In-contrast,-the-effect-of-edgefiltering-is-not-so-apparent-as-only-the-GNN-and-SVM-NS-models-use-edge-filteringwith-top-20%-and-MST-3,-respectively.- On-the-other-hand,-CNN-and-SVM-AM-useunfiltered-brain-graphs.- We-expect-that-a-sparse-graph-is-preferable-for-GNN-sincethere- are-fewer-messages-to-aggregate-while-updating-the-node-embeddings.- Thesemessages- are-also-less-likely-to-be-a-product-of-false-positive-brain-interaction,- thusleading-to-better-node-and-graph-embeddings.-

Furthermore, it-is-worth-noting-that-although-GNN-accepts-two-inputs, the relativecontribution-of-each-input-information-is-largely-unclear. The results-suggest-that-thenode-feature-matrix-should-contribute-slightly-more-since-the-MLP-baseline-outperforms-the-CNN-(Table-5.3). It-could-be-argued-that-the-GNN-uses-only-the-topologicalinformation-provided-by-the-graph-structure-to-enable-message-passing, but-the-FC-isnot-fully-reflected-in-the-node-embeddings-and-graph-embeddings, by-extension. Nevertheless, we believe that the FC information is utilised to some extent by the GNNs since these models perform better than the GNN-euclid, which arguably utilises merely the topological information (Table 5.2). However, the extent to which the information provided by the FC measures is contained within the learned graph embedding remains unclear. One can merely speculate without introducing an additional mechanism into the GNN architecture, which is beyond the scope of this chapter.

Finally, the GNN architecture utilised in this study is relatively simple as one of the simplest GCNs was used, and the readout layer merely computes the maximum of the node embeddings. Previous EEG-GNN applications demonstrated the advantages of using more complex graph convolutional layers and edge pooling mechanisms [77]. We hypothesise that exploiting a learnable edge-filtering mechanism akin to that utilised by Zhong et al. [311] might improve the classification compared to the edge-filtering methods used in this study.

5.5 Conclusion

GNN-is-an-effective-model-for-learning-on-graph-structured-data,-such-as-FC-EEGbrain-graphs.- However,-in-the-absence-of-consent-about-the-ideal-FC-measure-forestimating-EEG-brain-graphs,-the-effect-of-an-FC-measure-on-the-performance-of-GNNclassifiers-is-unclear.- In-this-chapter,-we-have-selected-eight-common-FC-measures-toinvestigate-this-effect.-

First, we demonstrated that GNN models are superior to classical machine learning and CNN models for brain graph classification. Unfortunately, the utilised GNN architecture is a black box model. Thus, future work should focus on implementing interpretable GNN architectures that achieve similar performance but additionally offerinterpretability, such as which nodes, i.e. brain regions, drive the prediction. Besides providing an opportunity for experts to validate such models, interpretable predictions might also serve in the development of GNN informed targeted treatment.

Finally, we showed that utilising FC measures to define the brain graph results in improved performance of GNN models compared to a fixed electrode distance based graph structure. While using an FC measure improves the performance, no concrete FC measure can be recommended as the ideal choice. Thus, in future research, the choice of suitable FC measure should be carefully evaluated in the context of the given research question. Alternatively, focusing on fusion methods might lead to developing a novel composite measure of FC.

5.6 Chapter Summary

This- chapter- systematically- evaluates- various- FC- methods- in- inferring- EEG- braingraphs- for- training- GNN- to- classify- AD- patients.- It- compares- GNNs- utilising- FCbased- brain- graphs- with- baseline- models,- demonstrating- the- superior- performance- of-GNN-models.-

The chapter emphasises that GNN, leveraging information from both FC braingraphs and node feature matrices, outperforms other models, highlighting the unique ability of GNNs to process these inputs simultaneously, unlike other DL and ML models.

The results indicate that FC-based graphs perform better than static distance graphs, suggesting that GNNs can effectively leverage the information about FC to improve predictions. Despite these successes, the choice of FC measure remains ambiguous as none of the testes FC measures perform significantly better than all others.

Additionally, the chapter explores the impact of frequency bands and edge filtering methods on model performance. Frequency band specific and sparse brain graphs are consistently favoured over full-frequency range and fully connected graphs.

This-chapter-focused-on-relatively-simple-GNN-architectures-to-highlight-the-generalstrengths-of-GNNs-and-to-fairly-test-the-effect-of-FC-measures.- However,-the-resultingmodels-do-not-offer-any-explainability,-a-crucial-property-for-predictive-modelling-inhealth-related-settings.- Thus,-future-work-needs-to-emphasise-explainability-to-allowfor-a-clear-interpretation-of-the-predicted-diagnosis-outcome.-

Chapter 6

Adaptive Gated Graph Convolutional Network for Explainable Diagnosis

6.1 Introduction

¹The brain-is-a-complex, densely-connected system that operates across multiple spatialand temporal scales. Neurological diseases, such as AD, can alter the connectivity of the brain and thus disrupt brain function [76, 72, 207, 150].

Multiple-studies-propose-GNN-based-architectures-to-process-EEG.-However,-GNNmethods-for-EEG-based-diagnosis-of-AD-are-limited-[142,-229].-GNN-EEG-implementations-often-include-several-steps:- (1)-input-construction,-i.e.- graph-structure-andnode-features;- (2)-GNN-encoder-to-learn-node-embeddings;- and- (3)-aggregation-ofnode-embeddings-to-a-graph-embedding,-which-can-be-used-in-the-final-classificationstep.-

There are various approaches to realise the graph construction in step (1). Node features are commonly defined as EEG time-series signal [229, 166, 8, 163], or a statistical summary of the signal in the time domain [214, 249], the frequency domain [142, 244], or the differential entropy [166, 291, 53, 132, 301, 244]. Based on NW-literature, many approaches define the brain graph using FC measures [142, 229, 178, 48,

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214.-249.-166.-163].- The-graph-structure-can-also-be-based-on-the-distance-between-EEG-electrodes-[249,-291,-53].-However,-such-an-approach-largely-ignores-brain-connectivity-information.- Alternatively, the brain-graph-can-be-automatically-learned-by-themodel, either-as-a-learnable-mask-shared-across-samples-[171, -166, -244]-or-by-pairwisenode-feature-distance-minimisation-regularised-by-an-additional-graph-loss-function-[311,-132,-301].-While-such-approaches-are-flexible-and-should-converge-to-an-optimalgraph-structure-with-respect-to-a-given-learning-task,-the-learned-brain-graph-mightnot-be-representative-of-the-underlying-brain-connectivity,-i.e.-such-a-graph-structuremight-overestimate-the-strength-of-the-task-relevant-edges-compared-to-the-underlyingconnectivity.- In-this-chapter, an-adaptive-graph-learning-mechanism-is-proposed-basedon-node-feature-enhancement-via-CNN-and-subsequent-graph-construction.- This-isachieved-using-a-correlation-similarity-measure-of-power-spectral-density-and-sparsifiedvia-k-nearest-neighbours-(KNN)-edge-selection.- Thus,-it-combines-the-strength-of-the-FC-based-and-automated-graph-learning-methods.-Such-a-combination-overcomes-thelimitations-of-fully-learnable-graphs-described-above-since-the-correlation-computationis-ultimately-detached-from-the-classification-task.- However,-it-should-be-noted-thatthe adaptively learned graph structure reflects brain region similarity rather than a functional-relationship-assumed-by-classical-FC-measures.-

The design of GNN encoders in step (2) for EEG applications has been mainly limited to simple architectures, such as the ChebConv [48, 8, 249, 291, 53, 132, 163], and simple GCN [142, 171, 307, 166, 244, 311]. However, we hypothesise that such node embedding updating mechanisms are not optimal for EEG tasks. These graph convolutions update node embeddings by summing the initial embedding and the aggregated messages from the neighbouring nodes. Such updating implies that information from different scales contributes equally to the final node embeddings, hence graph embeddings as well. While brain disruptions caused by AD occur across multiple spatial scales, their predictive power is likely different. Therefore, a gating mechanism is crucial for filtering and weighting the information collected across different scales. We propose to adopt the gated graph convolution [175]-to address this issue.

Finally, we implement the aggregation of node embeddings in step (3) by adopting the adaptive structure aware pooling (ASAP) node pooling mechanism [215] to first learn the most important clusters of nodes, which are in turn concatenated to form the graph embedding. This is in contrast to the previous approaches that do not use any node pooling and form graph embeddings via simple element-wise readout layers [142, 289, 214, 166, 307, 178, 311] or concatenating all nodes of the graph [229, 48].

Other-node-pooling-approaches-were-tested-for-EEG-applications-[77,-289].-In-contrastto-ASAP-pooling, these-approaches-pool-the-graph-by-selecting-a-specified-number-ofnodes-without-considering-their-local-context-within-the-graph.- Therefore, importantinformation-might-be-lost-due-to-such-node-pooling.-

In this chapter, we propose a novel GNN model for explainable AD classification, which can adaptively enhance node features and dynamically construct brain graph structures as shown in Figure 6.1. The learned brain graphs can then be used for the interpretation of predictions. Moreover, a clustering based node pooling mechanism is adopted to coarsen the brain graph, thus localising the brain regions that contribute to the predictions. Finally, we conduct extensive ablation and parameter sensitivity experiments to elucidate the importance of the individual blocks within the proposed model architecture.

6.2 Methods

The proposed adaptive gated graph convolutional network (AGGCN) model consists of three blocks: a graph learning module, a GNN encoder and a classifier. The graph learning module receives a node feature matrix as input, enhances it using a 1D-CNN and learns the brain graph structure. The GNN encoder then uses the output of the graph learning module as input, i.e. a featured, weighted, undirected graph. The encoder generates a graph embedding used by the classifier to output the predicted probabilities.

6.2.1 EEG Pre-processing

As-a-neurophysiologist-confirmed-the-EEG-signal-to-be-artefact-free,-we-did-not-furtherclean-the-signals.- The-signals-are-filtered-using-a-band-pass-Butterworth-filter-to-a-rangeof-0.5-Hz-and-45-Hz-and-down-sampled-to-200-Hz.- Finally,-1-second-long-windows-with-50%-overlap-are-created-to-increase-the-sample-size.-

6.2.2 Node Feature and Graph Learning

The node-features are defined as power spectral density computed from 1-second long-EEG-signals with 1-Hz-increments from 1-to 45-Hz. Hence, the input is a node feature matrix $\mathbf{X} \in \mathbb{R}^{N \times D_{in}}, D_{in} = 45.$

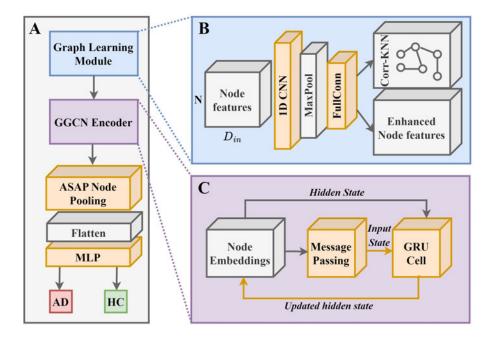


Figure 6.1: The architecture of the proposed adaptive gated graph convolutional network. A) The proposed model consists of a graph learning module, gated graph convolutional neural network (GGCN) encoder, ASAP node pooling module, and a three-layer MLP outputting the predicted probabilities. B) Graph learning module takes a $N \times D_{in}$ node feature matrix as input. Node features are defined as power spectral density from 1 to 45 Hz ($D_{in} = 45$) computed for all N EEG electrodes (N = 23). Then, a 1D CNN enhances them. The brain graph structure is then constructed as a correlation graph between the outputs from the 1D CNN and made sparse by a k-nearest-neighbour edge selection (Corr-KNN). C) The enhanced node features and the learned graph structure are then passed to a GGCN encoder. GGCN applies message passing and gated recurrent unit (GRU) recursively over R iterations.

The input is then passed to a CNN with batch normalisation, L_{CNN} 1D convolutional layers and a maximum pooling with kernel size 2 and step size 2. The output is flattened and fed to a fully connected layer with hidden size h_{CNN} and batch normalisation. This neural network outputs a matrix of enhanced node features $\mathbf{X}' \in \mathbb{R}^{N \times D_{h_{CNN}}}$.

A-graph-structure-is-then-inferred-from-the-enhanced-node-features-by-computingthe-absolute-value-of-Pearson's-correlation-for-each-pair-of-nodes. Thus, a-uniquegraph-structure-is-learned-for-each-input-sample-and-is-defined-by-an-adjacency-matrix- $\mathbf{A} \in \mathbb{R}^{N \times N}$ with N = 23-being-the-number-of-EEG-channels. In-order-to-producesparse-graphs, the k-nearest-neighbours-algorithm-is-utilised. This-means-that-the kstrongest-edges-are-preserved-for-each-node. This-proposed-graph-learning-module-has-multiple-hyperparameters-that-control-itsarchitecture. Namely, these are the number of convolutional-layers- L_{CNN} , the kernelsize (which-is-equal-to-the-step-size), the number of filters, the hidden-size h_{CNN} , the dropout-rate- $drop_{CNN}$ and the k_{KNN} parameter that controls the graph-sparsity.

6.2.3 Graph Neural Network Encoder and Classifier

A-graph-convolution-extends-the-classical-convolution-from-the-Euclidean-domain-to-thegraph-domain.- The-input-graph-is-given-by- $G = (\mathbf{N}, \mathbf{A}, \mathbf{X}')$ -where-N is-the-set-of-nodes,- \mathbf{A} is-the-learned-graph,- and- \mathbf{X}' is-the-enhanced-node-feature-matrix.- A-simple-graphconvolution-is-defined-by-the-message-passing-mechanism-wherein-the-node-embeddingof-node-i is-learned-by-aggregating-information-from-its-1-hop-neighbourhood,- i.e.nodes-connected-with-an-edge,-as-follows:-

$$\mathbf{x}_{\mathbf{i}}^{\mathbf{l+1}} = \mathbf{x}_{\mathbf{i}}^{\mathbf{l}} + \mathbf{\Theta} \sum_{j \in N(i)} e_{ij} \mathbf{x}_{\mathbf{j}}^{\mathbf{l}}, \tag{6.1}$$

where $\mathbf{x_i^l}$ are the node features of node i at the l^{th} layer, $\mathbf{x_i^0}$ is the i^{th} row of the input-node feature matrix \mathbf{X} , and $\mathbf{\Theta}$ is a learnable linear transformation. N(i) and e_{ij} are the neighbourhood of node i and the edge weight connecting nodes i and j given by the adjacency matrix \mathbf{A} , respectively. Stacking L graph convolutional layers then means aggregating information iteratively from 1-hop to L-hop neighbourhoods, thus gradually going from local to global information about the graph.

Note-that-the-aggregated-message-is-added-to-the-initial-node-embedding- \mathbf{x}_{i}^{1} . Thus,-the-entire-information-collected-from-each-L-hop-neighbourhood-is-always-fully-integrated-into-the-node-embedding. However, information-might-be-distributed-unequally-across-spatial-scales-in-brain-graphs. The-GGCN-[175]-addresses-this-problem-by-in-troducing-a-mechanism-to-decide-what-information-should-be-retained-at-each-scale-selectively:-

$$\mathbf{m}_{\mathbf{i}}^{(\mathbf{r+1})} = \sum_{j \in N(i)} e_{ji} \cdot \mathbf{\Theta}^{\mathbf{r+1}} \cdot \mathbf{x}_{\mathbf{j}}^{(\mathbf{r})}, \tag{6.2}$$

$$\mathbf{x}_{i}^{(\mathbf{r+1})} = \operatorname{GRU}(\mathbf{m}_{i}^{(\mathbf{r+1})}, \mathbf{x}_{i}^{(\mathbf{r})}), \tag{6.3}$$

where $\mathbf{m_i}$ are the aggregated messages, \sum is the aggregation function, $\Theta^{\mathbf{r}}$ is a learnable matrix for iteration r, which maps the node features from shape $[1, D_{h_{CNN}}]$ to $[1, D_{h_{GNN}}]$, and GRU-is the gated recurrent unit [56]. Briefly, a GRU-is a recurrent neural-network-layer-with-update, reset, and input-gates that allow the network to recursively update or forget information about the input. The node embeddings are learned recursively up to R iterations with a shared GRU-gate, which is equivalent to stacking R GCN-layers.

The node embeddings are then passed through an activation function and a batchnormalisation layer. Finally, the node embeddings are passed to the node pooling module. The hyperparameters of the proposed encoder are the number of iterations R, the hidden size h_{GNN} , the activation function, the aggregation function and the dropout rate $drop_{GNN}$ applied after the encoder.

Node Pooling

After-learning-the-node-embeddings, the model-learns-a-coarsened-graph-using-the-ASAP-pooling-mechanism-[215]. This-pooling-first-learns-N clusters, each-centred-at-one-node, also-named-ego-graphs. The membership-of-node j in the ego-cluster-centred-at-node-i is given-by-the $\mathbf{S_{ij}}$ matrix. Note-that-this-is-a-soft-cluster-assignment-matrix; thus, each-node-can-belong-to-multiple-clusters-with-varying-membership-strengths. The clusters-are-learned-as-follows:-

$$S_{ij} = a_{ij}, \tag{6.4}$$

$$a_{ij} = \operatorname{softmax}\left(\theta^{\mathrm{T}} \sigma \left(\boldsymbol{\Theta} \mathbf{x}_{\mathbf{i}}^{\mathrm{m}} \| \mathbf{x}_{\mathbf{j}}\right)\right), \qquad (6.5)$$

$$\mathbf{x}_{\mathbf{i}}^{\mathbf{m}} = \max_{j \in N(i)} \mathbf{x}_{\mathbf{j}},\tag{6.6}$$

where a_{ij} is the attention score and the membership strength, θ and Θ are learnable vector and matrix, respectively. σ is the LeakyReLU activation function, and $\mathbf{x_i^m}$ is the master query representing the initial cluster embedding. The attention scores are also subject to a dropout probability $drop_{pool}$. The final cluster embedding is then calculated as an attention weighted sum, which is additionally weighted by the cluster score ϕ_i :

$$\mathbf{x_i^c} = \phi_i \sum_{j \in N(i)} a_{ij} \mathbf{x_j},\tag{6.7}$$

where the cluster score ϕ_i is computed by the local extremum graph convolution [215]:-

$$\phi_i = \Theta_1 \cdot \mathbf{x_i} + \sum_{j \in N(i)} e_{ji} \cdot (\Theta_2 \mathbf{x_i} - \Theta_3 \mathbf{x_j}), \qquad (6.8)$$

Condition-	Accuracy-	AUC-	Sensitivity-	Specificity-	F1-
EC-	$89.1^{-}\pm 1.4^{-}$	0.895 ± 0.016	$92.95^{-}\pm 2.59^{-}$	$85.16^{-}\pm 2.45^{-}$	89.7-± 1.4-
EO-	85.56 ± 0.96	0.834 ± 0.015	$90.88^{-}\pm 2.01^{-}$	79.98 ± 1.47	86.55 ± 0.98
EC+EO-	$81.79^{-}\pm 1.26^{-}$	$0.82^{-}\pm 0.016^{-}$	84.27 ± 2.19	$79.22^{-}\pm\ 2.05^{-}$	$82.46^{-}\pm 1.27^{-}$

Table 6.1: Performance of the proposed AGGCN in EC, EO and combined (EC+EO) conditions.

which is designed to measure the relative importance of each cluster.

The cluster embedding \mathbf{x}_{i}^{c} is then used to select the top k scoring clusters, which will be included in the coarsened graph:

$$\bar{i} = Top_k(\mathbf{X}^{\mathbf{c}}), k \in [1, 2, \dots N], \qquad \bar{\mathbf{S}} = \mathbf{S}(:, \bar{i})$$
(6.9)

$$\mathbf{A}^{\mathbf{p}} = \mathbf{\bar{S}}^{\mathrm{T}} \cdot \mathbf{A} \cdot \mathbf{\bar{S}}, \qquad \qquad \mathbf{X}^{\mathrm{p}} = \mathbf{X}^{\mathbf{c}}(:,\bar{i})^{-} \qquad (6.10)^{-1}$$

where Top_k is a function that returns the indices of clusters \overline{i} . $\overline{\mathbf{S}}$ and $\mathbf{X}^{\mathbf{p}}$ are the prunedsoft-cluster assignment matrix and the pruned cluster embedding matrix, respectively, and $\mathbf{A}^{\mathbf{p}}$ is the adjacency matrix of the coarsened graph.

The graph-pooling module has the following hyperparameters: the size of the pooled graph k_{pool} , the dropout rate $drop_{pool}$ and the negative slope of the LeakyReLU activation.

Multilayer Perceptron Classifier

The cluster embedding matrix $\mathbf{X}^{\mathbf{p}}$ of the coarsened graph returned by the node pooling module is flattened and fed to a MLP classifier. Specifically, a L_{MLP} -layer MLP with hidden size h_{MLP} is utilised with a block of batch normalisation, activation function, and dropout layers utilised between the fully connected layers. The final layer outputs a two-dimensional vector of log-probabilities for each class.

The classifier has the following hyperparameters: the number of layers L_{MLP} , hidden-size h_{MLP} , activation function and dropout rate $drop_{MLP}$.

6.2.4 Model Implementation and Evaluation

The proposed AGGCN-model-was-implemented-using-PyTorch-1.10-[205], and PyTorch-Geometric 2.0.2 [89] and trained on a laptop with Intel i7 CPU, 16 GB RAM and an NVIDIA RTX-2070 GPU.

The-model-is-trained-by-minimising-the-cross-entropy-loss.- The-model-performance-

is evaluated using repeated (30 times) 10-fold stratified group cross-validation (onegroup = subject identifier) and trained on the dataset collected during the eyes-closed condition. Since all participants have multiple samples, keeping all the samples from the same participant within the same fold is crucial to prevent information leakage. In order to prevent overfitting, another fold is utilised for validation to implement early stopping and is used to optimise hyperparameters. Thus, in each iteration of the crossvalidation, one fold is used as validation, one fold as testing, and the remaining eight folds form the training set.

A-stochastic-gradient-descent-optimiser-and-an-exponential-learning-rate-schedulerare-used-to-train-the-model-with-a-batch-size-of-128-for-200-epochs.-If-validation-lossdoes-not-decrease-for-15-epochs,-the-training-is-stopped-early.-Additionally,-zero-mean-Gaussian-noise-with-standard-deviation- σ is-added-to-the-input-during-training-withprobability- p_{noise} to-improve-the-generalisability-of-the-model.- Eventually,-the-bestmodel-was-identified-using-the-average-cross-validated-F1-score-measured-on-the-validation-folds.-The-selected-model-was-then-retrained-and-tested-on-the-dataset-obtainedduring-the-eyes-open-condition-and-the-combined-dataset-from-both-conditions.- Thefinal-results-are-then-reported-using-the-test-folds-only.- The-stability-of-the-performance-is-assessed-by-computing-the-standard-deviation-of-the-samples-collected-overthe-30-times-repeated-cross-validation.-

Note-that-the-hyperparameters-of-the-proposed-model-are-optimised-using-Bayesianoptimisation. - Ten-warm-up-random-iterations-were-used-to-initialise-the-optimisation,followed- by- 200- optimisation- iterations. - The- optimisation- is- evaluated- only- on- thevalidation- sets- to- prevent- overfitting. - Moreover, - we- carry- out- parameter-sensitivityexperiments-to-verify-the-influence-of-a-few-key-hyperparameters-of-the-proposed-modelarchitecture. - Specifically, - these- are- the- number- of- iterations- of- the- GGCN- encoder, the- size- of- the- pooled- graphs, - the- sparsity- of- the- learned- graph- and- the- choice- ofaggregation-function-of-the-GGCN-encoder. - Due-to-the-computational-cost-of-runningthese-experiments, -we-reduce-the-number-of-repeats-of-the-cross-validation-from-30-to-5. - The-hyperparameters-of-the-model-are-reported-in-Appendix-C-(Table-C.2).-

6.3 Results and Discussion

In-this-section,-we-report-the-experimental-results-of-our-AGGCN-model.-As-illustratedin-Table-6.1,-our-AGGCN-has-shown-robust-performance-across-all-the-conditions.-Notethat-the-best-performance-was-achieved-during-the-EC-condition.-This-is-likely-becausewith eyes closed, the ocular artefacts are minimised; thus, the underlying dynamics are easier to detect. The performance remains high even in the EO condition, suggesting that the proposed model can detect underlying patterns in both EC and EO conditions. However, the performance decreases significantly on the EC+EO combined dataset. We hypothesise that the patterns learned under the EC and EO conditions share relatively little information; thus, the EC+EO model performs significantly worse. We explore this further in section 6.3.3.

In-addition,- the- hyperparameter- values- of- the- optimised- model- are- reported- in-Appendix-C-(Table-C.1).-

6.3.1 Comparison with the Baselines

The proposed model was compared to seven baseline models proposed in the literature across the three conditions. The first baseline is the best-performing model fromour previous work [142]. It is a GNN with two spatial graph convolutional layers, maximum readout and brain graph defined using the amplitude envelope correlation (AEC-GNN). The second baseline model is the spatio-temporal graph convolutional network (STGCN) that uses temporal convolutions and ChebConv layers and defines the brain graphs using wavelet coherence [229]. Then, two CNN-based models, PSD-CNN [118] and Wavelet-CNN [115], trained on PSD and wavelet transform, respectively, were used. Next, two traditional machine learning approaches were utilised: support vector machine trained on node degree computed from phase lag index graph (NS-SVM) [202], and a logistic regression trained on vectorised adjacency matrices obtained from coherence graphs across seven frequency bands (AM-SVM) [197]. Finally, we use an MLP model where the input is a flattened PSD node feature matrix [142] without using graph-domain information.

Table 6.2 shows the f1 scores of various models across different conditions. Note that all seven models were evaluated under the same setting (e.g. the same 1-second EEG window samples). We can observe that our proposed AGGCN outperforms the baselines across all conditions. Moreover, STGCN was originally evaluated using a cross-validation setup, which mixed samples from the same subject in their original paper. [229]. It is expected that its performance drops significantly when evaluated using stratified group cross-validation in our experiments.

Model-	EC-	EQ-	EC+EO-	No of-
WIOUEI		EO		parameters-
AEC-GNN-[142]-	81.61 ⁻ ± 3.16 ⁻	77.91 ± 1.1	76.74-± 1.87-	445,204-
MLP-[142]-	82.01 ± 4.39	76.51 ± 3.34	77.47-± 4.26-	54,628,354-
PSD-CNN-[118]-	88.15 ± 0.77	$80.89^{-}\pm 1.45^{-}$	79.51 ± 1.74	3,420,432-
STGCN-[229]-	46.71 ± 8.58	44.34-± 7.33-	38.25 ± 17.16	662,754-
Wavelet-CNN- $[115]$ -	51.35 ± 5.61	57.52 ± 8.02 -	59.27 ± 6.44	46,755,208-
AM-SVM-[197]-	86.3 ± 1.5	$83.8^{-}\pm 1.3^{-}$	$80.31^{-}\pm 1.3^{-}$	×
NS-SVM-[202]-	55.93 ± 3.04	50.32 ± 3.36	52.9 ± 2.08	×
Proposed-	89.7 ± 1.4	$\textbf{86.55} \pm \textbf{0.98}$	82.46 ± 1.27	2,208,861-

Table 6.2: The F1 score and the number of trainable parameters of the baseline models and the proposed method across conditions. The best-performing model is highlighted in bold.

6.3.2 Model Ablation Study

We-perform-ablation-experiments-to-determine-the-contribution-of-each-module-of-theproposed-model.- The-following-seven-ablated-variants-of-the-proposed-model-weretested-in-our-experiments.-

- A:-no-node-pooling;-
- B:-graph-learning-replaced-with-a-fully-connected-graph;-
- C:-GGCN-replaced-with-a- R^{th} -order-ChebConv-(R = 4);-
- D:-variants-A-and-B-combined;-
- E:-variants-A-and-C-combined;-
- F:-variants-B-and-C-combined;-
- G:-variants-A,-B-and-C-combined.-

The ablation results in Figure 6.2 reveal that each of the proposed modules contributes significantly to the high performance of the proposed architecture. For variant A, we can observe that the contribution of the node pooling module is significant, albeit relatively small. However, this module reduces the number of parameters of the model and helps to produce explainable predictions (Figure 6.7 and Figure 6.8). Without the node pooling, the final MLP classifier would have $N \times h_{GNN} \times h_{MLP}$ parameters (N = 23), but node pooling reduces it to $k_{pool} \times h_{GNN} \times h_{MLP}$ ($k_{pool} = 3$). For variant B, it is not surprising that its performance decreases significantly as the graph

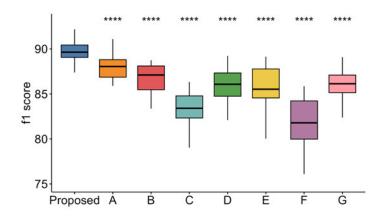


Figure 6.2: F1 scores of model variants. The asterisks report the p-value of a nonparametric Mann-Whitney U test measuring the difference between AGGCN and the ablated variants.

learning-module-is-replaced-with-a-fully-connected-graph.- Thus,-it-cannot-leveragegraph-domain-information-except-in-the-node-pooling-module.-

Next, we demonstrate that the GGCN encoder improves performance significantly compared to a ChebConv encoder according to variant C. A ChebConv layer is similar to a GGCN in its iterative nature, i.e. ChebConv iteratively updates node embeddings by approximating the eigendecomposition of graph Laplacian. However, ChebConv does not have any gating mechanism, which means that information across scales contributes to the final embedding equally. Since all of the major modules of the proposed are shown to contribute to the final performance significantly, it is unsurprising that the rest of the ablated models with more than one of these modules perform significantly worse as well (Variants D-G in Figure 6.2). Note that some of the ablated models maintain a relatively low variance of performance. We speculate this is because the ablated models can still learn robust embeddings, but some of the information within the data remains inaccessible, which would be enabled by the removed module.

The parameter sensitivity experiments also support the optimal values of crucialhyperparameters of the proposed model (Appendix C, Figs C.1, C.2, C.3 and C.4). It is worth noting that the proposed architecture allows training relatively deep models (using up to eleven GGCN iterations) with only a minor performance decrease (Fig-C.1). We can also observe that although the optimal values of these hyperparameters result in the best performance, the performance doesn't change much with adjacent values near the optima. This demonstrates that although the proposed model requires a relatively large number of hyperparameters to be determined, its performance remains robust with sub-optimal values, thus suggesting generalisability potential.

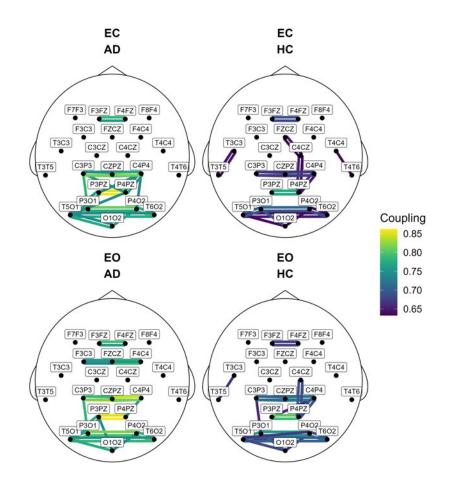


Figure 6.3: Top 30 strongest edges of the AGGCN-learned graphs of AD and HC cases in EC and EO conditions (average of all samples).

6.3.3 Explainability of AGGCN

The proposed model-generates plausible-and-consistent-explanations-for-its-predictions.-We-generate-multiple-types-of-prediction-explanations.-Specifically, these-are-derived-from-the-following:-(1)-graph-learning,-(2)-node-embedding-and-GGCN-encoder,-(3)-node-pooling,-and-(4)-feature-masking.-Except-for-type-(4),-these-explanations-could-be-obtained-for-individual-samples.-However,-we-visualise-the-diagnosis-averaged-explanations-to-explore-the-patterns-learned-by-the-proposed-model.-

Graph Learning

The graph-learning-module-learns-a-clear-difference-between-the-AD-and-HC-cases,-as-shown-in-Figure-6.3-(alternatively-Figure-C.5).-The-learned-brain-graphs-show-that-AD-

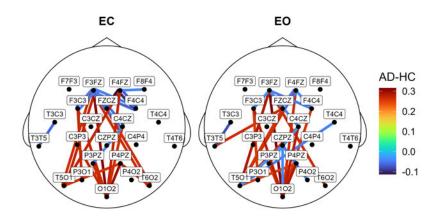


Figure 6.4: The differences between AGGCN-learned graphs for AD and HC cases in EC and EO conditions show the AD-related connectivity disruption. The average of all samples, the top 30 strongest edges were preserved. Values above zero indicate AD increase, while values below zero indicate AD decrease.

cases-have-increased-connectivity-overall,-while-HC-graphs-seem-more-sparse-with-fewdensely-connected-regions.- A-well-defined-cluster-of-densely-connected-nodes-is-presentin-both-groups-within-the-centro-parietal-and-occipital-regions-and-a-few-strong-edgesin-the-frontal- and-temporal-regions.- The-locations- of-the-strongest-edges- are- consistent-across-conditions.- Figure-6.4-then-shows-the-top-30-edges,-where-the-largestincrease/decrease-in-coupling-was-observed-in-AD.- AD-seems-to-have-increased-couplingstrength-in-long-distance-edges,-particularly-between-frontal-and-parietal/occipital-regions.- These-increases-are-quite-consistent-between-conditions.- In-contrast,-AD-caseshave-decreased-coupling-strength,-mostly-in-local-connections-in-the-frontal-(EC)-andfrontal-and-centro-parietal-(EO)-regions.-

Additionally, we statistically compared the learned graph structures to determine differences between AD and HC cases across EC and EO conditions (Figure C.6)

Node Embeddings and GGCN

Another-prediction-explanation-can-be-derived-from-the-node-embeddings-obtainedby-the-GGCN-(Fig-6.5).- In-particular, we-visualise-the-node-embeddings-obtainedafter-four-iterations-of-GGCN-and-compress-them-to-1D-representation-using-principal-component-analysis-(PCA)-and-extracting-the-first-principal-component.- PCA-isfitted-for-each-condition-separately.- The-node-embeddings-do-not-express-a-change-

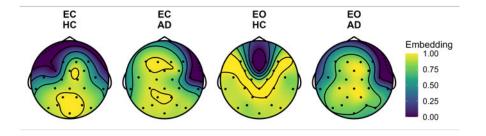


Figure 6.5: Averaged node embeddings across nodes expressed via the first component of PCA for AD and HC cases across EC and EO conditions. Note that embedding value does not suggest increased or decreased activity within a given area but rather the similarity of nodes.

in-activity-but-rather-a-node-similarity.- Generally, the node-embedding-explanationsshow-two-large-regions-of-similar-embeddings.- In-EC, these-are-frontotemporal-andcentro-parietal-regions, and right-frontotemporal-and-the-rest-of-the-regions-for-HCand-AD, respectively.- The-HC-similarity-region-in-the-EO-condition-is-reduced-fromfrontotemporal-to-only-the-frontal-region.- In-contrast, the-AD-similarity-region-expands-from-the-right-frontotemporal-region-to-the-left-side.- This-further-highlights-thedifferences-in-learned-patterns-under-the-EC-and-EO-conditions, thus-explaining-thereduced-performance-in-the-combined-EC+EO-condition.-

Next, the role of the gating mechanism is elucidated by analysing the amount of information gathered at each scale, i.e. iteration of GGCN (Figure 6.6). We measure this by computing the average Euclidean distance between the initial and updated node embedding at each iteration, i.e. $\mathbf{x}_i^{(r)}$ and $\mathbf{m}_i^{(r+1)}$ in Eq. 6.3. For instance, a small distance means a small amount of information was gathered at that scale. Local information contributes highly to the node embeddings of the AD cases, and then the degree of contributions linearly decreases with increasing graph scale. The opposite pattern is observed for HC cases, where the later iterations influence the node embeddings. This highlights the degradation of global and distributed information caused by AD since the model can efficiently learn with fewer iterations, i.e. most information is obtained from the first-three iterations.

Node Pooling Module

The node pooling mechanism can be exploited to derive two explanations. First, we analyse the frequency with which each node is included in the coarsened graph, i.e. pooling frequency (Figure 6.7). Second, cluster attention scores (i.e. a_{ij} in Eq. 6.5) can

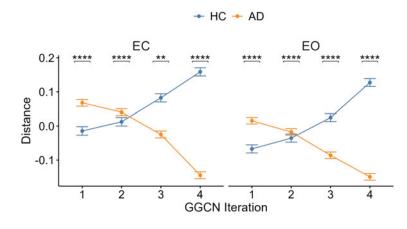


Figure 6.6: The average distance between initial node embedding and updated node embeddings shows the amount of information retained in each iteration of GGCN, i.e. going from local to global information. The asterisks denote the p-value of non-parametric Mann-Whitney U tests comparing the average distance between AD and HC cases and EC and EO conditions.

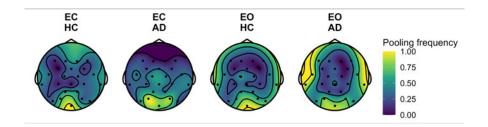


Figure 6.7: The average probability of a node being included in the coarsened graph by the ASAP node pooling module for AD and HC cases across EC and EO conditions. Averaged from all samples and min-max normalised.

be-used-to-identify-important-hubs-that-are-highly-represented-in-the-clusters-learned-by-the-node-pooling-module-(Figure-6.8).-

The nodes in parieto-occipital regions are consistently selected with high poolingfrequency-for AD and HC cases across both EC and EO conditions (Figure 6.7). Additionally, in EC condition, HC cases frequently select frontal nodes while AD cases tendto select central nodes. In contrast, in the EO condition, there seems to be more variation in the pooling frequency, with temporal nodes having a high pooling frequency for AD and HC cases.

Note- that- the- nodes- of- the- pooled- graphs- are,- in- fact,- cluster- embeddings,- i.e.attention-weighted-sum-of-node-embeddings- (Eq. 6.7).- We-visualise- the-nodes- with-

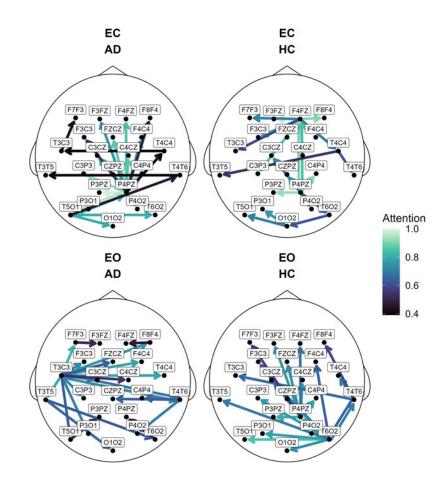


Figure 6.8: Attention scores learned by the node pooling module $(a_{ij}$ in Eq. 6.5), indicating the amount of information transferred from the source node into a cluster centred at the target node. Averaged for all AD and HC cases across EC and EO conditions (single strongest edge preserved for each target cluster node).

the highest attention scores of each cluster to highlight important hubs (Figure 6.8). The attention scores are directed edges from a source node, transferring information to the cluster centred at the target node. Alternatively, these scores can be interpreted as a cluster membership strength. This information transfer should be interpreted as information flow within the model and most likely does not reflect an information flow within the brain.

In-EC,-AD-cases-show-a-large-hub-at-the-P4PZ-node-with-strong-long-distanceand-short-distance-to-various-nodes.-Additionally,-there-is-a-smaller-hub-at-the-T5O1.-Similarly,-in-EO,-AD-cases-have-a-large-hub-at-the-T3C3-node-and-a-smaller-one-at-theT4T6-node.-In-contrast,-HC-cases-do-not-have-any-apparent-hubs-in-the-EC-condition,with-only-a-small-hub-at-the-P4PZ-node.- The-attention-links-also-seem-to-be-rathershort-distance.-In-the-EO-condition,-HC-cases-show-a-large-hub-at-the-T6O2-node-andsmaller-hubs-at-the-P4PZ-and-T4T6-nodes.-

This-variance-between-EC-and-EO-conditions-displayed-in-the-pooling-frequencyand-attention-scores-suggests-a-plausible-answer-to-why-it-is-challenging-for-the-modelto-learn-joint-representation-in-the-EC+EO-combined-condition.- We-speculate-this-iscaused-by-the-additional-dynamics-introduced-by-the-visual-processing-during-the-EOcondition.-

Feature Masking

We utilise feature masking to elucidate the importance of the frequency components summarised at each node by the node feature vector, i.e. PSD. In this, values at a selected part of the node feature vectors are replaced by zeroes and the model is retrained on this modified dataset. The relative reduction in f1 scores was then measured and visualised in Fig 6.9 for EC and EO conditions.

In-both-EC-and-EO-conditions, the frequencies between 6-and 10-Hz-are the mostimportant-since-their-masking-reduced-performance-by-4.82%-and-9.18%, respectively. This-fits-well-with-the-well-described-increase-of-power-as-well-as-functional-connectivityin-AD-within-these-frequencies-corresponding-to- θ and low- α bands-[13,-141]. Similarly, masking-of-the-[1, 5], [36, 40]-and-[41, 45]-frequency-ranges-results-in-a-significantperformance-decrease-in-both-EC-and-EO. Additionally, in-EO-condition, the-[11, 15],-[16, 20]-and-[26, 30]-frequency-ranges-produce-a-significant-performance-decrease.

6.3.4 Limitations and Future Work

Although-our-approach-achieves-competitive-performance,-we-identify-a-few-drawbacks.-First,-the-relatively-small-size-of-our-dataset-imposes-a-limit-on-fitting-complex-models.-We-address-this-issue-by-segmenting-the-EEG-signals-into-short-windows.- The-shortwindow-length-means-that-the-model-might-not-be-able-to-represent-information-fromlow-frequency-components-of-the-signal.-

Next, we do not explore alternative node feature representations beyond PSD inthis study. PSD is merely a linear frequency domain representation of the signal. Including time-domain and nonlinear information in the node features might improve the expressiveness of the model. Similarly, the proposed graph learning mechanism

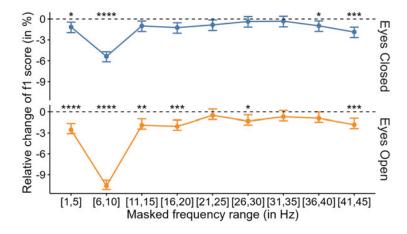


Figure 6.9: Relative change in F1 score when parts of node features are masked, showing the importance of frequency components for the classification task for eyes closed and eyes open conditions. The asterisks denote the p-value of non-parametric Mann-Whitney U tests comparing whether the relative change is significantly different from 0.

is-limited-to-linear-coupling-patterns-because-(1)-it-is-inferred-from-the-node-featuresand-(2)-it-is-expressed-as-Pearson's-correlation-coefficient.-Future-work-should-exploreother-forms-of-FC-that-might-be-integrated-into-the-graph-learning-mechanism-andstudy-ways-to-include-more-complex-frequency-dependent-coupling-information.-

Finally, the model architecture might be limited by the relatively large number of hyper-parameters that need to be optimised. However, this limitation should be mitigated by utilising a validation set during the optimisation. Moreover, we explore the model stability with respect to some of the important hyperparameters in the parameter sensitivity experiments. These suggest that the performance achieved by the proposed model is not limited purely to the optimal values of the hyperparameters.

6.4 Conclusion

This-work-proposes-a-novel-graph-learning-model-that-performs-highly-in-the-ADdiagnosis-task.- We-show-that-the-model-produces-robust-and-clinically-relevant-explanations-for-its-predictions-via-the-novel-graph-structure-learning-module-and-thenode-pooling-mechanism.- Finally,-we-highlight-the-importance-of-utilising-the-gatingmechanism-within-a-message-passing-encoder.- This-allows-the-model-to-represent-themultiscale-distributed-network-disruptions-accurately.-

6.5 Chapter Summary

This-chapter-introduces-a-novel-GNN-model-for-explainable-AD-classification.- Themodel-dynamically-reconstructs-brain-graph-structures-and-enhances-node-featuresadaptively-from-the-data.- The-resulting-brain-graphs-aid-in-interpreting-predictions.-Additionally,-we-employ-a-clustering-based-node-pooling-mechanism-to-localise-significant-brain-regions-contributing-to-predictions.-

The experimental results demonstrate the robust performance of our AGGCNmodel-across-various-conditions. Notably, the model-performs best-in-EC-condition-butretains high performance in EC condition. However, performance significantly drops in the combined (EC+EO) dataset, indicating the challenge of integrating informationfrom both conditions.

Comparison-with-seven-baseline-models-shows-the-superiority-of-AGGCN-acrossall-conditions.- Ablation-studies-further-highlight-the-importance-of-individual-modelmodules,-with-each-contributing-significantly-to-the-performance-or-explainability.-

The explainability of AGGCN is demonstrated by generating prediction explanations across multiple scales. Graph-learning reveals distinct brain connectivity patterns between AD and HC cases. Node embeddings and GGCN encoder showcase differences in learned patterns under EC and EO conditions. The node pooling mechanism identifies significant hubs in brain regions contributing to predictions. Feature masking illustrates the importance of frequency components in node feature vectors for AD classification.

While- achieving- competitive- performance, - limitations- include- dataset- size- constraints-and-potential-enhancements-in-node-feature-representations-and-graph-learningmechanisms.- Nonetheless, - the- model- demonstrates- stability- across- varying- hyperparameter-values-and-provides-clinically-relevant-explanations-for-AD-diagnosis.-

In-conclusion, the proposed AGGCN model proves effective for AD classification, offering interpretability and insights into brain connectivity patterns relevant to the disease.

Chapter 7

Conclusions

The research presented in this thesis aimed to answer the question of how to leverage graph-based representations to characterise and distinguish AD cases from age-matched HC using multivariate EEG signals. Various FC measures and data-driven methods were utilised to recover functional brain graph structures from EEG. Two approaches to extracting information from brain graphs were tested: (1) feature based ML and (2) data-driven DL representation learning.

(1)-relies-on-using-graph-theory-metrics-to-quantify-certain-aspects-of-brain-graphsand-has-been-deployed-in-Chapters-4-and-5-(partially).- (2)-uses-artificial-neural-networks-to-extract-features-useful-for-prediction-automatically-and-has-been-deployed-in-Chapters-5-and-6.-

Chapter 4 reports- the- use- of- CBS- as- a- novel- measure- of- FC- both- within- andbetween-frequency-bands-by-introducing-multilayer-graph-representations.- The-reconstructed- CBS-based-graphs- were- then- used- to- elucidate- the- role- of- frequency- bandsand-their-CFC-interactions-to-enable-information-integration-and-segregation-and-howthese-roles- are-influenced- by- AD.- This-information-is-subsequently-used-to-train-MLmodel-for-AD-classification.-

Chapter 5 then reports an empirical evaluation of commonly used FC measures for training predictive models to enable accurate AD diagnosis. GNN-based models perform significantly better than other tested architectures. Additionally, it has been demonstrated that FC information is crucial for GNN design for EEG classification. However, the choice of optimal FC measure remains ambiguous, as none of the chosen FC measures performs consistently better.

Finally, **Chapter 6** introduces a novel-GNN-based architecture for explainable diagnosis of AD. The proposed model implements a data-driven graph-learning mechanism,

thus-avoiding-the-issue-of-selecting-an-appropriate-FC-measure. Multiple-sample-specific-explanations-can-be-derived-from-the-proposed-model-across-various-spatial-levels,-i.e.-edge-level,-node-level-and-cluster-level.

7.1 Achieved Research Objectives

7.1.1 Predictive Power of Nonlinear and CFC Connectivity Compared to Linear and WFC Alternatives

Answers-to-this-objective-were-addressed-in-Chapters-4-and-5.-Specifically,-Chapter-4compares-nonlinear-FC-measure-of-CFC-and-WFC-(i.e.-CBS)-with-its-linear-alternativelimited-to-WFC-(i.e.-CS).-Second,-Chapter-5-compares-several-commonly-used-linearand-nonlinear-FC-measures-in-terms-of-predictive-performance-using-four-classificationapproaches.-

CBS-and-CS-based-graphs-were-compared-in-terms-of-detecting-statistical-differences-between-AD-and-HC-cases-and-classification-performance. As-CBS-detects-comparable-differences-as-CS-and-even-performs-significantly-better-in-the-classificationtask,-a-conclusion-can-be-drawn-that-the-inclusion-of-nonlinear-and-CFC-informationimproves-AD-characterisation-and-prediction. However,-as-CBS-is-not-directly-comparable-to-CS,-the-exact-contribution-of-nonlinear-connectivity-remains-ambiguous.

Next,-5-investigated-the-classification-performance-of-linear-and-nonlinear-FC-measures.- GNNs- trained- on- linear- and- nonlinear- FC- graphs- perform- similarly.- Thus,there-is-likely-no-advantage-gained-by-considering-nonlinear-information.- In-contrast,some-of-the-considered-nonlinear-FC-measures-such-as-MI-and-PLV-lead-to-consistentsignificant-performance-gains-when-using-SVM-and-CNN-models.-

Overall, this thesis demonstrates several advantages of considering both nonlinear and CFC connectivity in combination with linear and WFC approaches for modelling AD. However, both linear and WFC connectivities are likely dominant in AD and HC EEG signals.

7.1.2 Methods for Analysing Cross-frequency Coupling from a Graph Perspective

The answer to this objective was addressed in Chapter 4. In the literature review chapter (Chapter 2), a research gap has been identified concerning the lack of CFC-

modelling-from-a-graph-perspective. This-thesis-proposed-using-CBS-to-reconstructmultilayer-brain-graphs-that-incorporate-both-WFC-and-CFC-information.

The proposed multilayer graph framework was then used to elucidate the roles of frequency components and their CFC interactions. Both WFC and CFC roles of high-frequency components were shown to be disrupted in AD. In contrast, both WFC and CFC roles of low-frequency components seem to be generally increased in AD, thus suggesting a plausible compensatory mechanism for the loss of high-frequency coupling. In conclusion, this thesis demonstrates the utility of modelling both CFC and WFC within a graph based framework to reveal novel AD-related disruptions.

7.1.3 Graph Learning and Graph Neural Networks to Study Neurodegenerative Diseases and Facilitate Diagnosis

This-objective-was-addressed-in-Section-2.4-and-Chapters-5-and-6.-First, applications-of-GNNs-for-EEG-based-classification-were-systematically-reviewed.-The-main-identified-limitations-include-a-lack-of-experiments-with-a-broader-range-of-GCN-layers,-limited-model-explainability- and-missing-integration-of-CFC-information.- Moreover,-GNN-based-diagnosis-of-AD-remains-a-largely-unexplored-area.-

Therefore, Chapter 5-first-investigated the effect of commonly used FC-measureson-GNN-performance-for-EEG-based-classification-of-AD-using-relatively-simple-GNNarchitecture. Results reported in this chapter demonstrate a clear advantage of GNNsfor AD-classification compared to baseline models. Additionally, the use of FC-basedbrain graphs result in superior GNN-performance compared to fixed distance-based graphs, indicating the importance of considering FC-information when designing GNNarchitectures. Chapter 6-then introduces a novel GNN-architecture for the classification of AD. This model performs significantly better than previously proposed ML-and DLapproaches, thus further demonstrating the advantages of using GNNs.

7.1.4 Graph Neural Network for Automatically Reconstructing Brain Graph Structures

Multiple-FC-measures-are-commonly-used-in-the-literature-to-reconstruct-brain-graphsfrom-EEG.- However, - results- reported-in- Chapter- 5- show- ambiguous- results- regarding-choosing-the-optimal-FC-measure.- In-order-to-circumvent-this-issue, - data-drivenmethods-can-instead-be-leveraged-to-reconstruct-brain-graph-structure-from-the-data.- The systematic review of EEG-GNNs (Section 2.4, has identified various data-driven graph learning approaches incorporated within GNN, such as dot-product-based or attention-based methods.

An alternative data-driven graph learning mechanism has been investigated in Chapter-6, utilising a well-known FC measure to produce brain graph structures. The learned graph structures share multiple characteristics with traditional FC graphs and also demonstrate their expressiveness in explaining edge-level differences between AD and HC cases.

7.1.5 Graph Neural Network for Explainable Prediction of Neurodegenerative Diseases

Producing-diagnosis-explanations-is-crucial-to-enable-model-validation-by-clinical-experts.-However,-this-has-often-been-overlooked-in-previously-proposed-DL-based-models,-including-GNNs.- Chapter-6,-thus,-delves-into-designing-a-GNN-architecture-thatcan-produce-prediction-explanations-across-multiple-spatial-scales.- The-proposed-modelhas-been-demonstrated-to-produce-consistent-explanations.-

On-the-global-graph-scale,-the-model-leverages-more-information-from-local-interactions-of-AD-cases-compared-to-HC,-suggesting-the-loss-of-global-information-processingdue-to-AD.- The-model-also-identified-the-emergence-of-a-large-hub-in-the-parietal-regionin-AD-cases-that-contain-both-short- and-long-range-edges.- This-parietal-hub-mightindicate-a-compensatory-mechanism-to-counteract-the-disruption-of-global-informationprocessing.- Finally,- on- the- node-level,- the- model- shows- the- importance- of- parietaland-occipital-regions-for-AD-classification.- These-results-demonstrate-the-potential-of-GNNs-models-for-precise-explainable-prediction-from-EEG-signals.-

7.2 Research Limitations

The research presented in this thesis has a few limitations that could be addressed in future research. First, the reported experiments were all performed on the same dataset. This is mainly due to the cost of obtaining other datasets and with no open access datasets available when these experiments were carried out. The main limitation of the used dataset is its limited size, i.e. 20 AD and 20 HC cases. The small sample size was attempted to circumvent by further splitting the signals into small windows, thus allowing the training of DL models. However, using signal windowing is not applicable for-statistical-analysis-since-there-is-shared-variance-between-windows-from-the-same-participant,-thus-violating-the-independence-assumption-of-most-statistical-tests.-

Secondly, the generalisibility of the proposed methods is unclear due to the limited dataset and lack of validation on external datasets. Moreover, there is a risk of hyperparameter overfitting to the used dataset. This limitation could be addressed by utilising nested cross-validation. Due to the high computational cost of such model validation, we opted for the traditional cross-validation approach commonly used in the literature. We acknowledge the potential risk of such an approach. However, it can be argued that since the AD-related patterns reported in this thesis fit well with the findings reported in the literature, the proposed methods show a potential to generalise well to unseen data. This section outlines the limitations common to the whole thesis. Additionally, each chapter discussed limitations specific to the work presented in the given chapter.

7.3 Future Work

The research objectives set-out-in-this-thesis were largely achieved, but several-interesting questions remain to be answered by future research. The methods proposed inthis thesis were evaluated only in terms of distinguishing AD cases from HC. However, all of the methods are general and flexible enough to potentially (1) generalise to larger AD datasets, (2) be applied to the classification of other neurological diseases and disorders beyond AD and (3) to produce valuable insights about brain function and disease/disorder-related disruptions.

The issue of (1) has already been described in the previous section. Beyond the methodology-related issues brought about by the small sample size, validation on larger, more diverse datasets would be beneficial. Ideally, the dataset should sample data from various countries and ethnically diverse participants to ensure a broad generalisation of the results. (2) would be an exciting extension of the reported work. The proposed methodology does not make any assumptions about the nature of a disorder aside from the assumption of graph disruption. Thus, the methods are likely to perform well in other EEG-based classification tasks such as Parkinson's disease, frontotemporal dementia or epilepsy. Finally, (3) is based on the same assumption of the general nature of the proposed methods. Thus, the multilayer graph analysis and novel GNN model should generate comparable insights to those reported for AD cases.

Another-avenue-for-future-research-lies-in-exploring-various-pre-training-techniques-

to allow for the training of more complex and plausibly more powerful GNN models, preferably even on small datasets, i.e. datasets on less common diseases. An ideal pre-training population-independent task might be a regression task, i.e. predicting multivariate EEG signals T steps ahead. Moreover, an accurate multivariate regression GNN model could be further used to simulate additional samples, thus increasing the training set.

A-related-future-research-direction-would-be-utilising-GNNs-combined-with-unsupervised-learning-to-derive-novel-data-driven-FC-measures-or-even-causality-measures.-Separating-graph-learning-from-training-a-model-for-a-specific-classification-task-mightoffer-significant-advantages.-This-would-be-in-contrast-to-the-AGGCN-model-(Chapter-6).- By-learning-the-graph-in-isolation-(i.e.- without-optimising-the-model-for-classification),-the-obtained-edge-weights-would-be-guaranteed-to-encode-brain-similarity-orcausality-between-brain-regions.- In-contrast,-AGGCN-style-graph-learning-might-bebiased-towards-edges-helpful-in-solving-the-classification-task.-

Although, this thesis demonstrated that incorporating CFC information into reconstructed brain graphs provides novel ways of characterising AD. However, combining GNNs and CFC based graphs remains unexplored. Generally, only WFC brain graphs have been thus far utilised as input to GNN models. Two ways of leveraging CFC information in GNNs might be of interest in future research. One approach could directly utilise multilayer brain graphs similar to those proposed in Chapter 4-as an input to a GNN model. Alternatively, a single layer CFC graph, e.g. $\delta - \gamma$ graph, would serve as input-akin to how WFC graphs have been used in previously proposed approaches.

Finally, while automatically diagnosing AD is crucial, it is merely a first step to deploying automatic diagnostic models in clinical settings. Future research needs to expand the predictive modelling proposed in this thesis to both predict AD in early stages, i.e. conversion from MCI stage, and functional outcomes of the disease, i.e. symptom severity for monitoring and possibly evaluation of treatment effectiveness. Thus, this thesis is a small step in EEG based diagnosis of AD but a giant leap for this author.

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Appendices

Appendix A

Additional results from Cross-Frequency Multilayer Network Analysis with Bispectrum-based Functional Connectivity (Chapter 4)

A.1 Statistical power

We-calculate-the-statistical-power-given-our-sample-size-(N = -40)-as-a-function-of-the-effect-size-(Cohen's-d)-of-a-two-sample-t-test-with-a-two-sided-alternative-hypothesis-and-a-significant-p-value-of-0.05-(Figure-A.1).- Sufficient-power-(80%)-is-reached-with-an-effect-size- ≥ 0.45 .-

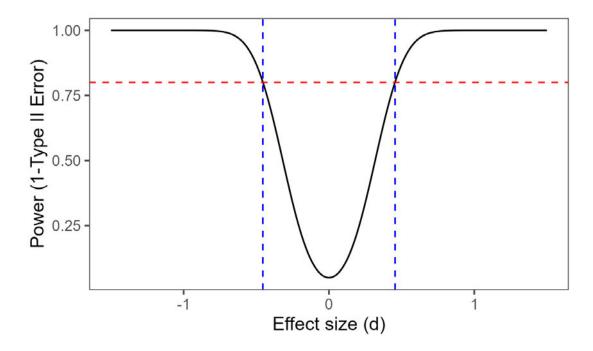


Figure A.1: Statistical power for different Cohen's d effect size values with sample size 40.

A.2 Results for epoch 1

In-this-section,-we-report-the-results-of-the-statistical-comparisons-and-corresponding-figures-using-only-data-from-the-first-epoch.-

The comparisons of average coupling computed with CS and CBS are shown in Tables A.1 and A.2, respectively. Additionally, the corresponding figures of connectivity matrices computed with CS and CBS are shown in Figures A.2 and A.3.

The comparisons of node strength computed with CS and CBS are shown in Table A.3 and Figure A.4, and Table A.4 and Figure A.5, respectively.

Results-of-comparisons-of-the-unweighted-multilayer-network-metrics-are-reportedin-Tables-A.5,-A.6-and-A.7-for-edge-betweenness,-global-vulnerability-and-local-vulnerability,-respectively.-The-corresponding-figures-are;-edge-betweenness-(Figure-A.6),global-vulnerability-(Figure-A.7)-and-local-vulnerability-(Figure-A.8).-

Results-of-comparisons-of-the-weighted-multilayer-network-metrics-are-reported-in-Tables-A.8,-A.9-and-A.10-for-edge-betweenness,-global-vulnerability-and-local-vulnerability,-respectively.- The-corresponding-figures-are;- edge-betweenness- (Figure-A.9),global-vulnerability-(Figure-A.10)-and-local-vulnerability-(Figure-A.11).-

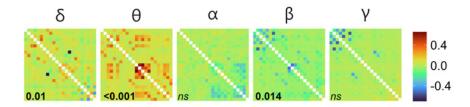


Figure A.2: Difference of average connectivity matrices (AD - HC) measured with CS in epoch 1 of (A) AD and (B) HC. For visualisation purposes, the values were min-max normalised. Digits in black denote a *p*-value testing for the difference in global coupling (p < 0.05 in bold, in italics otherwise).

Table A.1: Comparisons of the mean of adjacency matrix constructed with CS in epoch 1. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number of epochs where significant differences were observed (E), difference estimate μ with 95% confidence interval. Reliable differences (significant in all three epochs) are highlighted with bold text.

Frequency-band-	Test	Difference-estimate-(95%-CI)-
α	U=337, p=0.227, d=0.17, E=1	$\mu = -0.27 \cdot (-0.79 \cdot 0.25)$
β	t(36.97)=-2.72, p=0.014, d=-0.72, E=3	$\mu = -0.68 \cdot (-1.18 \cdot -0.18)$
δ	t(35.89)=2.99, p=0.01, d=0.78, E=3	$\mu = 0.73 \cdot (0.24 \cdot 1.22)$
γ	t(36.45) = -1.22, p = 0.227, d = -0.32, E = 0	$\mu = -0.32 (-0.84 \cdot 0.2)^{-1}$
θ	t(36.85)=5.47, p; 0.001, d=1.44, E=3	$\mu = 1.17 \cdot (0.74 \cdot 1.6)^{-1}$

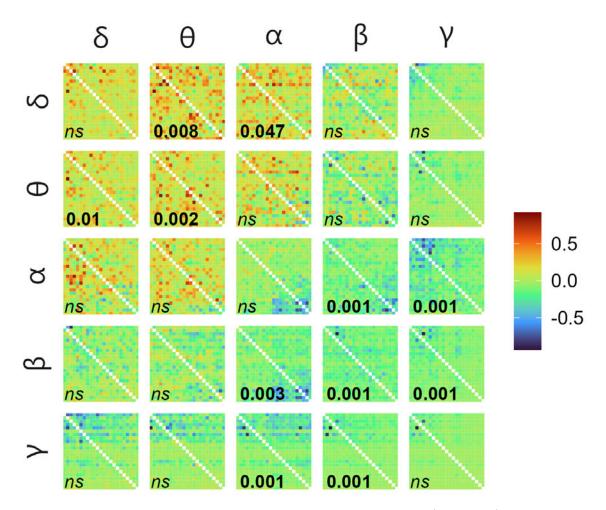


Figure A.3: Difference of average connectivity matrices (AD - HC) measured with CBS with input frequency on the vertical facets and output frequency on the horizontal. For visualisation purposes, the values were min-max normalised. Digits in black denote a *p*-value testing for the difference in global coupling (p < 0.05 in bold, in italics otherwise).

	reported as follows: statistics alternative), number of epoc confidence interval. Reliable		of freedom), p-value of the ificant differences were ob snificant in all three epochs	reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number of epochs where significant differences were observed (E), difference estimate μ with 95% confidence interval. Reliable differences (significant in all three epochs) are highlighted with bold text.	(or nonparametric imate μ with 95% d text.
	φ	h	α	ß	λ
y	t(27.35)=2.19, t=0.055, d=0.57, t=0.57, t=0.	t(27.35)=2.19, Tp=0.055, d=0.57, t(24.81)=3.13, p=0.008, d=0.81, t(27.35)=2.19, t=0.008, d=0.81, t=0.008, t=0.008, t=0.81, t=0.	t(24.35)=2.33, $p=0.047$, $d=0.61$,	t(34.64)=-0.91, p=0.368, d=-0.24,	U=332, T=0.182, d=0.18, d=0.
5	$E=2.7\mu = -0.55(0.04-1.05)$	$E=3, \ \mu = 0.75(0.27 \ 1.24)$	$E=3, \ \mu=0.58(0.08 \ 1.08)$	$E=0, \mu = -0.24(-0.76-0.29)$	$E=0, -\mu = -0.33(-0.8-0.11)$
0	t(27.46)=3, p=0.01, d=0.78,	t(33.06)=3.7, p=0.002, d=0.97,	t(24.48)=1.99, 7p=0.069, -d=0.52,	t(25.38) = -1.75, rp = 0.104, rd = -0.45,	U=275, T=0.047, d=0.3, T=0.047, T=0.3, T=0.0, T=0
ь	$E=3, \mu = 0.73(0.24 \ 1.21)$	$E=3, \ \mu=0.87(0.4 \ 1.34)$	$E=1, \tau \mu = -0.5(-0.01 - 1.01)$	$E=1, -\mu = -0.44(-0.95-0.07)$	$E=1, 7\mu = -0.5(-1.03-0.08)$
ġ	t(29.63)=1.49, p=0.161, d=0.39, t	t(28.61)=2.22, p=0.055, d=0.58, d=0.	t(36.22)=-2.16, p=0.055, d=-0.57, d=-	t(36.89) = -3.8, p = 0.001, d = -1,	t(35.38)=-3.92, $p=0.001$, $d=-1.03$,
3	$E=2, \tau \mu = -0.38(-0.13-0.9)$	$E=1, -\mu = -0.56(0.05 - 1.06)$	$E=1, \tau \mu = -0.55(-1.05 - 0.04)$	E=3, $\mu = -0.9(-1.37 - 0.42)$	E=3, $\mu = -0.91$ (-1.38 -0.45)
Q	t(32.77)=-1.79, p=0.099, d=-0.47,	t(22.34) = -1.48, 7p = 0.161, 7d = -0.38,	t(36.77)=-3.5, p=0.003, d=-0.92,	t(36.41)=-3.89, $p=0.001$, $d=-1.02$,	t(33.54)=-3.99, $p=0.001$, $d=-1.04$,
ς.	$E=0.7\mu = -0.46(-0.97-0.05)$	$E=1, -\mu = -0.38(-0.89-0.14)$	E=3, $\mu = -0.84(-1.32 - 0.36)$	E=3, $\mu = -0.91$ (-1.38 -0.44)	E=3, $\mu = -0.93$ (-1.39 -0.46)
i	U=289, p=0.058, d=0.27,	U=288, p=0.058, d=0.27,	t(36.04)=-3.87, $p=0.001$, $d=-1.01$,	t(34.55)=-3.83, p=0.001, d=-1,	U=229, fp=0.007, fd=0.39, f
2	$E=0, -\mu = -0.43(-0.97 - 0.02)$	$E=0, \tau \mu = -0.46(-1.08-0.02)$	E=3, $\mu = -0.91$ (-1.38 -0.44)	$E=3, \mu = -0.9(-1.37 - 0.43)$	$E=1, \mu = -0.73(-1.21 - 0.27)$

Table A.2: Comparisons of the mean of adjacency matrix constructed with CBS in epoch 1. The results are

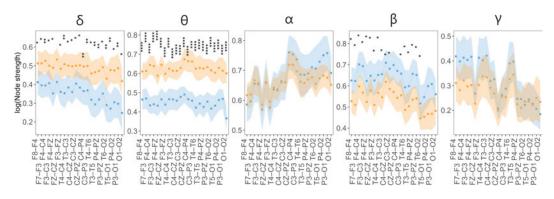


Figure A.4: Node strength (min-max normalised) measured with CS in epoch 1 of HC (blue) and AD (orange): mean with 95% confidence intervals. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "**", $p \le 0.01$ "**", and $p \le 0.05$ "*".

channel	8	θ	σ	β	~
₽8_ ₽2	t(36.66)=-2.16, p=0.038, d=-0.57,	t(35.85)=-4.45, p<0.001, d=-1.16,	t(30.27)=-0.93, $p=0.749$, $d=-0.24$,	t(36.15)=2.4, $p=0.041$, $d=0.63$,	U=543, $p=0.32$, $d=0.25$,
	$E=3, \mu = -0.55$ (-1.06 -0.04)	$E=3, \mu = -1.01 (-1.46 - 0.55)$	$E=0, \ \mu = -0.24 \ (-0.76 \ 0.28)$	E=3, $\mu = 0.6 \ (0.1 \ 1.11)$	$E=0, \mu = 0.5$ (-0.04 1.08)
67_63	t(35.61) = -2.7, p = 0.014, d = -0.71,	t(35.35)=-4.27, p<0.001, d=-1.12,	t(35.59)=-0.65, p=0.861, d=-0.17,	t(36.99)=2.9, p=0.034, d=0.76,	t(35.4)=2.33, $p=0.32$, $d=0.61$,
0.1.1.7	$E=3, \ \mu = -0.67 \ (-1.17 \ -0.17)$	E=3, $\mu = -0.98$ (-1.44 -0.52)	$E=0, \mu = -0.17$ (-0.7 0.35)	$E=3, \mu = 0.72 \ (0.22 \ 1.21)$	$E=0, \mu = 0.59$ (0.08 1.09)
F4-C4	t(37)=-3.16, $p=0.01$, $d=-0.83$,	t(36.07)=-6.72, p<0.001, d=-1.77,	t(33.41)=-0.29, p=0.969, d=-0.08,	t(36.99)=2.59, p=0.035, d=0.68,	t(35.73)=1.62, p=0.388, d=0.42,
	$E=3, \mu = -0.77 (-1.26 - 0.28)$	$E=3, \mu = -1.33 (-1.72 - 0.93)$	$E=0, \ \mu = -0.08 \ (-0.6 \ 0.45)$	$E=3, \mu = 0.65 (0.15 1.15)$	$E=0, \mu = 0.42$ (-0.1 0.93)
F3-C3	t(36.34)=-1.97, p=0.054, d=-0.51,	t(35.29)=-5.79, p<0.001, d=-1.52,	t(34.49)=-0.11, p=0.969, d=-0.03,	t(36.96)=2.82, p=0.034, d=0.74,	U=537, $p=0.32$, $d=0.24$,
50-63	$E=0, \mu = -0.5$ (-1.01 0.01)	E=3, $\mu = -1.22$ (-1.64 -0.8)	$E=0, \mu = -0.03$ (-0.56 0.5)	E=3, $\mu = 0.7 \ (0.2 \ 1.19)$	$E=0, \ \mu = 0.54 \ (-0.04 \ 1.08)$
F4-FZ	U=245, $p=0.011$, $d=0.36$,	t(36.67)=-4.42, p<0.001, d=-1.16,	U=423, $p=0.969$, $d=0.01$,	t(32.52)=2.13, p=0.049, d=0.56,	U=549, $p=0.32$, $d=0.26$,
	$E=3, \ \mu = -0.72 \ (-1.33 \ -0.22)$	$E=3, \ \mu = -1 \ (-1.46 \ -0.55)$	$E=0, \mu = 0.01 (-0.42 0.5)$	$E=3, \mu = 0.54 (0.03 1.04)$	$E=0, \mu = 0.55$ (0.01 1.12)
FZ-CZ	t(36.37)=-2.97, $p=0.01$, $d=-0.78$,	t(36.2)=-4.78, p<0.001, d=-1.25,	U=458, p=0.861, d=0.08,	t(35.7)=1.45, p=0.159, d=0.38,	U=521, $p=0.388$, $d=0.21$,
1	$E=3, \mu = -0.73 (-1.23 - 0.24)$	$E=3, \mu = -1.06 (-1.51 - 0.62)$	$E=0, \mu = 0.14$ (-0.33 0.61)	$E=0, \mu = 0.38$ (-0.14 0.89)	$E=0, \mu = 0.39$ (-0.12 0.84)
F3-FZ	t(36.5)=-2.74, p=0.014, d=-0.72, F_{1} = $\frac{1}{2}$, $\frac{1}{2}$ = $\frac{1}{2}$	t(33.84)=-4.38, p<0.001, d=-1.15, F=-3, u=-0, ag (-1.4F, -0.54)	U=416, $p=0.969$, $d=0.01$, F=0, $u = -0.03$ (-0.48.0.42)	t(35.05)=2.53, p=0.037, d=0.66, E=2, m=0.63, m=0.66, d=2, m=0.63, m=0.13, 1.13)	t(36.82)=2.05, p=0.32, d=0.54, p=0.54, p=0.52
	+ (35.2)3.150.00 (-1.11 - 0.10)	+(34.66)4.63.57(-1:40-0:03)	11-428 n-0 069 d-0 02	+(34.47)-1.84.5-0.03	$\pm (36.99) - 1.11$ ± -0.02 (0.01 ± 0.03)
T4-C4	$E=3, \mu = -0.76$ (-1.25 -0.28)	$E=3, \mu = -1.04 (-1.49 - 0.59)$	$\mathbf{E}=0, \ \mu=0.03 \ (-0.43 \ 0.48)$	$\mathbf{E}=0, \ \mu = 0.47 \ (-0.04 \ 0.98)$	$\mathbf{E}=0, \ \mu=0.29 \ (-0.23 \ 0.81)$
ەت E	t(36.64) = -2.64, $p = 0.014$, $d = -0.69$,	t(35.14)=-4.42, p<0.001, d=-1.16,	t(31.65)=-0.13, p=0.969, d=-0.03,	U=585, p=0.034, d=0.34,	t(35.93)=1.47, $p=0.42$, $d=0.39$,
T 3-C3	E=3, $\mu = -0.66$ (-1.16 -0.16)	$E=3, \ \mu = -1 \ (-1.46 \ -0.55)$	$E=0, \mu = -0.03$ (-0.56 0.49)	E=3, μ = 0.66 (0.14 1.18)	$E=0, \ \mu = 0.38 \ (-0.14 \ 0.91)$
C4-CZ	t(36.72) = -3.03, p=0.01, d= -0.8, p= -0.74 (1.24, 0.25)	t(36.89) = -4.42, p < 0.001, d = -1.16, E = 2, u = -1.01, f = 0.55)	U=459, $p=0.861$, $d=0.08$, w=0, $u=0.14$ (-0.27 , 0.65)	t(36.95)=2.19, p=0.049, d=0.57, p=0.57, p=0.57, p=0.57, p=0.51, p=0.	U=453, $p=0.818$, $d=0.07$, $T=0.12$, $L=0.22$, $d=10$
	$E=3, \mu = -0.14$ (-1.24 -0.29) +(34.34)=-2.13 $E=0.030$ d=-0.56	$E=3, \mu = -1.01 (-1.40 -0.09)$ +(35,35)=-4.63 n < 0.001 d=-1.21	$\frac{11-441}{11-441} = 0.14 (-0.37 0.09)$	$\pm (34 \ 44) = 2 \ 12 \ 5 = 0.03 \ (0.03 \ 1.00)$	$E=0, \mu = 0.12$ (-0.37 0.01) 11=507: n=0.46: d=0.18.
C3-CZ	$E=3, \mu = -0.54 (-1.04 - 0.03)$	$E=3, \mu = -1.04 (-1.49 - 0.59)$	$\mathbf{E}=0, \ \mu=0.07 \ (-0.42 \ 0.53)$	$E=3, \mu = 0.54 (0.03 \ 1.04)$	$E=0, \mu = 0.3$ (-0.15 0.76)
27_52	t(37)=-2.33, p=0.027, d=-0.61,	t(32.04)=-5.32, p<0.001, d=-1.4,	t(36.07)=1.13, p=0.749, d=0.3,	t(36.49)=2.66, p=0.034, d=0.7,	U=471, p=0.681, d=0.1,
	$E=3, \mu = -0.59 (-1.09 - 0.08)$	$E=3, \ \mu = -1.16 \ (-1.59 \ -0.72)$	$E=0, \mu = 0.29 (-0.23 0.82)$	$E=3, \mu = 0.67 (0.16 1.17)$	$E=0, \ \mu = 0.17$ (-0.29 0.66)
C4-P4	t(36.99) = -2.63, p = 0.014, d = -0.69, p = 0.014, d = -0.69, p = 0.014, d = -0.69, d = 0.014, d = -0.014, d = -	U=123, p<0.001, d=0.61, D=0.	t(35.04)=0.98, p=0.749, d=0.26, p=0.26, p=0.	t(36.88) = 2.69, $p = 0.034$, $d = 0.71$, p = 0.22, $c = 7.627$, $c = 7.137$	U=441, p=0.818, d=0.04, p=0 0.00 / 0.49 0 fe)
	(01.0-0.11-0.00) = -0.00	$D = 0, \mu = -1.03 (-1.14 -0.03)$	$\mu = 0, \mu = 0.20$ (-0.21 0.16)	(111110) = 0.01 = 0.01	$\mu = 0, \mu = 0.00$ (-0.40 0.00)
C3-P3	$t(3t) = 2.44$, p=0.022, $\alpha = -0.64$, E=3, $\mu = -0.61$ (-1.12 -0.11)	t(34.15) = -5.54, $p < 0.001$, $d = -1.49$, $E = 3$, $\mu = -1.2$ (-1.62 -0.77)	f(36.66) = 1.01, $p = 0.749$, $d = 0.27$, $E = 0, \mu = 0.26$ (-0.26 0.79)	t(30.30) = 2.12, $p = 0.049$, $d = 0.50$, $E = 3$, $\mu = 0.54$ (0.03 1.05)	$U=470$, $p=0.681$, $d=0.1$, $E=0$, $\mu = 0.2$ (-0.27 0.68)
Ē	t(32.57)=-2.68, p=0.014, d=-0.7,	t(36.14)=-5.24, p<0.001, d=-1.38,	t(32.51)=0.53, p=0.861, d=0.14,	t(35.8)=2.02, $p=0.058$, $d=0.53$,	t(36.85)=1.08, $p=0.592$, $d=0.28$,
9.T 7 .T.	E=3, $\mu = -0.66$ (-1.16 -0.17)	E=3, $\mu = -1.14$ (-1.57 -0.7)	$E=0, \mu = 0.14$ (-0.39 0.66)	$E=0, \mu = 0.51 (0.01 1.02)$	$E=0, \ \mu = 0.28 \ (-0.24 \ 0.81)$
T_{3-T_5}	U=194, $p=0.004$, $d=0.46$,		t(33.11)=0.68, p=0.861, d=0.18,	U=565, $p=0.042$, $d=0.3$,	t(35.22)=0.91, p=0.679, d=0.24,
	$E=3, \mu = -0.92 (-1.44 - 0.43)$	$E=3, \ \mu = -1.04 \ (-1.5 \ -0.59)$	$E=0, \mu = 0.18 (-0.35 0.7)$	$E=3, \mu = 0.55 (0.08 \ 1.07)$	$E=0, \mu = 0.24$ (-0.29 0.77)
P4-PZ	t(36.07) = -3.11, $p = 0.01$, $d = -0.81$, $E=3$, $\mu = -0.76$ (-1.24 -0.27)	t(36.38) = -5.44, p<0.001, d=-1.43, E=3, $\mu = -1.16$ (-1.59 -0.73)	$\mathbf{U} = 492$, $\mathbf{p} = 0.749$, $\mathbf{d} = 0.15$, $\mathbf{E} = 0, \ \mu = 0.3$ (-0.2 0.72)	$t(36.53) = 2.71$, $p = 0.034$, $a = 0.71$, $E = 3$, $\mu = 0.67$ (0.18 1.17)	$\mathbf{U} = 441$, $\mathbf{p} = 0.815$, $\mathbf{d} = 0.04$, $\mathbf{E} = 0, \ \mu = 0.07$ (-0.33 0.49)
P3_PZ	t(36.54) = -2.93, $p = 0.01$, $d = -0.77$,	t(36.17)=-5.58, p<0.001, d=-1.46,	U=490, p=0.749, d=0.14,	t(36.81)=2.48, $p=0.037$, $d=0.65$,	U=464, $p=0.72$, $d=0.09$,
1	E=3, $\mu = -0.72$ (-1.21 -0.23)	E=3, $\mu = -1.18$ (-1.61 -0.76)	$E=0, \ \mu = 0.24 \ (-0.2 \ 0.85)$	$E=3, \mu = 0.62 \ (0.12 \ 1.12)$	$E=0, \mu = 0.12 (-0.28 0.7)$
T_{6-O2}	t(32.69) = -2.68, p = 0.014, d = -0.7,	t(35.19) = -4.53, p < 0.001, d = -1.19,	U=569, $p=0.153$, $d=0.3$,	t(29.14)=1.39, p=0.172, d=0.36,	U=388, p=0.818, d=0.04,
	$E=3, \mu = -0.66 (-1.16 - 0.17)$	$E=3, \mu = -1.02 (-1.47 - 0.57)$	E=0 , $\mu = 0.47$ (0.08 0.95)	$E=0, \mu = 0.36$ (-0.16 0.87)	$E=0, \ \mu = -0.08 \ (-0.54 \ 0.45)$
T5-01	$\mathbf{E} = \mathbf{E} = \mathbf{E} = \mathbf{E} = \mathbf{E}$, $\mathbf{P} = 0.002$, $\mathbf{a} = -1.11$, $\mathbf{E} = \mathbf{E} = \mathbf{E} = -0.98$ (-1.44 -0.51)	E=3. $u = -1.06$ (-1.51 -0.61)	$\mathbf{F} = 0.45 \cdot \mathbf{F} = 0.38 (-0.14 \ 0.91)$	$\mathbf{E} = 2$, $u = 0.55$ (0.03 1.06)	$\mathbf{E} = 0, \ \mathbf{m} = 0.07 \ (-0.4 \ 0.56)$
() ()	t(34.63) = -3.1, p=0.01, d= -0.83,	t(35.97)=-4.4, p<0.001, d=-1.16,	U=570, p=0.153, d=0.35,	t(33.26)=2.32, p=0.042, d=0.61,	U=399, $p=0.918$, $d=0.01$,
F4-02	$E=3, \ \mu = -0.77 \ (-1.26 \ -0.27)$	E=3, $\mu = -1.01$ (-1.47 -0.55)	$E=0, \mu = 0.66$ (0.16 1.1)	E=3, $\mu = 0.59 \ (0.08 \ 1.1)$	$E=0, \ \mu = -0.02 \ (-0.48 \ 0.43)$
P3_01	t(35.93)=-3.59, p=0.005, d=-0.95,	t(31.25)=-3.55, p=0.001, d=-0.94,	t(29.98)=2.43, $p=0.153$, $d=0.64$,	t(35.58) = 2.74, $p=0.034$, $d=0.73$,	U=379, $p=0.818$, $d=0.06$,
•	$E=3, \mu = -0.86 (-1.35 - 0.38)$	$E=3, \mu = -0.86 (-1.35 - 0.37)$	$E=0, \mu = 0.61 (0.11 1.12)$	$E=3, \ \mu = 0.69 \ (0.18 \ 1.19)$	$E=0, \ \mu = -0.09$ (-0.65 0.28)
01 - 02	t(30.32) = -3.03, p = 0.01, d = -0.82,	U=97, $p<0.001$, $d=0.65$,	t(27.04)=1.19, p=0.749, d=0.32,	t(34.76)=1.69, p=0.106, d=0.45,	U=338, p=0.679, d=0.12,
	$E=3, \mu = -0.76 (-1.27 - 0.26)$	E=3, $\mu = -1.32$ (-1.76 -0.86)	$E=0, \mu = 0.32 (-0.22 0.85)$	$E=0, \mu = 0.44 (-0.08 \ 0.97)$	$E=0, \mu = -0.14$ (-0.71 0.27)

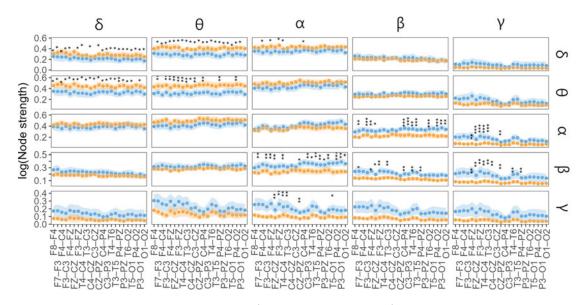


Figure A.5: Node strength (min-max normalised) measured with CBS in epoch 1 of HC (blue) and AD (orange): mean with 95% confidence intervals. The input frequency is on the vertical facets, and the output frequency is on the horizontal. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

Table A.4: Comparisons of node strength measured with CBS in epoch 1. The results are reported as follows:
statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number
of epochs where significant differences were observed (E), and difference estimate μ with 95% confidence interval
(CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	θ	α	β	λ
U=328, p=0.156, d=0.19, E=0, $\mu = -0.35$ (-0.94 0.18)	t(36.08)=-2.06, p=0.048, d=-0.54, E=3, μ =-0.52 (-1.03 -0.02)	U=293, p=0.093, d=0.26, E=0, μ =-0.52 (-0.99 0)	U=524, p=0.928, d=0.21, E=0, $\mu = 0.3$ (-0.09 0.79)	U=612, p=0.056, d=0.39, E=0, $\mu = 0.45$ (0.14 0.84)
U=286, p=0.043, d=0.27, E=3, μ =-0.66 (-1.08 -0.03)	t(27.65)=-2.62, p=0.015, d=-0.68, E=3, μ =-0.64 (-1.14 -0.15)	U=285, p=0.078, d=0.28, E=0, μ =-0.48 (-0.9 -0.04)	U=453, p=0.928, d=0.07, E=0, $\mu = 0.08$ (-0.25 0.58)	U=533, p=0.342, d=0.23, E=0, μ =0.17 (-0.02 0.42)
U=246, p=0.029, d=0.36, E=3, $u = -0.75$ (-1.14 -0.22)	t(31.71)=-3.04, $p=0.011$, $d=-0.79$, $F=3. u =-0.74$ (-1.22 -0.25)	t(34.36)=-2.98, $p=0.036$, $d=-0.78$, $F=3$. $u=-0.73$ (-1.22 -0.24)	U=463, $p=0.928$, $d=0.09$, $E=0$, $\mu=0.19$ (-0.34 0.72)	U=518, p=0.342, d=0.2, E=0, $\mu = 0.07$ (-0.03 0.24)
t(34.07)=-1.76, p=0.088, d=-	t(33.09)=-3.02, p=0.011, d=-0.79,	t(27.54)=-1.67, p=0.138, d=-	U=439, $p=0.928$, $d=0.04$, $E=0$,	U=568, $p=0.175$, $d=0.3$, $E=0$,
0.46, E=0, μ =-0.45 (-0.96 0.06)	E=3, $\mu =$ -0.74 (-1.22 -0.25)	0.43, E=0, μ =-0.42 (-0.94 0.09)	$\mu=$ 0.06 (-0.31 0.44)	$\mu=$ 0.14 (0.02 0.34)
U=293, $p=0.053$, $d=0.26$, $E=0$,	t(36.93)=-2.74, $p=0.014$, $d=-0.72$,	t(35.8)=-2.47, p=0.064, d=-	U=460, $p=0.928$, $d=0.08$, $E=0$,	U=519, $p=0.342$, $d=0.2$, $E=0$,
μ =-0.42 (-0.89 0)	E=3, μ =-0.68 (-1.18 -0.18)	0.65, E=0, μ =-0.62 (-1.12 - 0.12) 0.12)	$\mu=$ 0.1 (-0.28 0.52)	$\mu=$ 0.1 (-0.03 0.3)
t(36.27)=-2.4, $p=0.039$, $d=-0.63$,	t(35.68) = -3.05, p = 0.011, d = -0.8,	t(29.45)=-2.24, p=0.078, d=-	t(34.99)=0.98, p=0.928,	U=520, $p=0.342$, $d=0.2$, $E=0$,
E=3, μ =-0.6 (-1.11 -0.1)	E=3, μ =-0.74 (-1.23 -0.25)	0.58, E=0, μ =-0.56 (-1.06 -	d=0.26, E=0, μ =0.25 (-0.27	μ =0.08 (-0.02 0.24)
		0.06)	0.78)	
U=286, $p=0.043$, $d=0.27$, $E=3$,	t(36.29)=-2.62, p=0.015, d=-0.69,	t(34.63) = -2.77, $p = 0.036$, $d = -0.72$,	U=402, $p=0.928$, $d=0.04$, $E=0$,	U=517, $p=0.342$, $d=0.2$, $E=0$,
$\mu = -0.54 \ (-1 \ -0.05)$	E=3, μ =-0.65 (-1.15 -0.15)	E=3, μ =-0.68 (-1.18 -0.19)	μ =-0.06 (-0.54 0.45)	μ =0.11 (-0.03 0.24)
${\rm U}{=}258, {\rm p}{=}0.037, {\rm d}{=}0.33, {\rm E}{=}3,$	U=225, p=0.01, d=0.4, E=3, μ =-	U=286, $p=0.078$, $d=0.27$, $E=0$,	U=512, $p=0.928$, $d=0.19$, $E=0$,	U=509, $p=0.366$, $d=0.18$, $E=0$,
$\mu = -0.65 \ (-1.02 \ -0.19)$	0.83 (-1.25 -0.34)	μ =-0.49 (-0.92 -0.03)	μ =0.32 (-0.12 0.79)	μ =0.08 (-0.04 0.23)
U=274, p=0.039, d=0.3, E=3, μ =-	t(25.36)=-2.9, $p=0.012$, $d=-0.75$,	t(28.32)=-1.8, p=0.121, d=-	U=405, $p=0.928$, $d=0.03$, $E=0$,	U=540, $p=0.342$, $d=0.25$, $E=0$,
0.61 (-1.12 -0.08)	E=3, μ =-0.7 (-1.19 -0.22)	0.47, E=0, μ =-0.46 (-0.97 0.05)	μ =-0.04 (-0.53 0.51)	μ =0.13 (0 0.3)
U=280, $p=0.043$, $d=0.29$, $E=3$,	U=226, p=0.01, d=0.4, E=3, μ =-	t(31.13)=-3.03, $p=0.036$, $d=-0.79$,	U=443, $p=0.928$, $d=0.05$, $E=0$,	U=496, $p=0.464$, $d=0.16$, $E=0$,
μ =-0.6 (-1.16 -0.05)	0.97 (-1.44 -0.38)	E=3, μ =-0.74 (-1.22 -0.25)	$\mu=$ 0.06 (-0.51 0.67)	μ =0.1 (-0.04 0.3)
${\rm U}{=}285, {\rm p}{=}0.043, {\rm d}{=}0.28, {\rm E}{=}3,$	t(22.59)=-1.96, p=0.056, d=-	t(21.97)=-1.71, p=0.135, d=-	t(36.7)=0.44, $p=0.928$, $d=0.11$,	U=566, $p=0.175$, $d=0.3$, $E=0$,
$\mu = -0.46 \ (-0.85 \ -0.03)$	0.51, E=0, μ =-0.49 (-1 0.01)	0.45, E=0, μ =-0.43 (-0.94 0.08)	$E=0, \ \mu=0.11$ (-0.41 0.64)	$\mu=$ 0.15 (0.01 0.31)
U=250, $p=0.029$, $d=0.35$, $E=3$,	t(35.46)=-2.93, p=0.011, d=-0.77,	t(36.62)=-2.79, $p=0.036$, $d=-0.73$,	U=459, $p=0.928$, $d=0.08$, $E=0$,	U=465, $p=0.6666$, $d=0.09$, $E=0$,
$\mu = -0.59 \ (-1.07 \ -0.18)$	E=3, μ =-0.72 (-1.21 -0.23)	E=3, μ =-0.69 (-1.19 -0.19)	$\mu=$ 0.15 (-0.32 0.86)	μ =0.02 (-0.04 0.13)
U=273, p=0.039, d=0.3, E=3, μ =-	t(33.98)=-2.24, p=0.034, d=-0.58,	t(36.23)=-1.48, p=0.173, d=-	U=493, $p=0.928$, $d=0.15$, $E=0$,	U=465, $p=0.666$, $d=0.09$, $E=0$,
0.51 (-0.91 - 0.1)	E=3, μ =-0.56 (-1.07 -0.06)	0.39, E=0, μ =-0.38 (-0.9 0.13)	$\mu=$ 0.32 (-0.23 0.97)	$\mu = 0.04$ (-0.1 0.27)
U=244, $p=0.029$, $d=0.36$, $E=3$,	t(34.36)=-2.27, p=0.033, d=-0.59,	t(30.48)=-1.44, p=0.179, d=-	U=468, $p=0.928$, $d=0.1$, $E=0$,	U=451, $p=0.734$, $d=0.06$, $E=0$,
$\mu =$ -0.61 (-1.03 -0.2)	E=3, μ =-0.57 (-1.07 -0.07)	0.38, E=0, μ =-0.37 (-0.89 0.15)	μ =0.17 (-0.31 0.82)	$\mu = 0.03$ (-0.09 0.24)
U=270, $p=0.039$, $d=0.31$, $E=3$,	U=249, $p=0.013$, $d=0.35$, $E=3$,	t(31.24)=-1, p=0.324, d=-0.26,	U=450, $p=0.928$, $d=0.06$, $E=0$,	U=476, $p=0.642$, $d=0.11$, $E=0$,
μ =-0.47 (-0.86 -0.08)	μ =-0.62 (-1.08 -0.17)	\mathbf{E} =0, μ =-0.26 (-0.78 0.26)	$\mu=$ 0.11 (-0.24 0.6)	μ =0.06 (-0.07 0.2)
U=245, $p=0.029$, $d=0.36$, $E=3$,	t(34.26)=-2.84, $p=0.012$, $d=-0.74$,	t(32.62)=-1.82, $p=0.121$, $d=-$	U=464, $p=0.928$, $d=0.09$, $E=0$,	U=487, $p=0.536$, $d=0.14$, $E=0$,
$\mu = -0.71 \ (-1.12 \ -0.25)$	E=3, $\mu = -0.7$ (-1.19 -0.2)	$0.48, E=0, \mu = -0.46 (-0.98 \ 0.05)$	$\mu = 0.13$ (-0.25 0.59)	u = 0.06 (-0.05 0.2)

8	P4-PZ		U=206, p=0.01, d=0.44, E=3, $\mu = -$	08)=-2.35, p=0.074, d=	U=482, p=0.928, d=0.13, E=0,	U=469, p=0.666, d=0.1, E=0,
		$\mu = -0.79 (-1.14 - 0.26)$	1.02 (-1.53 -0.43)	0.61, $E=0$, $\mu =-0.59$ (-1.09 - 0.09)	$\mu = 0.28$ (-0.26 0.86)	$\mu = 0.03 \ (-0.04 \ 0.13)$
8	P3-PZ	Z U=275, p=0.039, d=0.3, E=3, $\mu = -$	t(36.39)=-3.37, p=0.01, d=-0.88,	t(33.6)=-2.14, p=0.078, d=-	U=422, $p=0.982$, $d=0$, $E=0$,	U=508, $p=0.366$, $d=0.18$, $E=0$,
		0.46 (-0.92 -0.06)	E=3, μ =-0.81 (-1.29 -0.33)	0.56, E=0, μ =-0.54 (-1.05 -	$\mu=$ 0.01 (-0.46 0.56)	μ =0.06 (-0.02 0.14)
				0.03)		
δ	T_{6-O2}		t(30.46)=-1.98, p=0.055, d=-	U=339, $p=0.222$, $d=0.17$, $E=0$,	U=435, $p=0.928$, $d=0.03$, $E=0$,	U=458, $p=0.718$, $d=0.08$, $E=0$,
		$\mu = -0.41 \ (-0.87 \ -0.03)$	0.52, E=0, μ =-0.5 (-1.01 0.01)	μ =-0.34 (-0.79 0.21)	$\mu=0.03$ (-0.33 0.34)	μ =0.02 (-0.07 0.13)
δ	T5-01	U=263, p=0.039, d=0.32, E=3,	t(34.26)=-2.71, p=0.014, d=-0.71,	t(27.33)=-1.53, $p=0.169$, $d=-$	U=424, $p=0.982$, $d=0.01$, $E=0$,	U=451, $p=0.734$, $d=0.06$, $E=0$,
		μ =-0.62 (-0.98 -0.17)	E=3, μ =-0.67 (-1.16 -0.17)	0.4, E=0, μ =-0.39 (-0.9 0.12)	$\mu=$ 0.02 (-0.39 0.54)	μ =0.02 (-0.07 0.19)
δ	$P_{4-O_{2}}$		t(30.49)=-2.66, p=0.015, d=-0.69,	t(26.21)=-1.97, p=0.097, d=-	U=382, $p=0.928$, $d=0.08$, $E=0$,	U=445, $p=0.737$, $d=0.05$, $E=0$,
		μ =-0.55 (-1.02 -0.12)	E=3, μ =-0.65 (-1.15 -0.16)	0.51, E=0, μ =-0.5 (-1 0.01)	μ =-0.13 (-0.55 0.27)	μ =0.01 (-0.06 0.1)
δ	P3-01		t(30.66)=-3, p=0.011, d=-0.78,	t(29.79)=-1.41, $p=0.18$, $d=-$	U=433, $p=0.928$, $d=0.03$, $E=0$,	U=445, $p=0.737$, $d=0.05$, $E=0$,
		μ =-0.48 (-1.07 -0.04)	E=3, μ =-0.73 (-1.22 -0.24)	0.37, E=0, μ =-0.36 (-0.88 0.15)	$\mu=$ 0.03 (-0.47 0.48)	μ =0.01 (-0.06 0.13)
8	O1-O2	2 U=226, p=0.029, d=0.4, E=3, $\mu = -$	U=216, p=0.01, d=0.42, E=3, $\mu=-$	t(30.41)=-2.82, $p=0.036$, $d=-0.74$,	U=373, $p=0.928$, $d=0.1$, $E=0$,	U=400, $p=0.763$, $d=0.04$, $E=0$,
		0.53 (-0.86 -0.21)	0.84 (-1.27 -0.42)	E=3, μ =-0.69 (-1.18 -0.2)	μ =-0.14 (-0.52 0.36)	μ =-0.01 (-0.09 0.07)
θ	F8-F4	t(35.97)=-2.35, $p=0.027$, $d=-0.62$,	t(36.95)=-2.9, p=0.007, d=-0.76,	t(36.02)=-1.94, p=0.148, d=-	U=517, $p=0.342$, $d=0.2$, $E=0$,	U=593, $p=0.065$, $d=0.35$, $E=0$,
		E=3, $\mu =$ -0.59 (-1.09 -0.09)	E=3, μ =-0.72 (-1.21 -0.22)	0.51, E=0, μ =-0.49 (-1 0.02)	$\mu=$ 0.37 (-0.11 0.89)	$\mu=$ 0.59 (0.2 1.03)
θ	F7-F3	t = t(30.41) = -2.59, p = 0.022, d = -0.67, t = 0.022, t = -0.67, t = 0.022, t = -0.022, t = 0.022, t = -0.022,	t(36.91)=-2.47, p=0.017, d=-0.65,	t(34.39)=-0.91, $p=0.403$, $d=-$	U=488, $p=0.4$, $d=0.14$, $E=0$,	U=514, $p=0.26$, $d=0.19$, $E=0$,
		E=3, μ =-0.64 (-1.14 -0.14)	E=3, μ =-0.62 (-1.12 -0.12)	0.24, E=0, μ =-0.24 (-0.76 0.29)	$\mu=$ 0.19 (-0.17 0.65)	μ =0.19 (-0.08 0.55)
θ	F4-C4	t $t(34.05)=-2.77$, $p=0.019$, $d=-0.72$,	t(36.27)=-3.85, p=0.003, d=-1.01,	t(33.75)=-2.46, p=0.09, d=-	U=489, $p=0.4$, $d=0.14$, $E=0$,	U=556, $p=0.103$, $d=0.28$, $E=0$,
		E=3, μ =-0.68 (-1.18 -0.19)	E=3, μ =-0.9 (-1.37 -0.43)	0.64, E=0, μ =-0.61 (-1.11 -	$\mu=$ 0.27 (-0.24 0.78)	$\mu = 0.31 (0.02 0.71)$
				0.11)		
θ	F3-C3		t(36.15)=-2.9, p=0.007, d=-0.76,	t(30.01)=-1.82, p=0.154, d=-	U=479, $p=0.442$, $d=0.12$, $E=0$,	
		E=3, $\mu = -0.56$ (-1.07 -0.06)	E=3, μ =-0.71 (-1.21 -0.22)	0.47, E=0, μ =-0.46 (-0.97 0.05)	μ =0.18 (-0.18 0.47)	$\mu=0.33~(0.09~0.65)$
θ	F_{4-FZ}		t(36.77)=-2.83, $p=0.008$, $d=-0.74$,	t(33.06)=-2.07, p=0.13, d=-	U=540, $p=0.276$, $d=0.25$, $E=0$,	U=588, $p=0.065$, $d=0.34$, $E=0$,
		$\mu = -0.67 (-1.18 - 0.09)$	E=3, μ =-0.7 (-1.2 -0.21)	0.54, E=0, μ =-0.52 (-1.03 -	$\mu=$ 0.4 (-0.02 0.82)	$\mu=$ 0.37 (0.08 0.73)
				0.02)		
θ	FZ-CZ	$z \mid t(35.78) = -3.12, p = 0.018, d = -0.82, $	t(36.93)=-3.8, p=0.003, d=-1,	t(28.02)=-1.79, p=0.154, d=-	t(28.13)=0.68, p=0.524,	U=535, $p=0.156$, $d=0.23$, $E=0$,
		E=3, μ =-0.76 (-1.25 -0.27)	E=2, μ =-0.9 (-1.37 -0.42)	0.47, E=0, μ =-0.45 (-0.96 0.06)	d=0.18, E=0, μ =0.18 (-0.35 0.7)	μ =0.17 (-0.01 0.39)
θ	F3-FZ	t $t(34.28)=-2.67$, $p=0.019$, $d=-0.7$,	t(35.71) = -3.11, p = 0.006, d = -0.81,	t(31.92)=-2.34, $p=0.09$, $d=-$	U=485, $p=0.406$, $d=0.13$, $E=0$,	U=573, $p=0.092$, $d=0.31$, $E=0$,
		E=3, μ =-0.66 (-1.16 -0.17)	E=3, μ =-0.76 (-1.24 -0.27)	0.61, E=0, μ =-0.58 (-1.09 -	$\mu=$ 0.24 (-0.27 0.68)	$\mu=$ 0.32 (0.07 0.63)
				0.08)		
θ	T4-C4	t $t(25.95)=-2.76$, $p=0.019$, $d=-0.72$,	t(36.93)=-2.33, p=0.024, d=-	t(29.78)=-1.04, p=0.368, d=-	U=585, $p=0.224$, $d=0.34$, $E=0$,	U=555, $p=0.103$, $d=0.28$, $E=0$,
		E=3, μ =-0.67 (-1.17 -0.18)	0.61, E=2, μ =-0.59 (-1.09 -	0.27, E=0, μ =-0.27 (-0.79 0.25)	$\mu=$ 0.58 (0.13 1.16)	$\mu=$ 0.29 (0.02 0.62)
		_				
θ	T3-C3		6)=-3.3,	t(34.11)=-1.67, p=0.177, d=-	U=428, $p=0.908$, $d=0.02$, $E=0$,	U=564, $p=0.095$, $d=0.29$, $E=0$,
		E=3, μ =-0.75 (-1.24 -0.27)	0.86, E=2, μ =-0.79 (-1.28 -	$0.44, \ \mathrm{E=0}, \ \mu = -0.43 \ (-0.94 \ 0.08)$	$\mu=$ 0.03 (-0.43 0.55)	$\mu = 0.35 (0.05 0.64)$
			0.31)			

θ	C4-CZ	t(35.54) = -2.94 $n = 0.019$ $d = -0.77$	t(34.62)=-3.41. n=0.005. d=-	t(28.26)=-2.5. $n=0.09$. $d=-$	U = 506, $n = 0.364$, $d = 0.18$, $E = 0$.	U = 539, $n = 0.149$, $d = 0.24$, $E = 0$.
		$E=3, \mu =-0.72$ (-1.21 -0.23)	ģ	μ =-0.62 (-	$\mu = 0.33$ (-0.19 0.83)	$\mu=0.18~(-0.02~0.41)$
				-0.12)		
θ	C3-CZ	t(23.6)=-2.49, p=0.024, d=-0.65,	t(33.44)=-2.97, p=0.007, d=-	t(22.5)=-2.39, p=0.09, d=-	t(33.59)=0.86, p=0.454,	U=569, $p=0.092$, $d=0.3$, $E=0$,
		E=3, μ =-0.62 (-1.11 -0.12)	0.78, E=2, μ =-0.73 (-1.21 -	0.62, E=0, μ =-0.59 (-1.09	d=0.22, E=0, μ =0.22 (-0.3	$\mu=$ 0.3 (0.04 0.59)
			0.24)	-0.09)	0.75)	
θ	CZ-PZ	t(37)=-2.82, $p=0.019$, $d=-0.74$,	t(36.79)=-3.37, p=0.005, d=-0.89,	t(35.33)=-2.36, p=0.09, d=-	t(34.44)=1.7, p=0.31, d=0.44,	U=496, $p=0.327$, $d=0.16$, $E=0$,
		E=3, μ =-0.7 (-1.19 -0.2)	E=3, μ =-0.81 (-1.3 -0.33)	0.62, E=0, μ =-0.59 (-1.09 -	$E{=}0,\ \mu={0.44}$ (-0.08 0.95)	μ =0.14 (-0.11 0.42)
				0.09)		
θ	C4-P4	t(36.99)=-2.31, p=0.028, d=-0.61,	t(36.11)=-3.02, $p=0.007$, $d=-0.79$,	t(34.42)=-1.21, p=0.294, d=-	U=536, $p=0.276$, $d=0.24$, $E=0$,	U=464, $p=0.511$, $d=0.09$, $E=0$,
		E=3, μ =-0.58 (-1.09 -0.08)	E=3, μ =-0.74 (-1.24 -0.25)	0.32, E=0, μ =-0.31 (-0.83 0.21)	$\mu=$ 0.41 (-0.06 0.94)	μ =0.11 (-0.21 0.45)
θ	C3-P3	t(36.15)=-2.71, p=0.019, d=-0.71,	t(36.81)=-2.96, $p=0.007$, $d=-0.78$,	t(36.38)=-1.24, $p=0.294$, $d=-$	t(27.93)=1.9, p=0.276, d=0.49,	U=500, $p=0.313$, $d=0.16$, $E=0$,
		E=3, μ =-0.67 (-1.17 -0.17)	E=3, μ =-0.73 (-1.22 -0.24)	0.33, E=0, μ =-0.32 (-0.84 0.2)	$E=0, \ \mu=0.48$ (-0.03 0.99)	μ =0.2 (-0.1 0.6)
θ	T4-T6	t(29.21)=-1.6, p=0.115, d=-	t(36.75)=-3.25, $p=0.005$, $d=-0.85$,	t(29.92)=-1.48, $p=0.224$, $d=-$	U=524, $p=0.31$, $d=0.21$, $E=0$,	U=509, $p=0.279$, $d=0.18$, $E=0$,
		0.42, E=0, μ =-0.41 (-0.92 0.1)	E=3, μ =-0.79 (-1.27 -0.3)	0.39, E=0, μ =-0.38 (-0.89 0.14)	$\mu=0.38$ (-0.11 1.05)	$\mu=$ 0.2 (-0.06 0.53)
θ	T3-T5	t(34.61)=-2.39, p=0.027, d=-0.63,	t(36.98)=-2.66, p=0.012, d=-	t(35.41)=-0.94, p=0.403, d=-	U=493, $p=0.4$, $d=0.15$, $E=0$,	U=518, $p=0.249$, $d=0.2$, $E=0$,
		E=3, μ =-0.6 (-1.1 -0.1)	0.7, E=2, μ =-0.66 (-1.16 -0.16)	0.25, E=0, μ =-0.25 (-0.77 0.28)	$\mu=$ 0.34 (-0.18 0.87)	μ =0.18 (-0.07 0.5)
θ	P4-PZ	t(36.29)=-3.83, p=0.008, d=-1,	t(36.56) = -4.44, $p = 0.001$, $d = -1.16$,	t(28.93)=-2.56, p=0.09, d=-	t(32.45)=1.08, p=0.4, d=0.28,	U=484, $p=0.417$, $d=0.13$, $E=0$,
		E=3, $\mu =$ -0.9 (-1.37 -0.43)	E=3, μ =-1.01 (-1.46 -0.55)	0.67, E=0, μ =-0.63 (-1.13 -	$\mathbf{E}{=}0,\ \mu={0.28}\ ({-}0.24\ 0.8)$	μ =0.08 (-0.08 0.32)
				0.14)		
θ	P3-PZ	t(36.71)=-2.89, $p=0.019$, $d=-0.76$,	t(33.34)=-3.28, p=0.005, d=-	t(30.05)=-1.52, p=0.222, d=-	U=505, $p=0.364$, $d=0.17$, $E=0$,	U=539, $p=0.149$, $d=0.24$, $E=0$,
		E=3, $\mu =$ -0.71 (-1.2 -0.22)	0.86, E=2, μ =-0.79 (-1.27 -	0.4, E=0, μ =-0.39 (-0.9 0.12)	$\mu=0.34$ (-0.21 0.79)	$\mu = 0.21$ (-0.02 0.46)
			0.31)			
θ	T6-O2	t(32.28)=-1.67, p=0.107, d=-	t(35.67)=-2.63, p=0.012, d=-	t(24.55)=-1.81, p=0.154, d=-	U=464, $p=0.524$, $d=0.09$, $E=0$,	U=478, $p=0.453$, $d=0.12$, $E=0$,
		0.43, E=0, μ =-0.43 (-0.94 0.09)	0.69, E=2, μ =-0.65 (-1.15 -	0.47, E=0, μ =-0.46 (-0.97 0.05)	$\mu=$ 0.17 (-0.29 0.56)	μ =0.09 (-0.12 0.41)
			(61.0			
θ	T5-01	t(33.94)=-2.48, $p=0.024$, $d=-0.65$,).87, p=0.409,	t(31.1)=1.99, $p=0.276$, $d=0.52$,	U=501, $p=0.313$, $d=0.17$, $E=0$,
		E=3, μ =-0.62 (-1.12 -0.12)	$E=2, \mu =-0.67 (-1.17 -0.17)$	0.23, E=0, μ =-0.22 (-0.75 0.3)	$E=0, \ \mu=0.5 \ (0 \ 1.01)$	μ =0.13 (-0.07 0.51)
θ	P4-O2	t(31.92)=-2.67, p=0.019, d=-0.7,	t(32.72)=-3.16, p=0.006, d=-	t(29.64)=-1.38, p=0.252, d=-	U=489, $p=0.4$, $d=0.14$, $E=0$,	U=468, $p=0.511$, $d=0.1$, $E=0$,
		E=3, μ =-0.66 (-1.15 -0.16)	0.82, E=2, μ =-0.76 (-1.25 -	0.36, E=0, μ =-0.35 (-0.87 0.16)	$\mu=$ 0.24 (-0.19 0.74)	μ =0.06 (-0.11 0.33)
¢	10 of				11-FEE	11-4690 511 40 00 E0
5	10-01		, p-0.001, 0.73 (-1.	(33.1)0.01, P-0.303, u		0—±03, p=0.311, u=0.03, ⊑=0, =0.07 (-0.11.0.11)
θ	01-02	U=222, p=0.018, d=0.4, E=3, $\mu = -$	t(36.47)=-3.58, $p=0.004$, $d=-0.94$,	t(24.68)=-2.06, p=0.13, d=-	U=508, $p=0.364$, $d=0.18$, $E=0$,	U=377, $p=0.511$, $d=0.09$, $E=0$,
		0.67 (-1.01 -0.34)	E=3, μ =-0.85 (-1.33 -0.38)	0.54, E=0, μ =-0.52 (-1.02 -	$\mu=$ 0.26 (-0.09 0.74)	μ =-0.05 (-0.28 0.18)
				0.01)		
σ	F8-F4	t(36.24)=-0.71, p=0.581, d=-	t(37)=-1.84, p=0.113, d=-0.48,	U=440, $p=0.763$, $d=0.04$, $E=0$,	U=611, $p=0.003$, $d=0.39$, $E=2$,	U=657, $p=0.001$, $d=0.48$, $E=2$,
		0.19, E=0, μ =-0.19 (-0.71 0.34)	$E=0, \mu = -0.47$ (-0.99 0.04)	μ =0.06 (-0.34 0.49)	$\mu=$ 0.65 (0.25 1.06)	μ =0.61 (0.27 0.92)
σ	F7-F3	U=292, p=0.244, d=0.26, E=0, 0 53 (_0 94 _0 01)	U=281, p=0.087, d=0.28, E=0, 0.57 (_1.02_0.07)	U=470, p=0.567, d=0.1, E=0, 0.13 (-0.27.0.54)	U=642, $p=0.001$, $d=0.45$, $E=2$, $\mu=0.78$ (0.37 1.07)	U=608, $p=0.004$, $d=0.38$, $E=2$, $\mu = 0.42$ (0.11.0.77)
		(10:0- 10:0-) 00:0 1				

	F4-C4	t(35.66)=-2.52, p=0.244, d=- 0.66, E=0, μ =-0.63 (-1.13 - 0.13)		t((35.35)=1.01, p=0.483, d=0.27, E=0, μ =0.26 (-0.26 0.79)	, p=0.001, d=0.43, (0.39 1.27)	d=0.5,
F3-C3	~	$t(29.47)=-0.98$, $p=0.452$, $d=-0.25$, $E=0$, $\mu =-0.25$ (-0.77 0.27)	t(31.94)=-2.27, p=0.087, d=- 0.59, E=0, μ =-0.57 (-1.07 - 0.07)	U=451, p=0.667, d=0.06, E=0, μ =0.11 (-0.4 0.57)	U=579, p=0.014, d=0.32, E=3, μ =0.52 (0.11 0.91)	U=669, p=0.001, d=0.51, E=3, μ =0.61 (0.29 0.93)
F4-FZ	й	t(35.99)=-1.18, p=0.371, d=- 0.31, E=0, μ =-0.31 (-0.83 0.21)	t (35.99)=-1.7, p=0.12, d=- 0.45, E=0, μ =-0.44 (-0.95 0.08)	t(31.17)=0.64, p=0.637, d=0.17, E=0, μ =0.17 (-0.36 0.69)	t(33.22)=3.7, p=0.001, d=0.97, E=1, μ =0.87 (0.4 1.34)	U=659, p=0.001, d=0.49, E=3, $\mu = 0.52 (0.23 0.89)$
FZ-CZ F3-FZ	Z Z	t(35.03)=-1.82, p=0.244, d=- 0.48, E=0, μ =-0.46 (-0.98 0.05) t(34.01)=-1.47, p=0.343, d=- 0.38, E=0, μ =-0.38 (-0.89 0.14)	t (32.72)=-2.56, p=0.087, d=- 0.67, E=0, μ =-0.64 (-1.13 - 0.14) t (33.83)=-1.83, p=0.113, d=- 0.48, E=0, μ =-0.47 (-0.98 0.04)	t(36.87)=0.96, p=0.494, d=0.25, E=0, μ =0.25 (-0.27 0.77) t(32.46)=0.77, p=0.567, d=0.2, E=0, μ =0.2 (-0.32 0.72)	t (38.94)=2.47, p=0.017, d=0.65, E=2, μ =0.62 (0.12 1.12) U=647, p=0.001, d=0.46, E=2, μ =0.81 (0.4 1.19)	$\begin{array}{llllllllllllllllllllllllllllllllllll$
T4-C4	C4	t(25.09)=-0.54, p=0.651, d=- 0.14, E=0, μ =-0.14 (-0.66 0.38)	$t(34.35)=-1.34$, $p=0.195$, $d=-0.35$, $E=0, \mu=-0.35$ (-0.86 0.17)	t(32.7)=2.13, $p=0.144$, $d=0.56$, E=0, $\mu = 0.54$ (0.03 1.04)		U=618, p=0.004, d=0.4, E=2, $\mu = 0.45$ (0.16 0.77)
T3-C3	ភ្	t(32.4)=-1.53, p=0.343, d=- 0.4, E=0, μ =-0.39 (-0.91 0.12)	t (34.34) =-2.13, p=0.087, d=- 0.56, E=0, μ =-0.54 (-1.04 - 0.03)	U=458, p=0.646, d=0.08, E=0, $\mu = 0.19 (-0.3 \ 0.67)$	t(34.7)=3.04, p=0.005, d=0.79, E=2, μ =0.74 (0.25 1.23)	U=633, p=0.002, d=0.44, E=2, $\mu = 0.56$ (0.22 0.94)
C4-	C4-CZ	t(36.79)=-2.01, p=0.244, d=- 0.53, E=0, μ =-0.51 (-1.02 0)	t(30.78)=-2.7, p=0.087, d=- 0.71, E=0, μ =-0.67 (-1.16 - 0.17)	U=488, p=0.483, d=0.14, E=0, μ =0.26 (-0.22 0.71)	U=617, p=0.003, d=0.4, E=2, $\mu = 0.68 (0.27 1.11)$	U=616, p=0.004, d=0.4, E=2, $\mu = 0.39$ (0.16 0.66)
C3-	C3-CZ	$t(24.59)=-1.39$, $p=0.351$, $d=-0.36$, $E=0$, $\mu=-0.36$ (-0.87 0.16)	t(29.58)=-1.95, p=0.113, d=- 0.51, E=0, μ =-0.49 (-1 0.02)	t($(35.05)=0.53$, p= 0.657 , d= 0.14 , E= 0 , μ = 0.14 (- 0.39 0.66)	t(37)=2.31, p=0.025, d=0.61, E=2, μ =0.58 (0.08 1.09)	U=626, p=0.003, d=0.42, E=2, $\mu = 0.68$ (0.27 1.06)
CZ-PZ	Zd	t(35.49)=-1.97, p=0.244, d=- 0.52, E=0, μ =-0.5 (-1.01 0.01)	t(35.95)=-2.45, p=0.087, d=- 0.64, E=0, μ =-0.61 (-1.11 - 0.11)	$t(37)=1.37, p=0.31, d=0.36, E=0, \mu=0.36$ (-0.16 0.88)	t(34.37)=3.33, p=0.003, d=0.88, E=3, $\mu = 0.81$ (0.32 1.3)	U=612, p=0.004, d=0.39, E=3, μ =0.55 (0.15 1.02)
C4-P4	P4	t(36.51)=-1.25, p=0.353, d=- 0.33, E=0, μ =-0.33 (-0.85 0.19)		t (36.98)=2.29, p=0.119, d=0.6, E=0, μ =0.58 (0.07 1.09)	01, d=0.52 [.31]	U=590, p=0.009, d=0.35, E=1, $\mu = 0.54$ (0.13 0.99)
C3-P3	P3	t(36.1)=-1.28, p=0.353, d=- 0.34, E=0, μ =-0.33 (-0.85 0.19)	t(36.53)=-1.79, p=0.113, d=- 0.47, E=0, μ =-0.46 (-0.97 0.05)	U=580, p=0.118, d=0.33, E=0, μ =0.62 (0.1 1.04)	t(36.73)=3.25, p=0.003, d=0.85, E=3, μ =0.79 (0.3 1.28)	U=608, p=0.004, d=0.38, E=1, $\mu = 0.57 (0.17 \ 0.98)$
T4-T6	L6	t(31.91)=-0.54, p=0.651, d=- 0.14, E=0, μ =-0.14 (-0.66 0.38)	t(34.88)=-1.89, p=0.113, d=- 0.49, E=0, μ =-0.48 (-0.99 0.03)	t(36.8)=1.9, p=0.151, d=0.5, E=0, $\mu = 0.49$ (-0.03 1)	U=671, p _i 0.001, d=0.51, E=3, $\mu = 0.99 (0.56 \ 1.38)$	U=598, p=0.007, d=0.36, E=1, $\mu = 0.43 (0.13 0.82)$
T_{3-T_5}	$\Gamma 5$	t(35.65)=-2, p=0.244, d=-0.52, E=0, μ =-0.51 (-1.02 0)	t(36.39)=-1.75, p=0.117, d=- 0.46, E=0, μ =-0.45 (-0.96 0.07)	U=510, p=0.31, d=0.18, E=0, μ =0.37 (-0.17 0.82)	U=641, p=0.001, d=0.45, E=3, $\mu = 0.81$ (0.39 1.26)	U=619, p=0.004, d=0.41, E=2, $\mu = 0.6 (0.22 \ 1.04)$
P4–PZ	ΡZ	t(34.44)=-1.35, p=0.351, d=- 0.35, E=0, μ =-0.35 (-0.87 0.17)	t (33.72)=-2.59, p=0.087, d=- 0.68, E=0, μ =-0.64 (-1.14 - 0.15)	t(36.7)=1.88, p=0.151, d=0.49, E=0, $\mu = 0.48$ (-0.03 0.99)	t(33.06)=4.29, pi0.001, d=1.12, E=2, $\mu = 0.98$ (0.52 1.44)	U=608, p=0.004, d=0.38, E=1, $\mu = 0.5$ (0.14 0.92)
P3-PZ	Z	t(28.47)=-1.51, p=0.343, d=- 0.39, E=0, μ =-0.39 (-0.9 0.13)	t(30.04)=-2.31, p=0.087, d=- 0.6, E=0, μ =-0.58 (-1.08 -0.07)	t(37)=1.67, p=0.211, d=0.44, E=0, μ =0.43 (-0.09 0.95)	$t(35.97)=2.76$, $p=0.009$, $d=0.73$, $E=3$, $\mu=0.69$ (0.19 1.19)	U=620, p=0.004, d=0.41, E=2, $\mu = 0.7 (0.25 \ 1.08)$

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3	70-0 T				p=0.000,	U-091, P-0.001, 4-0.30, E-1,
		$0.09, E=0, \mu = -0.09$ (-0.62 0.43)	$0.44,\mathrm{E}{=}0,\mu={-}0.43$ (-0.94 0.08)	$d=0.52, E=0, \mu = 0.5$ (-0.01	$E=3, \ \mu=0.7 \ (0.21 \ 1.2)$	$\mu=0.47~(0.13~0.87)$
				(10.1		
ъ	T5-01	U=366, $p=0.521$, $d=0.11$, $E=0$,	t(34.59)=-1.56, p=0.143, d=-	t(36.62)=2.5, p=0.118, d=0.65,	t(36.79)=3.42, p=0.002, d=0.9,	U=575, $p=0.017$, $d=0.32$, $E=1$,
		μ =-0.18 (-0.64 0.24)	0.41, E=0, μ =-0.4 (-0.92 0.11)	$E=0, \ \mu=0.63 \ (0.12 \ 1.13)$	E=3, $\mu = 0.82 \ (0.34 \ 1.31)$	$\mu=$ 0.37 (0.06 0.95)
σ	P4-O2	t(31.54)=-1.03, p=0.443, d=-	t(30.38)=-1.34, p=0.195, d=-	t(28.88)=2.39, p=0.118,	U=655, $p=0.001$, $d=0.48$, $E=3$,	U=571, $p=0.019$, $d=0.31$, $E=1$,
		0.27, E=0, μ =-0.27 (-0.79 0.25)	$0.35, E{=}0, \mu ={-}0.34 \ ({-}0.86 \ 0.17)$	d=0.62, E=0, μ =0.6 (0.1	$\mu = 0.77 \ (0.43 \ 1.23)$	$\mu=$ 0.37 (0.07 0.68)
				1.1)		
σ	P_{3-01}	U=399, $p=0.752$, $d=0.04$, $E=0$,		t(34.03)=3.15, p=0.062,	$t(36.78) = 4.26, p_i 0.001, d = 1.12,$	U=592, $p=0.008$, $d=0.35$, $E=1$,
		μ =-0.06 (-0.54 0.43)	0.23, E=0, μ =-0.23 (-0.76 0.29)	d=0.82, E=0, μ =0.76 (0.28	E=3, $\mu = 0.98$ (0.52 1.44)	$\mu=$ 0.46 (0.11 0.86)
				1.25)		
σ	01 - 02	t(36.08)=-1.86, p=0.244, d=-	t(29.2)=-2.17, p=0.087, d=-	t(25.85)=1.93, $p=0.151$, $d=0.5$,	U=655, $p=0.001$, $d=0.48$, $E=3$,	U=526, $p=0.101$, $d=0.22$, $E=0$,
		0.49, E=0, μ =-0.47 (-0.99 0.04)	0.57, E=0, μ =-0.55 (-1.05 -	E=0, $\mu = 0.49$ (-0.02 0.99)	$\mu = 0.88 \ (0.47 \ 1.37)$	$\mu=$ 0.22 (-0.05 0.53)
			0.04)			
β	F8-F4	U=551, $p=0.418$, $d=0.27$, $E=0$,	U=470, $p=0.537$, $d=0.1$, $E=0$,	U=595, $p=0.008$, $d=0.36$, $E=2$,	U=612, $p=0.005$, $d=0.39$, $E=2$,	U=659, $p=0.001$, $d=0.49$, $E=2$,
		$\mu=$ 0.41 (0.02 0.82)	$\mu=$ 0.19 (-0.23 0.64)	$\mu = 0.55 \; (0.17 \; 0.93)$	$\mu=$ 0.51 (0.2 0.85)	$\mu = 0.57 (0.23 0.99)$
β	F7-F3	U=525, $p=0.418$, $d=0.21$, $E=0$,	U=461, $p=0.588$, $d=0.08$, $E=0$,	U=613, $p=0.004$, $d=0.39$, $E=1$,	U=607, $p=0.006$, $d=0.38$, $E=2$,	U=627, $p=0.002$, $d=0.42$, $E=3$,
		μ =0.29 (-0.06 0.71)	μ =0.1 (-0.23 0.47)	$\mu=$ 0.64 (0.26 0.98)	$\mu=$ 0.41 (0.14 0.72)	$\mu = 0.45 \ (0.15 \ 0.81)$
β	F4-C4	U=497, $p=0.418$, $d=0.16$, $E=0$,	t(21.09)=2.13, p=0.227,	t(36.83)=3.1, p=0.005, d=0.81,	U=603, $p=0.006$, $d=0.37$, $E=1$,	U=654, $p=0.001$, $d=0.48$, $E=3$,
		$\mu=0.32$ (-0.14 0.88)	$\mu = 0.$	\sim	$\mu=0.63~(0.22~1.13)$	$\mu = 0.65 \ (0.22 \ 0.99)$
β	F3-C3	U=484, $p=0.5$, $d=0.13$, $E=0$,	U=459, $p=0.588$, $d=0.08$, $E=0$,	U=598, $p=0.007$, $d=0.36$, $E=3$,	U=583, $p=0.012$, $d=0.33$, $E=3$,	U=660, $p=0.001$, $d=0.49$, $E=3$,
		$\mu=$ 0.24 (-0.19 0.62)	μ =0.16 (-0.3 0.56)	$\mu = 0.6 \; (0.2 \; 0.95)$	$\mu = 0.49~(0.12~0.86)$	$\mu = 0.59 \ (0.24 \ 0.91)$
β	F4-FZ	U=499, $p=0.418$, $d=0.16$, $E=0$,	U=566, $p=0.175$, $d=0.3$, $E=0$,	t(30.06)=3.79, p=0.001,	U=641, $p=0.003$, $d=0.45$, $E=3$,	U=643, $p=0.001$, $d=0.46$, $E=3$,
		$\mu=$ 0.23 (-0.11 0.59)	$\mu=$ 0.45 (0.05 0.81)	d=0.99, E=2, μ =0.89 (0.42	$\mu = 0.69 \ (0.32 \ 1.14)$	μ =0.48 (0.2 0.83)
				1.36)		
β	FZ-CZ	U=523, $p=0.418$, $d=0.21$, $E=0$,	t(25.79)=1.13, p=0.429,	t(36.66) = 2.43, p = 0.02, d = 0.64,	t(35.15)=3.42, $p=0.003$, $d=0.9$,	U=647, $p=0.001$, $d=0.46$, $E=3$,
		$\mu=$ 0.37 (-0.06 0.84)	d=0.29, E=0, μ =0.29 (-0.23	E=3, μ =0.61 (0.11 1.12)	E=1, μ =0.82 (0.34 1.3)	$\mu = 0.44 \ (0.16 \ 0.76)$
			0.81)			
θ	F3-FZ	U=499, $p=0.418$, $d=0.16$, $E=0$,	U=566, $p=0.175$, $d=0.3$, $E=0$,	U=626, $p=0.003$, $d=0.42$, $E=2$,	U=658, $p=0.003$, $d=0.49$, $E=3$,	U=654, $p=0.001$, $d=0.48$, $E=3$,
		μ =0.27 (-0.17 0.72)	$\mu=$ 0.46 (0.07 0.92)	μ =0.74 (0.33 1.13)	$\mu = 0.68 \ (0.33 \ 1.05)$	$\mu = 0.52 \ (0.19 \ 0.89)$
θ	T4-C4	U=566, p=0.418, d=0.3, E=0,	U=500, p=0.429, d=0.16, E=0,	U=599, $p=0.007$, $d=0.37$, $E=2$,	U=626, $p=0.003$, $d=0.42$, $E=2$,	U=632, $p=0.002$, $d=0.43$, $E=2$,
		$\mu=$ 0.51 (0.09 1.04)	$\mu=$ 0.31 (-0.19 0.85)	$\mu=$ 0.7 (0.2 1.22)	$\mu=0.72~(0.28~1.12)$	$\mu=$ 0.48 (0.21 0.77)
β	T3-C3	U=527, $p=0.418$, $d=0.22$, $E=0$,	t(32.3)=0.91, p=0.487, d=0.24,	U=577, $p=0.016$, $d=0.32$, $E=3$,	U=616, $p=0.004$, $d=0.4$, $E=2$,	U=649, $p=0.001$, $d=0.47$, $E=2$,
		$\mu=$ 0.38 (-0.05 0.97)	$\mathbf{E}{=}0,\ \mu {=}0{.}24$ (-0.29 0.76)	$\mu = 0.55 \ (0.17 \ 1.05)$	$\mu=$ 0.73 (0.25 1.21)	$\mu=$ 0.54 (0.26 0.95)
β	C4-CZ	U=506, $p=0.418$, $d=0.18$, $E=0$,	U=422, $p=0.982$, $d=0$, $E=0$,	U=610, $p=0.005$, $d=0.39$, $E=2$,	U=599, $p=0.007$, $d=0.37$, $E=2$,	U=616, $p=0.003$, $d=0.4$, $E=2$,
		$\mu=$ 0.32 (-0.17 0.91)	$\mu=$ 0.02 (-0.43 0.55)	$\mu=0.65~(0.23~1.06)$	$\mu=$ 0.62 (0.17 1.13)	$\mu = 0.43 (0.15 0.69)$
β	C3-CZ	U=467, $p=0.571$, $d=0.1$, $E=0$,	t(32.68)=1.09, p=0.429,	t(36.22) = 1.66, p = 0.103,	t(35.09)=3.36, p=0.003,	U=640, $p=0.001$, $d=0.45$, $E=2$,
		μ =0.18 (-0.35 0.66)	d=0.28, E=0, μ =0.28 (-0.24	d=0.43, E=0, μ =0.43 (-0.09	d=0.88, E=2, μ =0.81 (0.33	$\mu=$ 0.63 (0.26 1.03)
			0.8)	0.94)	1.29)	
β	CZ-PZ	U=515, $p=0.418$, $d=0.19$, $E=0$,	t(30.19)=1.55, p=0.368, d=0.4,		U=568, $p=0.021$, $d=0.3$, $E=3$,	
		$\mu=$ 0.46 (-0.17 1.1)	$E=0, \ \mu=0.4$ (-0.12 0.91)	$\mu = 0.69 \ (0.26 \ 1.12)$	$\mu = 0.65 \ (0.11 \ 1.22)$	$\mu = 0.41 \ (0.12 \ 0.81)$

A.2 Results for epoch 1

β	C4-P4	U=517, p=0.418, d=0.2, E=0, $\mu = 0.46$ (-0.12 1.07)	U=525, p=0.368, d=0.21, E=0, μ =0.41 (-0.1 1.03)	U=667, p=0.001, d=0.5, E=3, μ =0.87 (0.46 1.32)	U=637, p=0.003, d=0.44, E=2, $\mu = 0.79$ (0.34 1.3)	U=601, p=0.005, d=0.37, E=2, μ =0.56 (0.13 1.15)
β	C3-P3	U=506, $p=0.418$, $d=0.18$, $E=0$, $\mu = 0.36$ (-0.14 0.95)	U=499, p=0.429, d=0.16, E=0, u = 0.33 (-0.16 0.86)	$U=644$, $p=0.001$, $d=0.46$, $E=3$, $\mu=0.82$ (0.37.1.24)	$U=584$, $p=0.012$, $d=0.34$, $E=3$, $\mu=0.63$ (0.15 1.23)	U=607, p=0.004, d=0.38, E=2, u = 0.55 (0.15 1.08)
β	T4-T6			=680, =0.86	U=632, $p=0.003$, $d=0.43$, $E=1$, $u=0.74$ (0.28 1.21)	U=623, $p=0.003$, $d=0.41$, $E=1$, $u=0.48$ (0.16 0.85)
β	T3-T5			=637, =0.75	$\mu = 0.89 (0.41 \ 1.36)$	$\mu = 0.5$ (0.17 0.92) $\mu = 0.5$ (0.17 0.92)
β	P4-PZ	U=476, p=0.5, d=0.11, E=0, $\mu = 0.22$ (-0.24 0.92)	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{llllllllllllllllllllllllllllllllllll$
β	P3-PZ	U=478, p=0.5, d=0.12, E=0, μ =0.33 (-0.27 0.91)	U=498, p=0.429, d=0.16, E=0, μ =0.3 (-0.15 0.74)	$t(36.96)=2.33, p=0.024, d=0.61, E=3, \mu=0.59 (0.08 1.1)$	U=595, p=0.008, d=0.36, E=3, $\mu = 0.74$ (0.21 1.2)	U=633, p=0.002, d=0.44, E=3, $\mu = 0.52 (0.23 \ 0.91)$
β	T6-O2	U=451, p=0.699, d=0.06, E=0, μ =0.1 (-0.31 0.66)	U=458, p=0.588, d=0.08, E=0, μ =0.11 (-0.39 0.58)	t(36.19)=2.59, p=0.015, d=0.68, E=3, μ =0.65 (0.15 1.14)	U=577, p=0.015, d=0.32, E=1, μ =0.49 (0.08 1.02)	U=580, p=0.013, d=0.33, E=1, μ =0.33 (0.08 0.67)
β	T_{5-O1}	U=460, p=0.623, d=0.08, E=0, μ =0.13 (-0.23 0.67)	$t(29.21)=1.93, p=0.273, d=0.5, E=0, \mu = 0.49 (-0.02 1)$	t(36.63)=3.92, p=0.001, d=1.03, E=3, μ =0.92 (0.45 1.39)	U=605, p=0.006, d=0.38, E=2, μ =0.65 (0.17 1.15)	U=584, p=0.011, d=0.34, E=1, $\mu = 0.27$ (0.04 0.71)
β	P4-02	U=436, p=0.848, d=0.03, E=0, μ =0.05 (-0.39 0.52)	U=519, p=0.368, d=0.2, E=0, μ =0.38 (-0.11 0.83)	t(32.51)=3.97, p=0.001, d=1.04, E=3, μ =0.92 (0.46 1.39)	U=590, p=0.009, d=0.35, E=2, $\mu = 0.55 (0.16 \ 0.95)$	U=584, p=0.011, d=0.34, E=1, μ =0.29 (0.07 0.53)
β	P3-01	U=504, p=0.418, d=0.17, E=0, $\mu = 0.4$ (-0.18 0.9)	t (29.35)=2.48, p=0.175, d=0.65, E=0, μ =0.61 (0.12 1.11)	t(35.09)=4.55, p ₁ 0.001, d=1.19, E=3, $\mu = 1.02$ (0.57 1.47)	U=621, p=0.003, d=0.41, E=2, μ =0.71 (0.31 1.14)	U=613, p=0.003, d=0.39, E=2, $\mu = 0.36$ (0.1 0.77)
β	01-02	U=431, p=0.871, d=0.02, E=0, $\mu = 0.03$ (-0.42 0.46)	U=503, p=0.429, d=0.17, E=0, $\mu = 0.27$ (-0.15 0.77)	t (31.39)=3.51, p=0.002, d=0.92, E=2, μ =0.83 (0.36 1.31)	U=591, p=0.009, d=0.35, E=3, $\mu = 0.67 (0.18 \ 1.12)$	U=568, p=0.021, d=0.3, E=1, $\mu = 0.24$ (0.03 0.53)
х	F8-F4	U=609, p=0.033, d=0.39, E=1, μ =0.35 (0.11 0.65)	U=570, p=0.109, d=0.31, E=0, μ =0.48 (0.05 0.89)	U=644, p=0.002, d=0.46, E=2, μ =0.6 (0.26 0.95)	U=658, p=0.001, d=0.49, E=2, $\mu = 0.62 (0.29 0.98)$	U=686, p:0.001, d=0.54, E=2, μ =0.65 (0.37 0.96)
7	F7-F3	U=568, p=0.06, d=0.3, E=0, $\mu = 0.22 (0.04 0.48)$	U=546, p=0.109, d=0.26, E=0, μ =0.36 (0 0.77)	U=624, p=0.003, d=0.42, E=2, μ =0.57 (0.2 0.89)	U=624, p=0.002, d=0.42, E=2, $\mu = 0.47 (0.15 \ 0.87)$	U=624, p=0.004, d=0.42, E=2, $\mu = 0.35$ (0.1 0.56)
٨	F4-C4	U=539, p=0.129, d=0.24, E=0, $\mu = 0.14$ (-0.01 0.35)	U=547, p=0.109, d=0.26, E=0, μ =0.3 (0 0.88)	U=655, p=0.001, d=0.48, E=3, μ =0.69 (0.26 1.28)	U=660, p=0.001, d=0.49, E=2, μ =0.64 (0.22 1.01)	U=634, p=0.004, d=0.44, E=2, μ =0.32 (0.11 0.63)
х	F3-C3	U=584, p=0.038, d=0.34, E=1, $\mu = 0.21 (0.06 \ 0.47)$	U=593, p=0.109, d=0.35, E=0, $\mu = 0.41$ (0.1 0.88)	U=655, p=0.001, d=0.48, E=3, μ =0.57 (0.27 0.9)	U=660, p=0.001, d=0.49, E=2, $\mu = 0.54$ (0.25 0.83)	U=650, p=0.003, d=0.47, E=2, $\mu = 0.3 (0.13 0.56)$
×	F4-FZ	U=583, p=0.038, d=0.33, E=1, μ =0.2 (0.04 0.42)	U=574, p=0.109, d=0.31, E=0, μ =0.33 (0.05 0.73)	U=680, p=0.001, d=0.53, E=3, μ =0.65 (0.31 1.02)	U=652, p=0.001, d=0.47, E=2, $\mu = 0.47$ (0.19 0.86)	U=628, p=0.004, d=0.42, E=2, μ =0.29 (0.11 0.64)
λ	FZ-CZ	U=581, p=0.038, d=0.33, E=1, $\mu = 0.17$ (0.03 0.39)	U=552, p=0.109, d=0.27, E=0, μ =0.19 (0.01 0.47)	U=634, p=0.002, d=0.44, E=3, μ =0.5 (0.21 0.75)	U=646, p=0.001, d=0.46, E=2, μ =0.37 (0.16 0.65)	U=619, p=0.004, d=0.41, E=1, μ =0.18 (0.06 0.31)
Х	F3-FZ	U=594, p=0.038, d=0.36, E=1, $\mu = 0.2 (0.06 \ 0.43)$	U=575, p=0.109, d=0.32, E=0, $\mu = 0.39$ (0.08 0.83)	$\begin{array}{llllllllllllllllllllllllllllllllllll$	U=647, p=0.001, d=0.46, E=2, $\mu = 0.44$ (0.16 0.79)	U=627, p=0.004, d=0.42, E=1, $\mu = 0.3$ (0.11 0.62)
7	T4-C4	U=538, p=0.129, d=0.24, E=0, μ =0.16 (-0.01 0.38)	U=556, p=0.109, d=0.28, E=0, μ =0.29 (0.02 0.58)	U=573, p=0.017, d=0.31, E=3, $\mu = 0.32 (0.05 0.63)$	U=615, p=0.003, d=0.4, E=2, $\mu = 0.38$ (0.14 0.68)	U=614, p=0.005, d=0.4, E=1, $\mu = 0.23$ (0.09 0.55)

T3-C3	3 U=617, p=0.033, d=0.4, E=1,	U=563, $p=0.109$, $d=0.29$, $E=0$,	U=607, $p=0.004$, $d=0.38$, $E=2$,	U=647, $p=0.001$, $d=0.46$, $E=2$,	U=636, $p=0.004$, $d=0.44$, $E=2$,
	$\mu=$ 0.26 (0.1 0.48)	$\mu=0.34~(0.04~0.72)$	$\mu=$ 0.42 (0.14 0.82)	$\mu=$ 0.54 (0.25 0.9)	$\mu=0.31~(0.11~0.6)$
C4-CZ	\mathbb{Z} U=515, p=0.218, d=0.19, E=0,	U=536, $p=0.128$, $d=0.24$, $E=0$,	U=615, $p=0.004$, $d=0.4$, $E=1$,	U=615, $p=0.003$, $d=0.4$, $E=2$,	U=619, $p=0.004$, $d=0.41$, $E=1$,
	$\mu=$ 0.1 (-0.03 0.29)	$\mu=$ 0.26 (-0.02 0.6)	$\mu=$ 0.45 (0.13 0.79)	$\mu=$ 0.41 (0.14 0.78)	$\mu=0.22~(0.06~0.54)$
C3-CZ	\mathbb{Z} U=588, p=0.038, d=0.34, E=1,	U=539, $p=0.124$, $d=0.24$, $E=0$,	U=607, $p=0.004$, $d=0.38$, $E=2$,	U=627, $p=0.002$, $d=0.42$, $E=2$,	U=623, $p=0.004$, $d=0.41$, $E=2$,
	$\mu=$ 0.22 (0.05 0.4)	$\mu=$ 0.27 (-0.01 0.67)	$\mu=$ 0.5 (0.17 0.92)	$\mu=$ 0.5 (0.18 0.89)	$\mu=0.24~(0.08~0.47)$
CZ-PZ	\mathbb{Z} U=524, p=0.191, d=0.21, E=0,	U=554, $p=0.109$, $d=0.27$, $E=0$,	U=653, $p=0.001$, $d=0.48$, $E=1$,	U=631, $p=0.002$, $d=0.43$, $E=2$,	U=578, $p=0.018$, $d=0.32$, $E=1$,
	$\mu=$ 0.08 (-0.01 0.25)	$\mu=$ 0.26 (0.01 0.57)	$\mu=$ 0.74 (0.33 1.19)	$\mu=$ 0.44 (0.16 0.83)	$\mu=$ 0.13 (0.02 0.27)
C4-P4	4 U=496, p=0.293, d=0.16, E=0,	U=482, $p=0.357$, $d=0.13$, $E=0$,	U=634, $p=0.002$, $d=0.44$, $E=1$,	U=593, $p=0.008$, $d=0.35$, $E=2$,	U=566, $p=0.029$, $d=0.3$, $E=1$,
	$\mu=$ 0.1 (-0.07 0.34)	$\mu=$ 0.13 (-0.14 0.52)	$\mu=$ 0.58 (0.21 0.98)	$\mu=$ 0.45 (0.1 0.98)	$\mu=$ 0.28 (0.03 0.7)
C3-P3	3 U=494, p=0.293, d=0.15, E=0,	U=545, $p=0.109$, $d=0.26$, $E=0$,	U=622, $p=0.003$, $d=0.41$, $E=1$,	U=610, $p=0.004$, $d=0.39$, $E=2$,	U=578, $p=0.018$, $d=0.32$, $E=1$,
	$\mu=$ 0.09 (-0.05 0.32)	$\mu=$ 0.25 (0 0.65)	$\mu=$ 0.48 (0.21 0.87)	$\mu=$ 0.46 (0.14 0.98)	$\mu=0.23~(0.05~0.55)$
T4-T6	$(6 \mid U=504, p=0.264, d=0.17, E=0, 1$	U=524, $p=0.17$, $d=0.21$, $E=0$,	U=594, $p=0.007$, $d=0.36$, $E=1$,	U=621, $p=0.003$, $d=0.41$, $E=1$,	U=593, $p=0.012$, $d=0.35$, $E=1$,
	$\mu=$ 0.13 (-0.07 0.37)	$\mu=$ 0.22 (-0.05 0.58)	$\mu=$ 0.43 (0.11 0.75)	$\mu=$ 0.42 (0.13 0.73)	$\mu=$ 0.24 (0.06 0.56)
T3-T5	[5] U=538, p=0.129, d=0.24, E=0,	U=523, $p=0.17$, $d=0.21$, $E=0$,	U=599, $p=0.006$, $d=0.37$, $E=2$,	U=625, $p=0.002$, $d=0.42$, $E=2$,	U=587, $p=0.015$, $d=0.34$, $E=1$,
	$\mu=$ 0.14 (-0.01 0.34)	$\mu=$ 0.29 (-0.07 0.61)	$\mu=$ 0.54 (0.17 0.98)	$\mu=$ 0.47 (0.17 0.85)	$\mu=$ 0.25 (0.06 0.51)
P4-PZ	Z U=521, p=0.194, d=0.21, E=0,	U=507, $p=0.218$, $d=0.18$, $E=0$,	U=611, $p=0.004$, $d=0.39$, $E=1$,	U=620, $p=0.003$, $d=0.41$, $E=2$,	U=578, $p=0.018$, $d=0.32$, $E=1$,
	$\mu=$ 0.08 (-0.03 0.25)	$\mu=$ 0.14 (-0.06 0.38)	$\mu=$ 0.58 (0.19 1.02)	$\mu=$ 0.44 (0.16 0.85)	$\mu=$ 0.12 (0.02 0.32)
P3-PZ	Z U=549, p=0.115, d=0.26, E=0,	U=507, $p=0.218$, $d=0.18$, $E=0$,	U=617, $p=0.004$, $d=0.4$, $E=2$,	U=647, $p=0.001$, $d=0.46$, $E=2$,	U=606, $p=0.006$, $d=0.38$, $E=1$,
	$\mu=$ 0.12 (0 0.31)	$\mu=$ 0.18 (-0.08 0.48)	$\mu=$ 0.6 (0.24 1)	$\mu=$ 0.49 (0.21 0.81)	$\mu=$ 0.18 (0.05 0.32)
T6-O2	0.2 U=506, p=0.264, d=0.18, E=0,	U=515, $p=0.204$, $d=0.19$, $E=0$,	U=585, $p=0.01$, $d=0.34$, $E=1$,	U=570, $p=0.019$, $d=0.31$, $E=1$,	U=543, $p=0.065$, $d=0.25$, $E=0$,
	$\mu=$ 0.09 (-0.04 0.25)	$\mu=$ 0.19 (-0.07 0.52)	$\mu=$ 0.52 (0.13 1)	$\mu=$ 0.27 (0.04 0.53)	μ =0.12 (-0.01 0.31)
T5-O1	1 U=494, p=0.293, d=0.15, E=0, $ $	U=500, $p=0.251$, $d=0.16$, $E=0$,	U=610, $p=0.004$, $d=0.39$, $E=1$,	U=580, $p=0.013$, $d=0.33$, $E=1$,	U=539, $p=0.071$, $d=0.24$, $E=0$,
	$\mu=$ 0.08 (-0.05 0.31)	$\mu=$ 0.19 (-0.1 0.57)	$\mu=$ 0.5 (0.15 0.87)	$\mu=$ 0.26 (0.04 0.61)	μ =0.11 (-0.01 0.37)
P4-O2	02 U=467, p=0.493, d=0.1, E=0,	U=513, $p=0.204$, $d=0.19$, $E=0$,	U=615, $p=0.004$, $d=0.4$, $E=1$,	U=603, $p=0.005$, $d=0.37$, $E=1$,	U=545, $p=0.063$, $d=0.26$, $E=0$,
	$\mu=$ 0.03 (-0.08 0.18)	$\mu=$ 0.12 (-0.05 0.39)	$\mu=$ 0.51 (0.21 0.9)	$\mu=$ 0.27 (0.08 0.47)	μ =0.1 (0 0.31)
P3-01	1 U=464, p=0.501, d=0.09, E=0,	U=495, $p=0.272$, $d=0.15$, $E=0$,	U=606, $p=0.004$, $d=0.38$, $E=2$,	U=596, $p=0.007$, $d=0.36$, $E=1$,	U=528, $p=0.099$, $d=0.22$, $E=0$,
	$\mu=$ 0.04 (-0.06 0.21)	$\mu=$ 0.15 (-0.1 0.66)	$\mu=$ 0.49 (0.18 0.79)	$\mu=$ 0.29 (0.07 0.61)	μ =0.09 (-0.01 0.34)
O1-O2	02 U=480, p=0.391, d=0.12, E=0, \Box	U=469, p=0.453, d=0.1, E=0,	U=594, p=0.007, d=0.36, E=2,	U=573, $p=0.018$, $d=0.31$, $E=1$,	U=488, $p=0.296$, $d=0.14$, $E=0$,
	$\mu=$ 0.05 (-0.07 0.19)	$\mu=$ 0.11 (-0.15 0.45)	$\mu=$ 0.47 (0.14 0.85)	$\mu=0.23~(0.03~0.51)$	$\mu = 0.05$ (-0.04 0.19)

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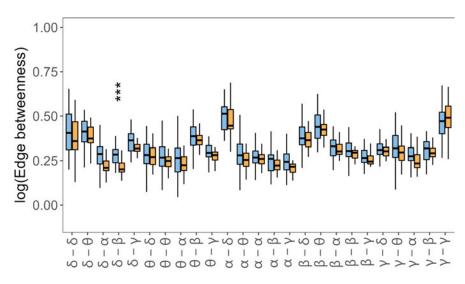


Figure A.6: Importance of each type of frequency coupling of HC (blue) and AD (orange) measured by edge betweenness in epoch 1. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.001$ "***", $p \leq 0.001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

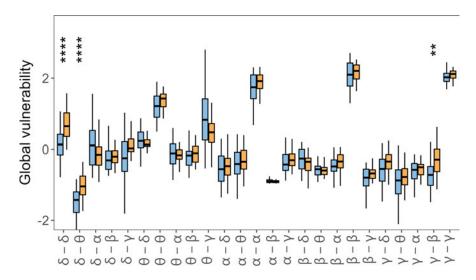


Figure A.7: Global vulnerability of HC (blue) and AD (orange) in epoch 1. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "***", $p \leq 0.01$ "**", and $p \leq 0.05$ "*".

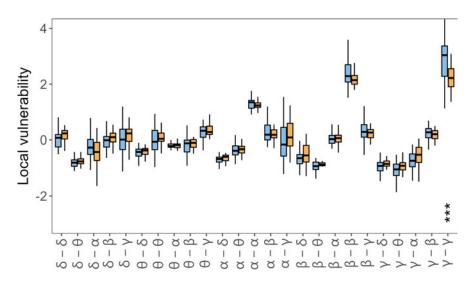


Figure A.8: Local vulnerability of HC (blue) and AD (orange) in epoch 1. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.0001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "**", $p \le 0.01$ "**", and $p \le 0.05$ "*".

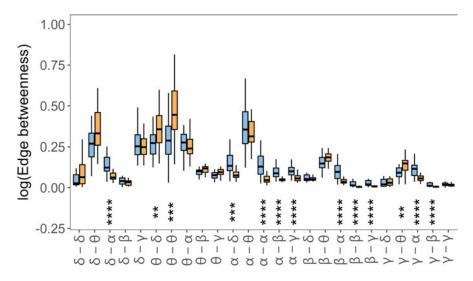


Figure A.9: Importance of each type of frequency coupling of HC (blue) and AD (orange) measured by weighted edge betweenness in epoch 1. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.0001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "**".

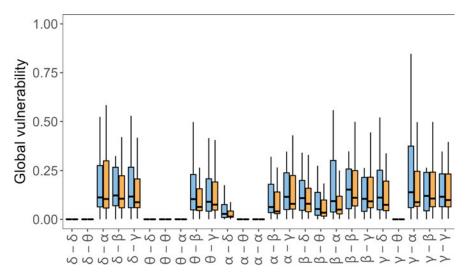


Figure A.10: Weighted global vulnerability of HC (blue) and AD (orange) in epoch 1. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks.

The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

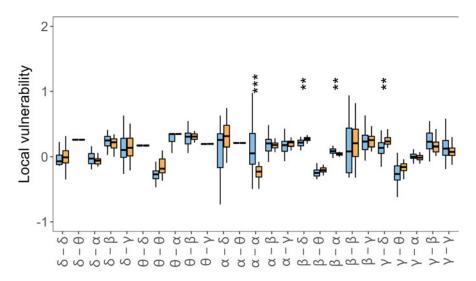


Figure A.11: Weighted local vulnerability of HC (blue) and AD (orange) in epoch 1. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "***", $p \leq 0.001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

Table A.5: Results from epoch 1 comparing unweighted edge betweenness. The results are reported as follows:
stausues value (degrees of freedom), p-value of the test, Conen's d'enect size of nonparameteric auternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were
observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted
with bold text.

_	δ	θ	σ	β	λ
4	t(36.68)=0.95, $p=0.348$, $d=0.25$,	U=508, p=0.175, d=0.18,	U=591, $p=0.007$, $d=0.35$,	U=636, $p=0.001$, $d=0.44$,	U=542, $p=0.058$, $d=0.25$,
	T=1, E=0, $\mu = 0.25$ (-0.28 0.77)	T=0, E=0, μ = 0.31 (-0.15 0.74)	T=16, E=2, $\mu = 0.62 \ (0.19 \ 1.09)$	T=17, E=3, $\mu = 0.7$ (0.33 1.1)	T=9, E=0, $\mu = 0.32 \ (0 \ 0.54)$
9	U=455, $p=0.594$, $d=0.07$,	U=513, $p=0.151$, $d=0.19$,	U=500, p=0.218, d=0.16,	U=517, $p=0.134$, $d=0.2$,	U=498, p=0.23, d=0.16,
Ь	T=0, E=0, μ = 0.11 (-0.28 0.55)	T=3, E=0, $\mu = 0.28$ (-0.15 0.71)	T=0, E=0, μ = 0.28 (-0.15 0.76)	T=0, E=0, $\mu = 0.33$ (-0.11 0.73)	T=0, E=0, μ = 0.2 (-0.13 0.57)
é	t(36.86)=1.34, $p=0.185$, $d=0.35$,	t(30.26)=1.16, p=0.25, d=0.3,	U=483, p=0.333, d=0.13,	U=521, $p=0.118$, $d=0.21$,	U=528, $p=0.095$, $d=0.22$,
3	T=0, E=0, μ = 0.35 (-0.17 0.87)	T=0, E=0, $\mu = 0.3$ (-0.22 0.82)	T=0, E=0, μ = 0.18 (-0.3 0.64)	T=0, E=0, $\mu = 0.31$ (-0.1 0.73)	T=3, E=0, $\mu = 0.19$ (-0.04 0.42)
0	U=489, p=0.289, d=0.14,	U=475, $p=0.399$, $d=0.11$,	U=472, p=0.426, d=0.11,	U=494, $p=0.255$, $d=0.15$,	U=508, p=0.175, d=0.18,
2	T=0, E=0, μ = 0.19 (-0.15 0.54)	T=0, E=0, μ = 0.15 (-0.23 0.59)	T=0, E=0, μ = 0.18 (-0.25 0.66)	T=1, E=0, $\mu = 0.23$ (-0.18 0.66)	T=1, E=0, $\mu = 0.27$ (-0.14 0.6)
	U=475, $p=0.399$, $d=0.11$,	U=504, $p=0.195$, $d=0.17$,	U=548, $p=0.047$, $d=0.26$,	U=479, $p=0.365$, $d=0.12$,	U=360, p=0.357, d=0.12,
-	T=0, E=0, μ = 0.15 (-0.22 0.52)	T=0, E=0, $\mu = 0.2$ (-0.13 0.53)	T=11, E=2, $\mu = 0.25 \ (0.01 \ 0.48)$	T=0, E=0, $\mu = 0.16$ (-0.18 0.44)	T=0, E=0, $\mu = -0.22$ (-0.68 0.23)

of thresholds where significant differences were observed (T), number of epochs where significant differences were **Table A.6:** Results from epoch 1 comparing unweighted global vulnerability. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	δ	θ	σ	β	λ
4	t(33.22)=-4.38, pi0.001, d=-1.14,	$U=168, p_i 0.001, d=0.51,$	U=532, p=0.083, d=0.23,	U=352, $p=0.294$, $d=0.14$,	t(32.49) = -1.94, $p = 0.058$, $d = -0.51$,
0	T=17, E=3, $\mu = -0.99(-1.45 - 0.54)$	T=18, E=3, $\mu = -0.91(-1.35 - 0.48)$	T=8, E=0, $\mu = 0.44(-0.06 \ 0.96)$	T=3, E=0, $\mu = -0.22(-0.62 \ 0.22)$	T=9, E=0, $\mu = -0.49(-1\ 0.02)$
9	t(30.36)=0.98, p=0.33, d=0.26,	U=326, $p=0.147$, $d=0.19$,	t(31.47)=0.67, p=0.503, d=0.18,	U=341, $p=0.224$, $d=0.16$,	U=546, p=0.05, d=0.26,
ь	T=0, E=0, $\mu = 0.25(-0.27 \ 0.78)$	T=0, E=0, $\mu = -0.41(-0.95 \ 0.14)$	T=0, E=0, $\mu = 0.18(-0.35 \ 0.7)$	T=0, E=0, $\mu = -0.26(-0.8 \ 0.17)$	T=9, E=0, $\mu = 0.49(-0.01 \ 0.95)$
i	t(32.58)=-0.95, p=0.344, d=-0.25,	t(36.41)=-0.83, p=0.412, d=-0.22,	U=352, p=0.296, d=0.14,	U=473, $p=0.414$, $d=0.11$,	U=356, $p=0.326$, $d=0.13$,
3	T=4, E=0, $\mu = -0.25(-0.77\ 0.27)$	T=0, E=0, $\mu = -0.22(-0.74 \ 0.31)$	T=0, E=0, $\mu = -0.28(-0.81 \ 0.2)$	T=3, E=0, $\mu = 0.03(-0.04 \ 0.1)$	T=1, E=0, $\mu = -0.21(-0.6 \ 0.24)$
9	t(36.92)=1.48, p=0.145, d=0.39,	U=455, p=0.594, d=0.07,	t(36.76)=-0.95, p=0.349, d=-0.25,	t(30.7)=-0.86, p=0.392, d=-0.23,	U=321, p=0.126, d=0.2,
٥.	T=8, E=0, $\mu = 0.38(-0.14\ 0.9)$	T=0, E=0, $\mu = 0.08(-0.31 \ 0.49)$	T=4, E=0, $\mu = -0.25(-0.78 \ 0.28)$	T=3, E=0, $\mu = -0.22(-0.75 \ 0.3)$	T=7, E=0, $\mu = -0.39(-0.84 \ 0.11)$
	U=327, p=0.151, d=0.19,	t(32.84)=-1.36, p=0.179, d=-0.36,	U=370, p=0.444, d=0.1,	U=235, $p=0.004$, $d=0.38$,	t(36.21)=-1.79, p=0.079, d=-0.47,
	T=2, E=0, $\mu = -0.23(-0.54\ 0.08)$	T=0, E=0, $\mu = -0.35(-0.87 \ 0.17)$	T=1, E=0, $\mu = -0.2(-0.68 \ 0.26)$	T=13, E=3, $\mu = -0.61(-1.02 - 0.2)$	T=7, E=0, $\mu = -0.46(-0.97 \ 0.06)$

Table A.7: Results from epoch 1 comparing unweighted local vulnerability. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	δ	θ	σ	β	κ
ч	U=308, p=0.083, d=0.23,	t(36.15)=-0.87, p=0.389, d=-0.23, d=-	t(37)=1.86, $p=0.068$, $d=0.49$,	t(35.43)=-1.95, p=0.056, d=-0.51,	t(34.87)=-1.11, p=0.27, d=-0.29,
0	T=9, E=0, $\mu = -0.4$ (-0.82 0.06)	T=2, E=0, $\mu = -0.23$ (-0.75 0.3)	T=9, E=0, $\mu = 0.48$ (-0.04 0.99)	T=7, E=0, $\mu = -0.5$ (-1.01 0.01)	T=0, E=0, $\mu = -0.29$ (-0.81 0.23)
0	U=361, p=0.365, d=0.12,	t(32.16) = -0.52, p = 0.606, d = -0.14,	U= 389 , p= 0.638 , d= 0.06 ,	t(29.01) = -0.85, $p = 0.399$, $d = -0.22$,	t(36.97)=-0.56, p=0.581, d=-0.15,
ь	T=0, E=0, $\mu = -0.21$ (-0.65 0.26)	T=2, E=0, $\mu = -0.14$ (-0.66 0.39)	T=0, E=0, $\mu = -0.08$ (-0.45 0.29)	T=0, E=0, $\mu = -0.22$ (-0.74 0.3)	T=0, E=0, $\mu = -0.15$ (-0.67 0.38)
d	t(35.69)=-1.77, p=0.082, d=-0.46,	t(36.82)=-0.42, p=0.677, d=-0.11,	U=504, $p=0.195$, $d=0.17$,	t(29.31)=1.25, p=0.216, d=0.33,	t(34.1)=-1.23, p=0.223, d=-0.32,
3	T=9, E=0, $\mu = -0.45$ (-0.97 0.06)	T=0, E=0, $\mu = -0.11$ (-0.64 0.42)	T=5, E=0, $\mu = 0.3$ (-0.19 0.61)	T=3, E=0, $\mu = 0.32$ (-0.2 0.84)	T=0, E=0, $\mu = -0.32$ (-0.84 0.2)
9	t(36.26)=-1.61, p=0.114, d=-0.42,	U=360, p=0.357, d=0.12,	t(36.89)=-0.95, $p=0.344$, $d=-0.25$,	U=519, $p=0.126$, $d=0.2$,	t(23.65)=0.83, $p=0.409$, $d=0.22$,
2	T=5, E=0, $\mu = -0.42$ (-0.94 0.1)	T=0, E=0, $\mu = -0.27 (-0.74 \ 0.25)$	T=2, E=0, $\mu = -0.25$ (-0.77 0.27)	T=1, E=0, $\mu = 0.39$ (-0.08 0.96)	T=4, E=0, $\mu = 0.22$ (-0.31 0.74)
i	U=283, $p=0.033$, $d=0.28$,	t(32.95)=-2.29, p=0.026, d=-0.6,	t(36.03)=-1.93, p=0.059, d=-0.51, t(36.03)=-1.93, p=0.059, d=-0.51, t(36.03)=-1.93, t(36.03)	U=474, $p=0.408$, $d=0.11$,	U=635, $p=0.001$, $d=0.44$,
	T=11, E=1, $\mu = -0.4$ (-0.81 -0.03)	T=11, E=1, $\mu = -0.58$ (-1.08 -0.07)	T=9, E=0, $\mu = -0.5$ (-1.01 0.02)	T=2, E=0, $\mu = 0.16$ (-0.26 0.61)	T=13, E=3, $\mu = 0.3$ (0.12 0.49)

of thresholds where significant differences were observed (T), number of epochs where significant differences were **Table A.8:** Results from epoch 1 comparing weighted edge betweenness. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

$ \begin{array}{c} \delta & \text{U}=666, \text{ pi0.001}, \text{ d}=0.53, \\ \mathbf{T}=19, \mathbf{E}=3, \mu=0.23 \ (0.15 \ 0.41) \\ \theta & \text{U}=660.5, \text{ pi0.001}, \text{ d}=0.54, \\ \mathbf{T}=17, \mathbf{E}=3, \mu=0.29 \ (0.01 \ 0.66) \\ 1.1-562, \mu=0.024, \\ \end{array} $		θ	σ	β	λ
$\begin{array}{c c} 0 & \mathbf{T}=19, \mathbf{E}=3, \ \mu=0\\ \hline \theta & \mathbf{U}=660.5, \ \mathbf{p}[0.1, \mathbf{E}=3, \ \mu=0.1, \mathbf{L}=72, \mathbf{E}=3, \ \mu=0.1, \mathbf{L}=72, \mathbf{E}=3, \ \mu=0.1, \mathbf{L}=72, \mathbf{E}=3, \ \mu=0.1, \mathbf{L}=72, \mathbf{E}=12, E$	01, d=0.53,	$U=603$, p $_{1}0.001$, d $=0.49$,	$U=693.5$, p $_{1}0.001$, d $=0.59$,	$U=704$, p $_{1}0.001$, d $=0.58$,	U=635, $p=0.001$, $d=0.44$,
$\theta \qquad \begin{array}{c} \mathbf{U} = 660.5, \ \mathbf{p}_{10.0}, \\ \mathbf{T} = 17, \ \mathbf{E} = 3, \ \mu = 117, \ \mathbf{E} = 3, \ \mathbf{E} = 1, \ \mathbf{E} = 3, \ \mathbf{E} = 1, \ \mathbf{E} = 1,$	0.23 (0.15 0.41)	$T=14, E=3, \mu = 0 (0 0.18)$	T=19, E=3, $\mu = 0.38$ (0.02 0.75)	T=19, E=3, $\mu = 0.97$ (0.58 1.33)	T=18, E=3, $\mu = 0.68$ (0.32 1.01)
T=17, E=3, $\mu = \frac{11-562}{200}$	001, d=0.54,	$U=675.5$, p $_{1}0.001$, d $=0.54$,	U=461, p=0.195, d=0.17,	U=518, p=0.027, d=0.29,	U=389, p=0.638, d=0.06,
11-5620 [T=12, E=3, $\mu = 0.43$ (0.03 0.84)	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=18, E=1, $\mu = 0 \ (0 \ 0)$	T=1, E=0, $\mu = -0.06$ (-0.3 0.23)
	U=563, p=0.011, d=0.33,	U=488, $p=0.096$, $d=0.22$,	U=297.5, p=0.058, d=0.25,	U=346, p=0.255, d=0.15,	U=481, p=0.349, d=0.12,
T=18, E=2, $\mu = 0 \ (0 \ 0.36)$	= 0 (0 0.36)	T=5, E=0, $\mu = 0 \ (0 \ 0)$	T=10, E=1, $\mu = -0.31$ (-0.64 0)	T=2, E=0, $\mu = -0.14$ (-0.43 0.13)	T=1, E=0, $\mu = 0.04$ (-0.04 0.12)
$_{a}$ U=694, p $_{i}$ 0.001, d=0.56,	01, d=0.56,	U=458, $p=0.559$, $d=0.08$,	U=377.5, p=0.481, d=0.09,	U=356, p=0.323, d=0.13,	$U=178$, $p_i0.001$, $d=0.49$,
T=18, E=3, $\mu = 0.34$ (0.16 0.62)	0.34 (0.16 0.62)	T=4, E=0, $\mu = 0.01$ (-0.12 0.17)	T=6, E=0, $\mu = 0$ (-0.06 0)	T=4, E=0, $\mu = -0.05$ (-0.17 0.06)	T=18, E=3, $\mu = -0.74$ (-1.18 -0.36)
U=625, p=0.001, d=0.42,	01, d=0.42,	U=337, p=0.201, d=0.17,	U=390, $p=0.649$, $d=0.06$,	$U=194$, $p_i0.001$, $d=0.46$,	$t(36.57) = -4.16$, $p_10.001$, $d = -1.09$,
T=18, E=3, $\mu = 1.06$ (0.45 1.49)	1.06 (0.45 1.49)	T=2, E=0, $\mu = -0.23$ (-0.71 0.13)	T=1, E=0, $\mu = -0.03$ (-0.15 0.13)	T=14, E=3, $\mu = -0.72$ (-1.1 -0.37)	T=19, E=3, $\mu = -0.96$ (-1.42 -0.5)

Table A.9: Results from epoch 1 comparing weighted global vulnerability. The results are reported as follows: statistics value (decrees of freedom) n-value of the test. Cohen's d effect size or nonnarameteric alternative number
of thresholds where significant differences were observed (T), number of epochs where significant differences were
observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted
with bold text.

$ \begin{array}{c c} \delta & U = 354, p = 0.311, d = 0.13, \\ T = 2, E = 0, \mu = 0 (0 0) \\ \theta & U = 480, p = 0.357, d = 0.12, \\ T = 1, E = 0, \mu = 0 (0 0) \\ \alpha & U = 366, p = 0.408, d = 0.11, \\ \end{array} $	11, d=0.13, t = 0 (0 0) 67, d=0.12, t = 0 (0 0) 08. d=0.11.	$\begin{array}{c} U=284, \ p=0.034, \ d=0.28, \\ T=12, \ E=1, \ \mu=0 \ (0 \ 0) \\ U=286, \ p=0.037, \ d=0.27, \\ T=13, \ E=1, \ \mu=0 \ (0 \ 0) \end{array}$	U=384, p=0.583, d=0.07, T=6, E=0, $\mu = 0$ (0 0)	U=670. p:0.001. d=0.51.	1/02 20)-3 00 000 7-0 2E
	u = 0 (0 0) $57, d=0.12,$ $u = 0 (0 0)$ $108. d=0.11.$	$\begin{array}{c} T=12, \ E=1, \ \mu=0 \ (0 \ 0) \\ U=286, \ p=0.037, \ d=0.27, \\ T=13, \ E=1, \ \mu=0 \ (0 \ 0) \end{array}$	T=6, E=0, $\mu = 0$ (0 0)		$v(z_1, z_3) = z_{\cdot 3}$, $p = 0.000$, $d = 0.13$,
	57, d=0.12, u = 0 (0 0) u = 0 (0 0) 0.08, d=0.11.	U=286, p=0.037, d=0.27, T=13, E=1, μ = 0 (0 0)		T=19, E=3, $\mu = 0.01$ (0 0.13)	T=15, E=2, $\mu = 0.71 \ (0.22 \ 1.2)$
	t = 0 (0 0) 108. d=0.11.	T=13, E=1, $\mu = 0 \ (0 \ 0)$	U=302, p=0.067, d=0.24,	U=373, $p=0.472$, $d=0.1$,	U=494, $p=0.255$, $d=0.15$,
	i08. d=0.11.		T=7, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=1, E=0, $\mu = 0.22$ (-0.19 0.71)
		U=306, p=0.077, d=0.23,	U=301, p=0.065, d=0.24,	U=359, p=0.349, d=0.12,	t(35.04)=-0.66, p=0.515, d=-0.17,
T=3, E=0, $\mu = 0 \ (0 \ 0)$	$\iota = 0 \ (0 \ 0)$	T=9, E=0, $\mu = 0 \ (0 \ 0)$	T=8, E=0, $\mu = -0.07 (-0.17 0)$	T=1, E=0, $\mu = 0 \ (0 \ 0)$	T=5, E=0, $\mu = -0.17 (-0.7 \ 0.35)$
$_{\scriptscriptstyle 2}$ U=617, p=0.002, d=0.4,	002, d=0.4,	U=341, $p=0.224$, $d=0.16$,	U=303, p=0.07, d=0.24,	U=459, $p=0.552$, $d=0.08$,	U=214, $p=0.001$, $d=0.42$,
^{<i>p</i>} T=12, E=3, $\mu = 0.02$ (0 0.13)	= 0.02 (0 0.13)	T=3, E=0, $\mu = 0 \ (0 \ 0)$	T=9, E=0, $\mu = 0 \ (0 \ 0)$	T=6, E=0, $\mu = 0.01$ (-0.05 0.06)	T=13, E=3, $\mu = -0.7$ (-1.07 -0.34)
t(35.38)=-1.22, p=0.228, d=-0.32,	=0.228, d=-0.32,	U=444, $p=0.717$, $d=0.05$,	U=339, p=0.212, d=0.17,	t(36.15)=-5.79, pi0.001, d=-1.52,	$U=186, p_10.001, d=0.48,$
7 T=0, E=0, $\mu = -0$	0.32 (-0.85 0.21)	T=0, E=0, $\mu = -0.32$ (-0.85 0.21) T=0, E=0, $\mu = 0.03$ (-0.19 0.31) T	T=0, E=0, $\mu = -0.15$ (-0.46 0.07)	T=20, E=3, $\mu = -1.22$ (-1.64 -0.79)	T=18, E=3, $\mu = -0.98$ (-1.44 -0.49)

Table A.10: Results from epoch 1 comparing weighted local vulnerability. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	δ	θ	σ	β	λ
x	U=634, $p=0.001$, $d=0.44$,	$U=691, p_{1}0.001, d=0.55,$	U=242, $p=0.005$, $d=0.36$,	$t(34.01) = -3.9, p_10.001, d = -1.02,$	U=478, p=0.374, d=0.12,
0	T=19, E=3, $\mu = 0.9$ (0.43 1.28)	$T=18, E=3, \mu = 0.96 (0.61 1.38)$	T=11, E=3, $\mu = -0.56$ (-0.95 -0.18)	T=11, E=3, $\mu = -0.91$ (-1.38 -0.44)	T=0, E=0, μ = 0.15 (-0.22 0.6)
9	$t(29.56)=3.73, p_10.001, d=0.97,$	$U=705$, p $_{1}0.001$, d $=0.58$,	U=296, $p=0.054$, $d=0.25$,	$t(36.97)=-4.26, p_10.001, d=-1.12,$	t(35.47) = -1.44, $p = 0.156$, $d = -0.38$,
>	T=19, E=3, $\mu = 0.87$ (0.4 1.34)	$T=17, E=3, \mu = 1.01 (0.63 1.35)$	T=9, E=0, $\mu = -0.43$ (-0.8 0.01)	T=12, E=3, $\mu = -0.98$ (-1.44 -0.52)	T=3, E=0, $\mu = -0.37$ (-0.89 0.15)
ė	$t(29.91)=3.86, p_10.001, d=1.01,$	$U=674$, p $_{i}0.001$, d $=0.52$,	U=233, $p=0.003$, $d=0.38$,	$U=192, p_{1}0.001, d=0.47,$	U=325, p=0.142, d=0.19,
3	T=18, E=3, $\mu = 0.9$ (0.43 1.37)	T=17, E=3, $\mu = 1$ (0.59 1.35)	T=11, E=3, $\mu = -0.66$ (-1 -0.26)	T=14, E=3, $\mu = -0.87$ (-1.31 -0.46)	T=5, E=0, $\mu = -0.25$ (-0.64 0.08)
a	t(31.81)=2.97, p=0.004, d=0.78,	$U=690, p_{1}0.001, d=0.55,$	U=296, $p=0.054$, $d=0.25$,	U=215, $p=0.001$, $d=0.42$,	t(36.94)=-1.63, p=0.11, d=-0.43,
5	T=18, E=3, $\mu = 0.72$ (0.24 1.21)	T=15, E=3, $\mu = 0.83$ (0.53 1.14)	T=9, E=0, $\mu = -0.45$ (-0.88 0.01)	T=11, E=3, $\mu = -0.8$ (-1.22 -0.36)	T=7, E=0, $\mu = -0.42$ (-0.94 0.1)
i	t(33.07)=0.65, p=0.519, d=0.17,	U=527, p=0.098, d=0.22,	U=360, p=0.357, d=0.12,	U=207, p=0.001, d=0.44,	U=162, $p_{10.001}$, $d=0.53$,
<u>,</u>	T=3, E=0, $\mu = 0.17$ (-0.35 0.69)	T=4, E=0, $\mu = 0.41$ (-0.13 0.95)	T=0, E=0, $\mu = -0.13$ (-0.47 0.21)	T=15, E=3, $\mu = -0.72$ (-1.07 -0.36)	T=16, E=3, $\mu = -0.81$ (-1.28 -0.47)

Table A.11: Comparisons of the mean of adjacency matrix constructed with CS in epoch 2. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number of epochs where significant differences were observed (E), difference estimate μ with 95% confidence interval. Reliable differences (significant in all three epochs) are highlighted with bold text.

Frequency-band-	Test-	Difference-estimate-(95%-CI)-
α	U=313, p=0.122, d=0.22, E=1-	$\mu = -0.4 (-0.87 \cdot 0.09)$
β	U=225, $p=0.003$, $d=0.4$, $E=3$	$\mu = -0.73 (-1.23 - 0.25)$
δ	U=657, p;0.001, d=0.48, E=3	$\mu = 0.93 \cdot (0.46 \cdot 1.4)$
γ	t(32.53)=-1.53, p=0.132, d=-0.4, E=0-	$\mu = -0.4 \cdot (-0.93 \cdot 0.12)$
θ	t(36.34)=4.5, p;0.001, d=1.18, E=3	$\mu = 1.02 \cdot (0.56 \cdot 1.47)$

A.3 Results of statistical tests for epoch 2

In-this-section, we report the detailed results of the statistical comparisons accompanying the figures reported in the main text computed using only data from the second epoch. The comparisons of average coupling computed with CS and CBS are shown in Tables A.11 and A.12, respectively. The comparisons of node strength computed with CS and CBS are shown in Tables A.13 and A.14, respectively. Results of comparisons of the unweighted multilayer network metrics are reported in Tables A.15, A.16 and A.17 for edge betweenness, global vulnerability and local vulnerability, respectively. Results of comparisons of the weighted multilayer network metrics are reported vulnerability, respectively. Results of comparisons of the weighted multilayer network metrics are reported vulnerability, respectively. Results of comparisons of the weighted multilayer network metrics are reported vulnerability, respectively. Results of comparisons of the weighted multilayer network metrics are reported vulnerability, respectively. Results of comparisons of the weighted multilayer network metrics are reported vulnerability, respectively. Results of comparisons of the weighted multilayer network metrics are reported vulnerability, respectively. Results of comparisons of the weighted multilayer network metrics are reported vulnerability, respectively.

	δ	θ	σ	β	λ
4	t(35.95)=3.8, p=0.002, d=0.99,	$t(34.94) = 4.97, p_10.001, d=1.3,$	t(35.53) = 4.07, $p = 0.001$, $d = 1.06$,	t(36.46)=0.1, p=0.919, d=0.03,	U=386, p=0.688, d=0.07,
0	$E=2, -\mu = -0.89(0.42-1.36)$	$\mathbf{E}{=}3,\ \mu={1.09}(0.65\ 1.53)$	$E=3, \mu = 0.94(0.48 \ 1.41)$	$E=0.7\mu = -0.03(-0.5-0.55)$	$E=0, \gamma\mu = -0.12(-0.58-0.35)$
9	$t(35.54)=4.66, p_10.001, d=1.22, t(35.55)=3.77,$	t(35.55)=3.77, p=0.002, d=0.99,	t(32.41)=2.24, rp=0.049, rd=0.58,	t(35.24)=-1.53, p=0.193, d=-0.4,	U=347, p=0.343, d=0.15,
Р	$E=3, \ \mu=1.04(0.59\ 1.49)$	$E=3, \ \mu=0.89 (0.42 \ 1.36)$	$E=1, -\mu = -0.56(0.06-1.07)$	$E=1, -\mu = -0.4(-0.91-0.12)$	$E=1, 7\mu = -0.31(-0.79-0.17)$
	t(33.87)=3.92, p=0.002, d=1.02,	t(33)=2.65, p=0.02, d=0.69, d=0.66,	t(35.33)=-0.39, p=0.755, d=-0.1,	t(29.7)=-2.76, $p=0.017$, $d=-0.73$,	t(34.87)=-2.91, $p=0.013$, $d=-0.77$,
3	$E=2, \gamma\mu = -0.91(0.45-1.38)$	$E=1, \tau \mu = -0.66(0.16 \cdot 1.15)$	$E=1, \tau \mu = -0.1(-0.64, 0.43)$	$E=3, \mu = -0.69(-1.2, -0.19)$	$E=3, \ \mu=-0.72$ (-1.22 -0.22)
0	t(36.51)=-0.26, p=0.831, d=-0.07,	t(34.36)=-0.84, p=0.506, d=-0.22,	t(28.17)=-2.39, $p=0.038$, $d=-0.63$,	$ t(28.17) = -2.39, \ p = 0.038, \ d = -0.63, \ \ t(33.65) = -2.89, \ p = 0.013, \ d = -0.76, \ \ t(36.98) = -3.22, \ p = 0.008, \ d = -0.85, \$	t(36.98) = -3.22, $p = 0.008$, $d = -0.85$,
2	$E=0, \gamma\mu = -0.07(-0.6-0.46)$	$E=1, \mu = -0.22(-0.74 - 0.3)$	E=3, $\mu = -0.61(-1.12 - 0.1)$	E=3, $\mu = -0.72(-1.22 - 0.22)$	E=3, $\mu = -0.78(-1.27 - 0.3)$
	U=384, p=0.688, d=0.07,	t(36.82)=-1.32,7p=0.268,7d=-0.35,	t(34.36)=-2.88, p=0.013, d=-0.76, t(36.88)=-3.15, p=0.008, d=-0.83,	t(36.88) = -3.15, $p = 0.008$, $d = -0.83$,	U=301, p=0.101, d=0.24,
~	$E=0, \tau \mu = -0.13(-0.65 \cdot 0.31)$	$E=0, \tau \mu = -0.34(-0.86-0.18)$	E=3, $\mu = -0.72(-1.21 - 0.22)$	$E=3, \mu = -0.77(-1.25 - 0.28)$	$E=1, 7\mu = -0.52(-0.98-0.03)$

Table A.12: Comparisons of the mean of adjacency matrix constructed with CBS in epoch 2. The results are	reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric	Iternative), number of epochs where significant differences were observed (E), difference estimate μ with 95%	confidence interval. Reliable differences (significant in all three epochs) are highlighted with bold text.
Table A.	reported a	alternative	confidence

statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number Table A.13: Comparisons of node strength measured with CS in epoch 2. The results are reported as follows: of epochs where significant differences were observed (E), and difference estimate μ with 95% confidence interval (CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

		-		c	
cnannet	0	θ	σ	Ð.	k
F8-F4	t(36.8)=-3.65, p=0.001, d=-0.96,	t(36.25)=-4.24, pi0.001, d=-1.11,	t(34.7)=0.06, p=0.994, d=0.02,	t(36.3)=3.83, p=0.002, d=1.01,	U=557, $p=0.108$, $d=0.28$,
	$E=3, \mu = -0.87$ (-1.35 -0.39)	$\mathbf{E=3}, \ \mu = -0.97 \ (-1.43 \ -0.51)$	$E=0, \mu = 0.02 \ (-0.51 \ 0.54)$	$E=3, \mu = 0.91$ (0.43 1.38)	$E=0, \ \mu=0.6 \ (0.03 \ 1.16)$
F7-F3	$t(36.82) = -4.23, p_10.001, d = -1.11,$	t(32.41) = -3.79, $p = 0.001$, $d = -0.99$,	U=369, $p=0.625$, $d=0.1$,	t(36.88)=3.46, p=0.003, d=0.91,	U=586, $p=0.104$, $d=0.34$,
	$E=3, \mu = -0.97$ (-1.43 -0.51)	$E=3, \mu = -0.89$ (-1.36 -0.42)	$E=0, \mu = -0.25 (-0.77 \ 0.28)$	$E=3, \mu = 0.83$ (0.35 1.31)	$E=0, \mu = 0.71 (0.17 1.19)$
F4-C4	$t(36.76) = -4.36$, $p_{10.001}$, $d = -1.15$, $F = -3$, $u = -1$, t_{-1} , a_{R} , n_{RA})	t(36.35)=-4.39, pi0.001, d=-1.15, F-31 (-1 48 -0 FF)	t(36.42)=0.44, $p=0.848$, $d=0.11$, $F=0$, $\mu = 0.11$ (-0.41 0.64)	t(34.27)=3.9, p=0.002, d=1.03, F=3, 0.02, 0.05, 0.02	U=568, $p=0.108$, $d=0.3$, $E=0$, $u=0.56$ (0.08 1 12)
	$(\pm 0.00 - 0.1 \pm 0.001 \pm - 0.00)$				II-FEO
F3-C3	$t(36.86) = -3.4, p = 0.001, d = -0.89, E = 2, \mu = -0.82$ (-1.3 -0.34)	$f(36.2) = -4.77$, $p_{10.001}$, $d = -1.26$, $E = 3$, $\mu = -1.07$ (-1.52 -0.62)	$f(36.86)=0.01$, $p=0.994$, $d=0$, $E=0$, $\mu = 0$ (-0.53 0.53)	$t(28.26) = 4.39$, $p = 0.001$, $d = 1.16$, $E = 3$, $\mu = 1.01$ (0.55 1.48)	$U=589$, $p=0.104$, $d=0.35$, $E=0, \mu = 0.67$ (0.13 1.22)
	t(36.77)=-3.79, p=0.001, d=-0.99,	U=176, pi0.001, d=0.5,	U=416, $p=0.994$, $d=0.01$,	t(35.62)=2.66, $p=0.02$, $d=0.7$,	t(35.96) = 2.24, p = 0.108, d = 0.59,
F4-F2	$E=3, \ \mu = -0.89 \ (-1.37 \ -0.42)$	$E=3, \ \mu = -0.86$ (-1.33 -0.42)	$E=0, \ \mu = -0.01 \ (-0.44 \ 0.44)$	$E=3, \ \mu = 0.66 \ (0.16 \ 1.16)$	$E=0, \ \mu = 0.57 \ (0.06 \ 1.07)$
E7 C4	t(36.61)=-4.23, pi0.001, d=-1.11,	t(36.78)=-3.52, p=0.001, d=-0.92,	U=533, p=0.294, d=0.23,	U=610, $p=0.007$, $d=0.39$,	U=507, p=0.395, d=0.18,
F 2-02	$E=3, \mu = -0.98$ (-1.44 -0.51)	$E=3, \ \mu = -0.84$ (-1.32 -0.36)	$E=0, \ \mu = 0.44 \ (-0.04 \ 0.9)$	$E=2, \ \mu = 0.69 \ (0.24 \ 1.17)$	$E=0, \ \mu = 0.35 \ (-0.15 \ 0.86)$
	t(36.97)=-3.05, p=0.004, d=-0.8,	U=217, p=0.002, d=0.41,	U=421, p=0.994, d=0,	t(36.99)=2.6, p=0.021, d=0.68,	U=578, p=0.104, d=0.32,
F3-FZ	$E=3, \ \mu = -0.75 \ (-1.24 \ -0.26)$	$E=3, \ \mu = -0.75$ (-1.16 -0.32)	$E=0, \ \mu = 0 \ (-0.54 \ 0.52)$	$E=3, \ \mu = 0.65 \ (0.15 \ 1.15)$	$E=0, \ \mu = 0.63 \ (0.18 \ 1.18)$
č	$t(36.79) = -4.14$, $p_i 0.001$, $d = -1.08$,	t(31.35)=-4.21, pi0.001, d=-1.1,	U=545, $p=0.24$, $d=0.26$,	t(36.72)=2.31, p=0.032, d=0.61,	U=516, p=0.395, d=0.2,
1.4-C4	$E=3, \mu = -0.96$ (-1.42 -0.49)	$E=3, \mu = -0.96 (-1.42 - 0.5)$	$E=0, \ \mu = 0.47 \ (-0.01 \ 0.9)$	$E=2, \ \mu = 0.58 \ (0.08 \ 1.09)$	$E=0, \ \mu = 0.37 \ (-0.14 \ 0.87)$
e C E	t(34.89)=-4.41, pi0.001, d=-1.15,	t(31.3)=-3.33, $p=0.002$, $d=-0.87$,	t(36.43)=-0.02, p=0.994, d=0,	t(36.18)=3.63, p=0.002, d=0.95,	t(36.61)=2.24, p=0.108, d=0.59,
r ollo	$E=3, \ \mu = -1$ (-1.46 -0.55)	$E=3, \ \mu = -0.8 \ (-1.28 \ -0.32)$	$E=0, \ \mu = 0 \ (-0.53 \ 0.52)$	$E=3, \mu = 0.87 (0.39 1.35)$	$E=0, \mu = 0.57 (0.06 \ 1.07)$
	t(36.77)=-2.84, $p=0.006$, $d=-0.75$,	$t(36.9)=-4.08, p_i0.001, d=-1.07,$	U=498, $p=0.353$, $d=0.16$,	t(35.84)=2.34, $p=0.032$, $d=0.62$,	U=480, p=0.547, d=0.12,
C4-C2	$E=3, \mu = -0.7$ (-1.2 -0.21)	$E=3, \mu = -0.95$ (-1.41 -0.48)	$E=0, \ \mu = 0.31 \ (-0.19 \ 0.72)$	$E=3, \mu = 0.59 (0.09 1.1)$	$E=0, \ \mu = 0.26 \ (-0.26 \ 0.78)$
5	t(36.69)=-2.98, p=0.004, d=-0.78,	t(36.77)=-3.27, $p=0.002$, $d=-0.86$,	U=465, p=0.666, d=0.09,	t(35.91)=2.77, p=0.016, d=0.73,	U=512, p=0.395, d=0.19,
C3-C2	$E=3, \ \mu = -0.73 \ (-1.22 \ -0.24)$	$E=3, \mu = -0.79 (-1.28 - 0.31)$	$E=0, \ \mu = 0.15 \ (-0.35 \ 0.63)$	$E=3, \mu = 0.69 (0.19 1.19)$	$E=0, \ \mu = 0.36 \ (-0.11 \ 0.91)$
C7_D7	$t(37)=-4$, $p_{1}0.001$, $d=-1.05$,	t(35.55)=-4.88, p;0.001, d=-1.28,	t(36.91)=1.44, $p=0.299$, $d=0.38$,	U=638, $p=0.002$, $d=0.45$,	U=452, $p=0.687$, $d=0.07$,
	$\mathbf{E=3}, \ \mu = -0.93 \ (-1.4 \ -0.47)$	$E=3, \mu = -1.09 (-1.53 - 0.64)$	$E=0, \ \mu = 0.37 \ (-0.15 \ 0.89)$	$E=3, \mu = 0.84 (0.4 1.33)$	$E=0, \ \mu = 0.12 \ (-0.36 \ 0.47)$
μ μ	t(36.53)=-4.28, pi0.001, d=-1.13,	$t(36.78) = -5.04$, $p_10.001$, $d = -1.32$,	U=522, p=0.294, d=0.21,	t(30.59)=3.39, p=0.004, d=0.9,	U=457, $p=0.659$, $d=0.08$,
	$E=3, \mu = -0.99$ (-1.45 -0.52)	E=3, $\mu = -1.11$ (-1.55 -0.67)	$E=0, \ \mu = 0.42 \ (-0.1 \ 0.9)$	$E=3, \ \mu = 0.83 \ (0.34 \ 1.31)$	$E=0, \ \mu = 0.13 \ (-0.4 \ 0.52)$
C3 D3	$t(36.05) = -4.06, p_10.001, d = -1.06,$	t(36.78)=-5.16, pj0.001, d=-1.36,	t(36.98)=1.27, p=0.353, d=0.33,	t(30.61)=4.03, $p=0.002$, $d=1.07$,	U=480, $p=0.547$, $d=0.12$,
01-00	$E=3, \mu = -0.94 (-1.41 - 0.48)$	$E=3, \ \mu = -1.13$ (-1.56 -0.69)	$E=0, \ \mu = 0.33 \ (-0.19 \ 0.85)$	$E=3, \mu = 0.95 (0.48 1.42)$	$E=0, \ \mu = 0.18 \ (-0.27 \ 0.62)$
тт.	U=203, $p=0.001$, $d=0.44$,	t(35.99)=-4.05, pi0.001, d=-1.06,	U=522, $p=0.294$, $d=0.21$,	t(30.07)=1.5, p=0.153, d=0.4,	t(34.14)=0.62, p=0.659, d=0.16,
	$E=3, \mu = -1.05 (-1.57 - 0.45)$	$E=3, \mu = -0.94$ (-1.4 -0.47)	$E=0, \ \mu = 0.42 \ (-0.09 \ 0.86)$	$E=0, \ \mu = 0.39 \ (-0.13 \ 0.92)$	$E=0, \ \mu = 0.16 \ (-0.37 \ 0.7)$
Т3_Т5	t(36.03)=-3.71, $p=0.001$, $d=-0.97$,	t(36.81)=-4.3, p;0.001, d=-1.13,	U=499, $p=0.353$, $d=0.16$,	t(34.53)=2.8, p=0.016, d=0.74,	t(33.29)=0.93, p=0.547, d=0.25,
	$E=3, \mu = -0.88$ (-1.35 -0.4)	$E=3, \mu = -0.98 (-1.44 - 0.53)$	$E=0, \ \mu = 0.33 \ (-0.19 \ 0.81)$	$E=3, \mu = 0.7 (0.2 1.2)$	$E=0, \mu = 0.25 (-0.28 \ 0.78)$
P4-P7.	t(37)=-3.4, $p=0.001$, $d=-0.89$,	t(36.88)=-4.39, pj0.001, d=-1.15,	t(35.75)=1.51, p=0.299, d=0.39,	t(35.16)=2.48, $p=0.025$, $d=0.65$,	U=410, $p=0.923$, $d=0.02$,
1	$E=3, \mu = -0.82$ (-1.3 -0.34)	$\mathbf{E=3},\ \mu=-1$ (-1.46 -0.54)	$E=0, \ \mu = 0.39 \ (-0.13 \ 0.91)$	$E=3, \mu = 0.63$ (0.12 1.13)	$E=0, \ \mu = -0.03 \ (-0.58 \ 0.48)$
P3-PZ	U=180, pi0.001, d=0.49,	t(36.4)=-3.49, p=0.001, d=-0.92,	t(32.48)=1.7, p=0.294, d=0.44,	U=577, $p=0.023$, $d=0.32$,	U=469, $p=0.613$, $d=0.1$,
	$E=3, \mu = -1.1$ (-1.67 -0.61)	$E=3, \mu = -0.84$ (-1.31 -0.36)	$E=0, \ \mu = 0.44 \ (-0.08 \ 0.95)$	$E=3, \mu = 0.65$ (0.13 1.24)	$E=0, \mu = 0.14 (-0.35 0.56)$
$T_{6-0.2}$	U=194, $p=0.001$, $d=0.46$,	t(35.12)=-4.06, p ₁ 0.001, d=-1.06,	U=610, $p=0.063$, $d=0.39$,	t(36.92)=1.41, p=0.163, d=0.37,	U=324, $p=0.395$, $d=0.17$,
	$E=3, \mu = -1.09$ (-1.59 -0.52)	$E=3, \mu = -0.94 (-1.4 - 0.48)$	$E=0, \mu = 0.68 \ (0.29 \ 1.1)$	$E=0, \ \mu = 0.37 \ (-0.15 \ 0.89)$	$E=0, \ \mu = -0.25 \ (-0.63 \ 0.13)$
T5-01	t(30.73)=-4.33, pi0.001, d=-1.14,	t(34.14)=-3.45, p=0.001, d=-0.91,	t(32.43)=2.69, p=0.111, d=0.71,	t(32.71)=1.62, p=0.128, d=0.43,	U=369, $p=0.659$, $d=0.08$,
	$E=3, \mu = -0.99$ (-1.46 -0.53)	$E=3, \mu = -0.83$ (-1.32 -0.35)	$E=0, \ \mu = 0.67 \ (0.17 \ 1.17)$	$E=0, \mu = 0.42 \ (-0.1 \ 0.95)$	$E=0, \ \mu = -0.11 \ (-0.5 \ 0.25)$
P4-O2	U=191, $p=0.001$, $d=0.45$,	t(32.17)=-3.35, $p=0.002$, $d=-0.88$,	U=545, $p=0.151$, $d=0.29$,	U=540, $p=0.039$, $d=0.28$,	U=358, $p=0.613$, $d=0.1$,
	$E=3, \mu = -1.2$ (-1.59 -0.56)	$E=3, \mu = -0.81$ (-1.3 -0.33)	$E=0, \mu = 0.5 \ (0.04 \ 0.95)$	$E=3, \mu = 0.57 (0.07 \ 0.96)$	$E=0, \ \mu = -0.15 \ (-0.6 \ 0.22)$
P3-O1	U=189, $p=0.001$, $d=0.44$, $r=0.001$, $r=0.44$, $r=0.001$, $r=1.044$, $r=$	$t(35.98) = -4.04$, $p_10.001$, $d = -1.07$, r = 0.05, $t = 0.05$, $t = 0.0$	t(35.57)=1.48, p=0.299, d=0.39, p=0.39, p=0.29, p=0.39, p=0.	t(25.07)=2.35, $p=0.032$, $d=0.62$, $r=0.6$ (0.00, 1.10)	U=409, p=0.968, d=0.01, E-0 0.01 / 0.42 0.28)
	(-1, -1, -1, -1, -1, -1, -1, -1, -1, -1,			(777, 600) = 0.0 - 0.0 - 0.00	
01-02	$\mathbf{F}(33.25) = -3.72$, $\mathbf{p} = 0.001$, $\mathbf{q} = -1$, $\mathbf{E} = 3$. $u = -0.9$ (-1.39 -0.42)	$\mathbf{r}(33.89) = -4.4$, $\mathbf{p}[0.001, \mathbf{d} = -1.19, \mathbf{E} = 3, u = -1.03 (-1.49 - 0.56)$	r(34.89) = 2.31, $p = 0.151$, $d = 0.02$, E = 0, $u = 0.59$ (0.08 1.11)	t(29.08) = 1.40, $p = 0.108$, $d = 0.39$, E = 0. u = 0.39 (-0.15 0.92)	U=314, $p=0.393$, $q=0.17$, $E=0. u = -0.2 (-0.6 0.12)$
_					

Table A.14: Comparisons of node strength measured with CBS in epoch 2. The results are reported as follows: statistics value (degrees of freedom). p-value of the test. Cohen's d effect size (or nonparametric alternative). number
of epochs where significant differences were observed (E), and difference estimate μ with 95% confidence interval
(CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

from	n channel	Ş	θ	σ	β	~
Ş	F8-F4	U=238, p=0.005, d=0.37, E=2, μ =-0.73 (-1.25 -0.23)	t(36.72)=-3.87, p;0.001, d=- 1.01, E=3, μ =-0.91 (-1.38 - 0.44)	t($(35.73)=-2.77$, p=0.008, d=-0.73, E=2, μ =-0.69 (-1.18 -0.19)	U=413, p=0.982, d=0.01, E=0, μ =-0.01 (-0.45 0.39)	U=519, p=0.715, d=0.2, E=0, μ =0.34 (-0.13 0.71)
δ	F7-F3	U=224, p=0.003, d=0.4, E=3, μ =-0.77 (-1.27 -0.32)	$t(36.93) = -3.82$, $p_i 0.001$, $d=-1$, $E=3$, $\mu = -0.9$ (-1.37 -0.43)	t(36.92)=-3.8, p=0.001, d=-1, E=2, $\mu = -0.9 (-1.37 - 0.42)$	U=393, p=0.982, d=0.06, E=0, μ =-0.11 (-0.48 0.49)	U=511, p=0.715, d=0.19, E=0, μ =0.2 (-0.08 0.44)
8	F4-C4	U=227, p=0.003, d=0.39, E=3, μ =-0.8 (-1.19 -0.37)	U=152, pi0.001, d=0.55, E=3, μ =-1.16 (-1.58 -0.66)	t((32.42)=-4.89, pi0.001, d=- 1.29, E=3, μ =-1.09 (-1.54 - 0.64)	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$ \begin{array}{llllllllllllllllllllllllllllllllllll$
δ	F3-C3	U=198, p=0.001, d=0.45, E=2, μ =-0.82 (-1.16 -0.41)	t(36.6)=-5, p;0.001, d=-1.31, E=3, μ =-1.1 (-1.54 -0.66)	t(36.22)=-4.03, p=0.001, d=-1.06, E=2, μ =-0.94 (-1.41 -0.47)	U=418, p=0.982, d=0, E=0, $\mu = 0$ (-0.5 0.43)	U=480, p=0.746, d=0.12, E=0, $\mu = 0.08 (-0.07 \ 0.26)$
δ	F4-FZ	U=198, p=0.001, d=0.45, E=2, μ =-0.89 (-1.36 -0.45)	$t(33.13)=-3.8$, $p_{10}.001$, $d=-$ 0.99, $E=3$, μ =-0.89 (-1.36 -0.42)	t(34.81)=-3.66, p=0.001, d=-0.96, E=2, μ =-0.87 (-1.34 -0.39)	$\begin{array}{llllllllllllllllllllllllllllllllllll$	U=524, p=0.715, d=0.21, E=0, μ =0.14 (-0.04 0.23)
8	FZ-CZ	U=199, p=0.001, d=0.45, E=3, $\mu = -0.81$ (-1.23 -0.41)	t (35.9)=-4.23, pl0.001, d=- 1.11, E=3, μ =-0.98 (-1.44 -0.51)	t(35.39)=-3.98, p=0.001, d=-1.05, E=2, μ =-0.93 (-1.4 -0.46)	U=417, p=0.982, d=0.01, E=0, μ =-0.02 (-0.5 0.39)	U=514, p=0.715, d=0.19, E=0, μ =0.06 (-0.03 0.18)
Ş	F3-FZ	t(37)=-3.51, p=0.002, d=-0.92, E=3, μ =-0.84 (-1.32 -0.36)	t(35.14)=-3.36, p=0.001, d=- 0.88, E=3, μ =-0.81 (-1.29 - 0.33)	t($(36.97)=-3.65$, $p=0.001$, $d=-$ 0.96, $E=3$, μ =-0.87 (-1.34 - 0.39)	U=417, p=0.982, d=0.01, E=0, μ =-0.01 (-0.44 0.4)	U=468, p=0.862, d=0.1, E=0, $\mu = 0.07 (-0.12 \ 0.2)$
s s	T4-C4	U=176, p=0.001, d=0.5, E=3, μ =-0.94 (-1.36 -0.49) 11-201 s-0 000 d-0 44 E-3	$t(36.75) = -4.36$, $p_{1}0.001$, $d = -1.15$, $E = 3$, $\mu = -1$ (-1.46 - 0.54) t(27) = -4 $t = 7$ = 0.01 $4 = -1$ 1 22	$ \begin{array}{c} t(36.44) = -3.22, p = 0.004, d = -0.84, \\ E = 1, \mu = -0.78 \ (-1.27 \ -0.29) \\ + (25 \ 81) - 2 \ 4 2 \ -0.000 \ -0.000 \ -0.00 \end{array} $	U=418, p=0.982, d=0, E=0, μ =- 0.01 (-0.38 0.36) 11-2470.8580.15 E-0	d=0.09, () d=0.14
s s	C4-CZ	U = 204, $p = 0.002$, $q = 0.44$, $k = 3$, $\mu = -0.94$ (-1.49 -0.39) t(35.74) = -2.24, $p = 0.029$, $d = -$.2, .34) 0.34	d=0.15, 8) d=0.12,	U = 490, $p = 0.715$, $q = 0.14$, $E = 0$, $\mu = 0.08 (-0.06 0.21)$ U = 504, $p = 0.715$, $d = 0.17$, $E = 0$,
Ś	C3-CZ	0.59, E=3, μ =-0.57 (-1.08 - 0.06) 0.06) t(35.77)=-3.17, p=0.003, d=-	E =3, μ =-0.85 (-1.33 -0.37) t(36.74)=-3.42, p=0.001, d=-0.9,	$\mu =$ -0.66 (-1.14 -0.18) t((35.57) = -2.79, p=0.008, d=-0.73, t(35.57) = -2.79, p=0.008, d=-0.73, t(35.57) = -2.79, t($\mu = 0.23 \ (-0.22 \ 0.67)$ $U = 446, D = 0.982, d = 0.05, E = 0.$	$\mu = 0.07 \ (-0.04 \ 0.2)$ $U = 490, p = 0.715, d = 0.14, E = 0,$
		0.83, $\vec{E}=3$, μ =-0.78 (-1.27 - 0.28)	(-1.31 -0.34)	$E=1, \mu =-0.69$ (-1.18 -0.19)	(-0.32 0.61)	(-0.05 0.2)
8	CZ-PZ	U=198, p=0.001, d=0.45, E=3, $\mu =$ -0.85 (-1.29 -0.35)	t(35.98)=-6.3, p:0.001, d=- 1.66, E=3, μ =-1.28 (-1.69 -0.87)	$t(35.45)=-4.18$, $p=0.001$, $d=-1.1$, $E=3$, $\mu=-0.97$ (-1.44-0.5)	U=439, p=0.982, d=0.04, E=0, μ =0.08 (-0.49 0.63)	U=438, p=0.905, d=0.04, E=0, $\mu = 0.02 (-0.09 \ 0.15)$
8	C4-P4	U=231, p=0.003, d=0.39, E=3, μ =-0.71 (-1.08 -0.28)	t(36.65)=-5.29, pi0.001, d=- 1.39, E=3, μ =-1.15 (-1.58 - 0.71)	t (36.68)=-4.07, p=0.001, d=-1.07, E=2, μ =-0.95 (-1.41 -0.48)	U=450, p=0.982, d=0.06, E=0, μ =0.09 (-0.36 0.59)	U=393, p=0.905, d=0.06, E=0, μ =-0.04 (-0.29 0.23)

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	C3-P3	U=207, p=0.002, d=0.44, E=3,	U=151, p _i 0.001, d=0.55, E=3,	t(36.61)=-3.86, p=0.001, d=-1.01,	U=426, $p=0.982$, $d=0.01$, $E=0$,	U=417, p=0.969, d=0.01, E=0,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.81 (-1.34 -0.38)		Ħ	=0.02	$\mu = 0 \ (-0.32 \ 0.33)$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	T4-T6		pi0.001,	t(36.03)=-3.01, p=0.005, d=-0.79,	p=0.982, d=0.08,	U=395, $p=0.905$, $d=0.05$, $E=0$,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			$\mu=$ -0.98 (-1.36 -0.56)	E=3, μ =-1.01 (-1.46	E=2, μ =-0.74 (-1.23 -0.25)	$\mu =$ -0.11 (-0.49 0.28)	μ =-0.02 (-0.16 0.1)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$							
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	T3-T5		(8)=-3.79, p;0.001,	p=0.008,	p=0.695, d=0.21,	U=444, $p=0.905$, $d=0.05$, $E=0$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.76 (-1.11 -0.31)	E=3, μ	E=1, μ =-0.69 (-1.19 -0.2)	$\mu =$ -0.27 (-0.61 0.11)	$\mu = 0.02 \; (-0.12 \; 0.16)$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	P4-PZ	_	pi0.001,	t(36.59)=-3.64, p=0.001, d=-0.95,	p=0.982, d=0.02,	U=432, $p=0.937$, $d=0.02$, $E=0$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.83 (-1.27 -0.38)	E=3, $\mu = -$	=-0.86 (-1.34	=0.03	$\mu = 0.01 \; (-0.11 \; 0.15)$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	P3-PZ		p;0.001,	t(31.72)=-3.03, $p=0.005$, $d=-0.79$,	p=0.982, d=0.01,	U=411, p=0.937, d=0.02, E=0,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.87 (-1.27 -0.29)	=-0.97 (-1.43	E=1, μ =-0.74 (-1.22 -0.25)	$\mu = -0.02 \ (-0.35 \ 0.36)$	μ =-0.01 (-0.1 0.09)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$				0.51)			
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	T6-O2		p=0.004,	p=0.008, d=0.35,	p=0.695, d=0.2, E=0, μ	U=382, $p=0.862$, $d=0.08$, $E=0$,
			μ =-0.72 (-1.12 -0.33)	E=2, μ =-0.73 (-1.22 -0.24)	(-1.01)	0.2 (-0.46 0.09)	$\mu = -0.03 \; (-0.12 \; 0.08)$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	T5-O1		(3) = -3.6, p = 0.001,	t(34.35)=-3.11, $p=0.005$, $d=-0.81$,	p=0.695, d=0.22,	U=354, $p=0.715$, $d=0.13$, $E=0$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.76 (-1.17 -0.3)	$E=3, \mu =-0.86$ (-1.34)	E=2, μ =-0.76 (-1.24 -0.27)	$\mu = -0.27 \ (-0.56 \ 0.07)$	μ =-0.04 (-0.12 0.05)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$				0.38)			
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	P4-O2		03)=-4.77, pi0.001, d	p=0.008,	p=0.858, d=0.15,	U=400, $p=0.905$, $d=0.04$, $E=0$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.9 (-1.37 -0.44)	E=3, μ =-1.06 (-1.51	=-0.71	$\mu = -0.22 \ (-0.54 \ 0.18)$	μ =-0.01 (-0.09 0.06)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$				0.62)			
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	P_{3-01}		pi0.001,		p=0.695, d=0.21,	U=379, $p=0.862$, $d=0.08$, $E=0$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.7 (-1.12 -0.31)	E=3, μ =-0.95 (-1.42	E=2, μ =-0.81 (-1.29 -0.33)	$\mu = -0.29 \ (-0.6 \ 0.09)$	$\mu =$ -0.02 (-0.09 0.05)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$				0.49)			
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	δ	01-02		ഥ	p;0.001,	p=0.695, d=0.19,	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-0.9 (-1.37 -0.44)	μ =-1.32 (-1.76 -0.86)	E=3, $\mu = -1.09$ (-1.54	$\mu = -0.25 (-0.77 0.1)$	μ =-0.04 (-0.12 0.05)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	θ	F8-F4		p=0.008, d		p=0.716, d=0.1,	
			E=3, μ =-0.88 (-1.36	E=3, μ =-0.72 (-1.21	E=0, μ =-0.53 (-1.04 -0.03)		μ =0.39 (-0.11 0.81)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$				0.23)			
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	θ	F7-F3		9)=-2.94, p=0.008,	t(35.49)=-2.15, $p=0.083$, $d=-0.56$,	p=0.926,	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			E=3, μ =-0.95 (-1.41	E=3, μ =-0.72 (-1.22	E=0, μ =-0.54 (-1.05 -0.04)		μ =0.43 (-0.1 0.94)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			0.49)				
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	θ	F4-C4	U=144, pi0.001, d=0.56, E=3,	2)=-4.24, p=0.001,	t(36.53) = -3.47, $p = 0.024$, $d = -0.91$,	p=0.926,	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			μ =-1.22 (-1.58 -0.72)	E=3, μ =-0.98 (-1.44	E=1, μ =-0.83 (-1.31 -0.35)	$E=0, \ \mu=0.08 \ (-0.45 \ 0.61)$	$\mu = 0.36 \; (0.03 \; 0.66)$
F3-C3 t(36.96)=-4.95, pi0.001, d=- t(35.37)=-4.58, p=0.001, d=- t(36.98) =-2.77, p=0.08, d=-0.73, p=0.73, p=0.716, q=0.19, 0=0.34 0.25 1.3, E=3, μ =-1.09 (-1.54 - 0.65) 1.21, E=3, μ =-1.04 (-1.49 - E=0, μ =0.69 (-1.18 - 0.19) E=0, μ =0.73, p=0.716, q=0.19, μ μ =0.25 1.3, E=3, μ =-1.09 (-1.54 - 0.65) 1.21, E=3, μ =-1.04 (-1.49 - E=0, μ =0.69 (-1.18 - 0.19) E=0, μ =0.73 μ =0.25 74-FZ t(29.34)=-3.71, p=0.001, d=- (1.58) (-1.32 - 1.03, d=0.73) μ =0.26 μ =0.25, p=0.654, d=-0.77, t(32.83)=0.76, p=0.716, d=0.2, 0.72) μ =0.26 0.97, E=3, μ =-0.87 (-1.34 - 0.4) 0.93, E=3, μ =-0.84 (-1.32 - 1.32 - 1.21 - 0.23) E=0, μ =0.2 (-0.32 0.72) μ =0.44	4	č p				0 1 0	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	θ	F3-C3		$(7) = -4.58$, $p = 0.001$, $d = \frac{1}{2}$	t(36.95) = -2.77, $p = 0.058$, $d = -0.73$,	p=0.716,	U=533, p=0.322, d=0.23, E=0,
$ F4-FZ t(29.34)=-3.71, \ p=0.001, \ d=- t(38.35)=-3.53, \ p=0.003, \ d=- t(34.01)=-2.95, \ p=0.054, \ d=-0.77, \ t(32.83)=0.76, \ p=0.716, \ d=-0.2, \ U=607, \ u=0.27, \ u=$			1.3, $\mathbf{L}=3$, $\mu =-1.09$ (-1.34 -0.09)	$\mathbf{r}=3, \ \mu = -1.04 \ (-1.49)$	$\mu = 0, \mu = -0.09$ (-1.18 -0.19)	$E=0, \mu = 0.13 (-0.54 0.73)$	$(ac.0 z 0.0-) cz.0 = \pi$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$,						
0.36)	θ	F4-FZ		$55) = -3.53$, $p = 0.003$, $d = E = 3$, $\mu = -0.84$ (-1.32)	t(34.01)=-2.95, p=0.054, d=-0.77, E=0, μ =-0.72 (-1.21 -0.23)	$p=0.716, 0.32 \ 0.72)$	U=607, p=0.074, d=0.38, E=0, $\mu = 0.44 \ (0.16 \ 0.67)$
				0.36)			

$ \begin{array}{llllllllllllllllllllllllllllllllllll$		54105	51 50		uca		5 10	геро	- CII 4							-
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	d=0.19,	p=0.322, d=0.23, (-0.03 0.58)	d=0.12,	d=0.32,	d=0.21,	p=0.799, d=0.09, (-0.19 0.34)	d=0.1,		d=0.03,	d=0.04,	d=0.21,	p=0.982, d=0.01, (-0.31 0.33)	p=0.967, d=0.04, (-0.19 0.31)	p=0.799, d=0.09, 5 (-0.29 0.14)	U=367, p=0.77, d=0.11, E=0, μ =-0.06 (-0.23 0.1)	d=0.02, 5)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	p=0.926, (-0.44 0.62)	p=0.982, (-0.5 0.55)	, d=0,		\sim		p=0.146, (0.07 1.09)			p=0.146, (0.08 1.09)	d=0.08,	p=0.56, (-0.2 0.84)	p=0.146, d=0.3, (0.08 1.01)	p=0.56, d=0.15, (-0.17 0.68)	d=0.15,	p=0.483, d=0.19, (-0.11 0.74)
FZ-CZ t(36.18)=-3.6, p=0.003, d=-0.35 129, E=3, μ =-1.09 (-1.53 E=2, μ =0.56 (-1.34-0.38) 129, E=3, μ =-1.09 (-1.53 E=2, μ =0.56 (-1.34-0.38) 131 T4-C4 t(31.27)=-2.15, p=0.003, d=-0.75 0.41 0.99, E=3, μ =-0.89 (-1.36 0.66, E=3, μ =0.53 0.41 0.41 D=0.003, d=-0.77 11.8, E=3, μ =-1.02 (-1.48 E=2, μ =0.71 (-12.0.22) 0.41 E=3, μ =0.001, d=-1.14, t(36.92)=-2.91, p=0.008, d=-0.77 11.8, E=3, μ =-0.86 (-1.45.0.54) E=2, μ =0.71 (-12.0.22) 0.57 2.515 =0.014 d=-0.71 11.8, E=3, μ =-0.86 (-1.45.0.53) E=2, μ =0.07 0.515 E=3, μ =-0.60 d=-0.75 0.515 E=3, μ =-0.61 d=-0.75 0.515 E=3, μ =-0.60 d=-0.75 0.515 E=3, μ =-0.61 d=-0.75 0.515 E=3, μ =-0.60 d=-0.75 0.55 E=2, μ =0.01 d=-0.75 0.55 E=2, μ =0.02 d=-0.75 0.56 E=2, μ =0.02 d=-0.75 0.515 E=2, μ =0.03 d=-0.75 </td <th>p=0.061, 51 (-1.12 -0.11</th> <td>p=0.083, (-1.03 -0.02</td> <td>$t(27.44)=-2.56$, $p=0.061$, $d=-0.67$, $E=0, \mu =-0.63$ (-1.13 -0.13)</td> <td>t(36.99)=-2.1, p=0.083, d=-0.55, E=0, μ =-0.53 (-1.05 -0.02)</td> <td>LO LO</td> <td>t(31.15)=-2.43, p=0.061, d=-0.64, E=0, μ =-0.61 (-1.11 -0.11)</td> <td>$t(36.91)=-1.86$, $p=0.121$, $d=-0.49$, $E=0$, $\mu =-0.48$ (-0.99 0.04)</td> <td>p=0.266, 3 (-0.85 0.19)</td> <td>t(34.92)=-1.31, p=0.266, d=-0.34, E=0, μ =-0.34 (-0.87 0.18)</td> <td>t(33.29)=-0.92, p=0.377, d=-0.24, E=0, μ =-0.24 (-0.76 0.28)</td> <td>p=0.19, .91 0.12)</td> <td>=0.31,</td> <td>p=0.301, 0.82 0.22)</td> <td>6</td> <td></td> <td></td>	p=0.061, 51 (-1.12 -0.11	p=0.083, (-1.03 -0.02	$t(27.44)=-2.56$, $p=0.061$, $d=-0.67$, $E=0, \mu =-0.63$ (-1.13 -0.13)	t(36.99)=-2.1, p=0.083, d=-0.55, E=0, μ =-0.53 (-1.05 -0.02)	LO LO	t(31.15)=-2.43, p=0.061, d=-0.64, E=0, μ =-0.61 (-1.11 -0.11)	$t(36.91)=-1.86$, $p=0.121$, $d=-0.49$, $E=0$, $\mu =-0.48$ (-0.99 0.04)	p=0.266, 3 (-0.85 0.19)	t(34.92)=-1.31, p=0.266, d=-0.34, E=0, μ =-0.34 (-0.87 0.18)	t(33.29)=-0.92, p=0.377, d=-0.24, E=0, μ =-0.24 (-0.76 0.28)	p=0.19, .91 0.12)	=0.31,	p=0.301, 0.82 0.22)	6		
FZ-CZ t(36.97)=-4.93, pi0.001, 0.65) t= -1.09 (-1. $129, E=3, \mu = -1.09$ (-1. 0.65 t(33.07)=-3.78, p=0.001, 0.99, E=3, $\mu = -0.89$ (-1. $118, E=3, \mu = -0.89$ (-1. (0.41) (1.8, E=3, $\mu = -0.84$ $1.18, E=3, \mu = -0.99$ (-1.45, -0.54) (0.57) (-1.45, -0.54) $1.18, E=3, \mu = -0.99$ (-1.45, -0.54) (-1.29, -0.54) (-1.29, -0.54) $1.3, E=3, \mu = -0.99$ (-1.45, -0.54) (-1.29, -0.51) (-1.29, -0.54) $2.3-CZ$ $(235.15)=-3.35, p=0.001, d=-3.42) (-1.29, -0.01) (-1.20, -0.01) C-4-CZ (235.15)=-3.35, p=0.001, d=-3.42) (-1.26, -0.24) (-1.26, -0.24) C-4-CZ (235.15)=-3.35, p=0.001, d=-3.42) (-1.26, -0.24) (-1.26, -0.24) C-2-PZ (235.29)=-5.67, p_10.001, d=-3.42) (-1.26, -0.24) (-1.26, -0.24) C-2-PZ (23.82)=-5.67, p_10.001, d=-3.42) (-1.26, -0.24) (-1.26, -0.24) C-2-PZ (23.82)=-5.67, p_10.001, d=-3.42) (-1.26, -0.24) (-1.26, -0.24) C-2-PZ (23.82)=-2.96, p=-0.08, (-1.26, -0.24) (-1.26, -0.24) $		(7) = -2.15, p=0.036, d= E=3, $\mu = -0.54$ (-1.05	.008, -0.22)	$t(36.92)=-2.91$, p=0.008, d=-0.76, E=2, μ =-0.72 (-1.21 -0.22)	$t(35.78)=-2.63, p=0.012, d=-0.69, E=2, \mu =-0.65 (-1.15 -0.16)$	t (32.08)=-2.73, p=0.01, d=-0.71, E=2, μ =-0.67 (-1.17 -0.18)	U=199, p=0.002, d=0.45, E=3, μ =-0.86 (-1.29 -0.38)	5)=-3.19, p=0.006, d= E=3, μ =-0.78 (-1.27	t(30.94)=-3.26, p=0.006, d=- 0.86, E=3, μ =-0.8 (-1.29 -0.31)	$\begin{array}{llllllllllllllllllllllllllllllllllll$		d= 39	t (32.17)=-2.74, p=0.01, d=-0.72, E=2, μ =-0.68 (-1.17 -0.18)	t(36.57)=-2.97, p=0.008, d=-0.78, E=2, μ =-0.73 (-1.22 -0.24)	t(36.49)=-2.92, p=0.008, d=-0.76, E=2, μ =-0.72 (-1.21 -0.22)	t(36.89)=-2.61, p=0.012, d=-0.69, E=2, μ =-0.65 (-1.15 -0.15)
	p;0.001, =-1.09 (-1.	(7) = -3.78, p=0.001, d= E=3, μ =-0.89 (-1.36	p;0.001, <i>i</i> =-1.02	t(37)=-4.34, p;0.001, d=-1.14, E=3, μ =-0.99 (-1.45 -0.54)	t(35.15)=-3.35, p=0.002, d=- 0.88, E=3, μ =-0.8 (-1.29 -0.32)	t(35.99)=-3.73, p=0.001, d=- 0.98, E=3, μ =-0.88 (-1.35 - 0.41)	pi0.001, 2 (-1.63 -0.		1)=-4.82, p _i 0.001, d= E=3, μ =-1.08 (-1.53		U=232, p=0.003, d=0.38, E=3, μ =-0.83 (-1.34 -0.34)	pi0.001, =-1.02 (-1.	$\begin{array}{llllllllllllllllllllllllllllllllllll$		U=200, p=0.001, d=0.45, E=3, μ =-1.02 (-1.47 -0.41)	pi0.001, .96 (-1.42 -
φ φ	FZ-CZ	F3-FZ	T4-C4	T3-C3		C3-CZ	CZ-PZ	C4-P4	C3-P3	T4-T6	$T_{3}-T_{5}$	P4-PZ	P3-PZ	T6-02	T5-01	P4-02
	θ	θ	θ	θ	θ	θ	θ	θ	θ	θ	θ	θ	θ	θ	θ	θ

θ	P3-01	t(36.88)=-3.74, p=0.001, d=-	t(36.73)=-3.19, p=0.006, d=-0.84,	t(36.9)=-1.13, p=0.302, d=-0.3,	t(29.51)=2, p=0.235, d=0.52, E=0,	U=425, $p=0.982$, $d=0.01$, $E=0$,
		0.98, E=3, μ =-0.88 (-1.36 -		$(-0.82 \ 0.23)$	$\mu = 0.5 \ (0 \ 1.01)$	(1
		0.41)				
θ	01-02	t(36.29)=-3.87, p=0.001, d=-	t(36.95)=-3.05, p=0.008, d=-	t(33.7)=-1.61, p=0.187, d=-0.42,	U=509, $p=0.489$, $d=0.18$, $E=0$,	U=392, $p=0.965$, $d=0.06$, $E=0$,
		1.01, E=3, μ =-0.91 (-1.38 -	0.8, E=3, μ =-0.75 (-1.24 -0.26)	E=0, μ =-0.41 (-0.93 0.1)	$\mu = 0.28 \ (-0.15 \ 0.86)$	μ =-0.03 (-0.25 0.17)
ė	то 170		2 0 0 7 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	11-271 708 4 1 E	*/36 86)	11E800 00E -10 33 E0
3	# 1_0 1	$E=2$. $\mu =-0.81$ (-1.29 -0.33)	p=0.03, (-1.16 -0.17)	0.19 (-0.67 0.35)		p-0.029, u-0.33, (0.11 0.9)
σ	F7-F3	t(36.66)=-3.96, p=0.001, d=-1.04,	t(35.07) = -3.26, $p = 0.015$, $d = -0.85$,	t(32.72)=-1.69, $p=0.791$, $d=-0.44$,	t(36.34)=1.23, p=0.244, d=0.32,	=585,
		E=2, μ =-0.92 (-1.39 -0.46)	Ŀ	E=0, μ =-0.44 (-0.96 0.08)	Ŀ	$\mu = 0.43 \ (0.11 \ 0.76)$
σ	F4-C4	$t(32.9)=-4.25, p_10.001, d=-1.12,$	t(36.6)=-3.38, $p=0.015$, $d=-0.89$,	U=416, $p=0.957$, $d=0.01$, $E=0$,	t(29.02)=1.31, p=0.227, d=0.35,	U=669, $p=0.001$, $d=0.51$, $E=3$,
		E=2, μ =-0.98 (-1.45 -0.52)	E=1, μ =-0.82 (-1.3 -0.33)	$\mu = -0.02 \ (-0.48 \ 0.48)$	E=0, $\mu = 0.35$ (-0.19 0.88)	$\mu=$ 0.66 (0.38 1.01)
σ	F3-C3	$t(36.94)=-4.23, p_i0.001, d=-1.11,$	t(36.72)=-3.46, p=0.015, d=-0.91,	U=394, $p=0.798$, $d=0.05$, $E=0$,	U=563, $p=0.049$, $d=0.29$, $E=3$,	U=670, $p=0.001$, $d=0.51$, $E=3$,
		E=2, μ =-0.98 (-1.44 -0.51)	E=1, μ =-0.83 (-1.31 -0.35)	μ =-0.12 (-0.58 0.37)	$\mu=$ 0.55 (0.05 0.99)	$\mu=$ 0.71 (0.33 0.99)
σ	F4-FZ	t(34.65)=-3.21, p=0.005, d=-0.84,	t(35.75)=-2.96, $p=0.021$, $d=-0.77$,	t(35.7)=-0.93, p=0.798, d=-0.24,	t(37)=1.76, $p=0.102$, $d=0.46$, $E=0$,	U=634, $p=0.005$, $d=0.44$, $E=3$,
		E=2, μ =-0.78 (-1.26 -0.29)	E=1, μ =-0.72 (-1.22 -0.23)	E=0, μ =-0.24 (-0.77 0.28)	$\mu = 0.45 \ (-0.06 \ 0.97)$	$\mu=$ 0.57 (0.25 0.91)
σ	FZ-CZ	$t(36.99)=-4.56, p_i0.001, d=-1.2,$	t(36.73)=-2.88, $p=0.022$, $d=-0.76$,	U=448, $p=0.798$, $d=0.06$, $E=0$,	t(29.42)=1.16, $p=0.263$, $d=0.31$,	U=582, $p=0.025$, $d=0.33$, $E=3$,
		E=1, μ =-1.03 (-1.48 -0.58)	E=1, μ =-0.71 (-1.21 -0.22)	$\mu = 0.08 \ (-0.38 \ 0.55)$	E=0, $\mu = 0.31$ (-0.23 0.84)	$\mu=$ 0.38 (0.1 0.69)
σ	F3-FZ	t(37)=-3.81, p=0.001, d=-1, E=1,	t(32.09)=-1.86, p=0.087, d=-0.49,	t(36.83)=-1.23, p=0.791, d=-0.32,	t(36.84)=0.87, p=0.386, d=0.23,	U=600, p=0.021, d=0.37, E=3,
		$\mu = -0.9 \ (-1.37 \ -0.43)$	E=0, μ =-0.47 (-0.98 0.04)	$E=0, \ \mu =-0.32 \ (-0.84 \ 0.2)$	E=0, $\mu = 0.23$ (-0.3 0.76)	$\mu=$ 0.52 (0.16 0.89)
σ	T4-C4	t(32.64)=-2.88, p=0.008, d=-0.75,	t(26.92)=-2.19, p=0.059, d=-0.57,	t(36.83)=-0.16, $p=0.913$, $d=-0.04$,	U=547, $p=0.072$, $d=0.26$, $E=0$,	U=576, $p=0.025$, $d=0.32$, $E=2$,
			E=0, μ =-0.55 (-1.05 -0.05)	E=0, μ =-0.04 (-0.57 0.49)	$\mu = 0.45 \ (0.01 \ 0.94)$	$\mu = 0.35 \ (0.08 \ 0.64)$
σ	T3-C3	t(35.81)=-3.05, p=0.007, d=-0.8,	t(36)=-2.65, $p=0.03$, $d=-0.69$, $E=1$,	t(31.98)=-0.65, $p=0.798$, $d=-0.17$,	U=560, $p=0.052$, $d=0.29$, $E=0$,	U=626, $p=0.006$, $d=0.42$, $E=2$,
		E=1, μ =-0.75 (-1.24 -0.26)	μ =-0.66 (-1.16 -0.16)	$E=0, \mu =-0.17 (-0.71 \ 0.36)$	$\mu = 0.6 \ (0.08 \ 1.04)$	$\mu = 0.6 \ (0.22 \ 0.95)$
σ	C4-CZ	t(34.74)=-2.36, $p=0.024$, $d=-0.62$,	t(35)=-2.57, $p=0.03$, $d=-0.67$, $E=1$,	U=404, $p=0.888$, $d=0.03$, $E=0$,	U=546, $p=0.072$, $d=0.26$, $E=0$,	U=575, $p=0.025$, $d=0.32$, $E=2$,
			μ =-0.64 (-1.14 -0.14)	5 (-0.48 0.37)	$\mu = 0.45 \ (-0.02 \ 0.85)$	$\mu = 0.36 (0.06 0.68)$
σ	C3-CZ	t(35.69)=-2.89, $p=0.008$, $d=-0.76$,	t(29.85)=-2.29, p=0.055, d=-0.6,	U=477, $p=0.798$, $d=0.12$, $E=0$,	t(32.74)=2.09, $p=0.068$, $d=0.55$,	U=594, $p=0.024$, $d=0.36$, $E=2$,
		E=1, μ =-0.71 (-1.2 -0.22)	E=0, μ =-0.57 (-1.08 -0.07)	$\mu = 0.19 \ (\text{-}0.3 \ 0.54)$	E=0, $\mu = 0.54 (0.02 \ 1.05)$	μ =0.5 (0.18 0.9)
σ	CZ-PZ	$t(36.56)=-4.71, p_i0.001, d=-1.24,$	t(36.45)=-2.6, p=0.03, d=-0.68,	U=491, $p=0.791$, $d=0.15$, $E=0$,	t(23.71)=2.68, p=0.024,	U=577, $p=0.025$, $d=0.32$, $E=3$,
		E=2, μ =-1.06 (-1.51 -0.61)	E=1, μ =-0.65 (-1.15 -0.15)	$\mu = 0.24 \; (-0.22 \; 0.72)$	$d=0.71, E=3, \mu = 0.68 (0.17$	$\mu=$ 0.45 (0.12 0.76)
			0100			0000 1 1010
σ	C4-P4	$t(36.53) = -4.43, p_i 0.001, d = -1.16, $	t(35.3) = -2.02, $p = 0.076$, $d = -0.53$,		=3.46, T	
		$E=2, \mu =-1.01 (-1.46 -0.55)$	$E=0, \mu = -0.51 (-1.02 0)$	$\mu = 0.39 \ (-0.14 \ 0.88)$	$d=0.92, E=3, \mu = 0.84$ (0.35 1.33)	$\mu = 0.33 \ (-0.04 \ 0.75)$
σ	C3-P3	t(36.17)=-3.54, $p=0.002$, $d=-0.93$,	t(34.82)=-2.24, $p=0.057$, $d=-0.59$,	U=463, $p=0.798$, $d=0.09$, $E=0$,	t(27.11)=2.69, p=0.024,	U=527, $p=0.114$, $d=0.22$, $E=0$,
		E=1, μ =-0.85 (-1.33 -0.37)	E=0, μ =-0.57 (-1.08 -0.06)	$\mu = 0.15 \ (-0.28 \ 0.69)$	d=0.71, E=3, μ =0.68 (0.17	μ =0.35 (-0.04 0.72)
					1.19)	
σ	T4-T6	t(34.51)=-2.91, $p=0.008$, $d=-0.76$,	t(31.99)=-1.66, p=0.117, d=-0.43,	t(35.19)=0.84, p=0.798, d=0.22,	U=604, $p=0.014$, $d=0.38$, $E=3$,	U=540, $p=0.09$, $d=0.25$, $E=0$,
			(-0.94 0.09)	=0.22 (-0.31 0.75)	$\mu=0.75~(0.24~1.18)$	(-0.02 0.59)
б	T3-T5	t(35.91)=-2.39, $p=0.023$, $d=-0.63$, $r=1$, $r=0.62$, 1 , 0.1	t(36.99) = -2.01, p = 0.076, d = -0.53, p = 0.076, d = -0.53, p = 0.076, d = -0.53, d	U=451, $p=0.798$, $d=0.06$, $E=0$, $U=0.106$, $E=0$, $U=0.106$,	U=573, p=0.035, d=0.31, E=3,	U=576, $p=0.025$, $d=0.32$, $E=2$, $U=5.44$ (0.110.04)
		$E=1, \mu = -0.0 (-1.1, -0.1)$	$E=0, \mu = -0.31 (-1.02 0)$	$(eo.0 & ec.0^{-}) \\ $	$(08.0 \ 61.0) \ 10.0 = \pi$	$\mu = 0.44 (0.11 0.04)$

E=0, E=2,	จ์ 1	E=0,	E=0,	E=0,	E=0,	E=0,		E=2,	, E=3,	1	, Е=3,	, E=3,		, E=3,		i, E=3,	, E=3,		E=2,	с Д		E=2,		E=2,		, E=3,		E=2,
$\begin{array}{llllllllllllllllllllllllllllllllllll$	$p = 0.020$, $(0.13 \ 0.94)$	U=522, p=0.12, d=0.21, $\mu = 0.18$ (-0.04 0.43)	U=525, p=0.114, d=0.21, μ =0.19 (-0.04 0.48)	U=525, $p=0.114$, $d=0.21$, u=0.19 (-0.04 0.45)	=530,	$\frac{\mu}{U=498}, \frac{(-0.03, 0.03)}{p=0.23}, \frac{d=0.16}{d=0.16},$	μ =0.15 (-0.1 0.48)	U=642, p=0.002, d=0.45, $\mu = 0.62 (0.32 0.93)$	U=616, p=0.006, d=0.4,	$\mu=0.45~(0.18~0.76)$	U=647, p=0.002, d=0.46, u = 0.49 (0.27 0.84)		$\mu=$ 0.52 (0.28 0.78)	U=662, p=0.001, d=0.49, E=3,	$\mu=$ 0.49 (0.24 0.73)	U=597, $p=0.009$, $d=0.36$, $E=3$, $u=0.33$ (0.09 0.64)	=633,	$\mu=$ 0.47 (0.19 0.78)	=606,	$\mu = 0.33 \ (0.12 \ 0.57)$	p=0.003, (0.21 0.82)	U=615, $p=0.006$, $d=0.4$,	$\mu = 0.34 \ (0.12 \ 0.6)$		$\mu = 0.41 \ (0.14 \ 0.72)$	=596,	μ =0.39 (0.12 0.73)	U=571, $p=0.026$, $d=0.31$, $\mu = 0.42 (0.07 0.9)$
t(29.69)=1.86, p=0.089, d=0.49, E=0, μ =0.48 (-0.04 1.01) t(34.15)=3.66, p=0.011,	, μ -	U=600, p=0.015, d=0.37, E=3, $\mu = 0.7 (0.21 \ 1.14)$	U=622, p=0.011, d=0.41, E=3, μ =0.84 (0.35 1.3)	U=591, p=0.021, d=0.35, E=3, u = 0.71 (0.19 1.15)	t(33.53)=3.05, p=0.014, d=0.8, p=0.8, p=0.14, d=0.8, p=0.14, d=0.8, p=0.14, d=0.14,	U=614, $p=0.013$, $d=0.4$, $E=3$, $U=614$, $p=0.013$, $d=0.4$, $E=3$,	$(0.3 \ 1.23)$	U=612, p=0.03, d=0.39, E=2, $\mu = 0.63 (0.23 1.06)$	=569,		U=549, p=0.054, d=0.26, E=0, $u=0.46$ (0.01 0.89)	U=596, p=0.031, d=0.36, E=3,	$\mu=0.63~(0.2~1.08)$	U=598, $p=0.031$, $d=0.36$, $E=3$,	$\mu=0.62~(0.19~1.07)$	t(37)=1.79, $p=0.082$, $d=0.47$, $E=0$, u=0.46 (-0.05 0.98)	U=574, $p=0.031$, $d=0.31$, $E=3$,	$\mu=$ 0.55 (0.12 1.03)	U=561, $p=0.038$, $d=0.29$, $E=2$,	$\mu = 0.49 \ (0.05 \ 0.92)$	p-0.031, u-0.32, (0.11 1.02)	t(35.68) = 2.48, $p = 0.031$, $d = 0.65$,	E=2, μ =0.63 (0.12 1.13)	t(36.04)=2.71, p=0.031, d=0.71,	E=2, $\mu = 0.68 \ (0.18 \ 1.18)$	=2.57, p=	$d{=}0.68, E{=}3, \mu = 0.64 (0.14)$	U=611, p=0.03, d=0.39, E=2, $\mu = 0.75 (0.25 1.24)$
U=457, p=0.798, d=0.08, E=0, $\mu = 0.12 (-0.29 0.63)$ U=507, p=0.791, d=0.18, E=0.	(-0.11 0.81)	$ \begin{array}{llllllllllllllllllllllllllllllllllll$	t(36.93)=1.65, p=0.791, d=0.43, E=0, μ =0.43 (-0.09 0.94)	$t(36.55)=1.33$, $p=0.791$, $d=0.35$, $E=0.\ \mu=0.35$ (-0.17 0.87)	t(36.84)=0.71, $p=0.798$, $d=0.19$, $r=0.10$	$t=0, \mu = 0.19 (-0.34 0.12)$ t(36.75)=0.51, p=0.798, d=0.13,		t(35.73)=1.81, p=0.087, d=0.48, E=0, μ =0.47 (-0.05 0.99)	U=540, $p=0.076$, $d=0.25$, $E=0$,	$\mu = 0.43 \ (-0.03 \ 0.91)$	U=556, p=0.049, d=0.28, E=3, u = 0.47 (0.04 0.95)		$\mu = 0.63 (0.16 0.99)$	t(35.97)=1.76, p=0.092, d=0.46,	E=0, μ =0.45 (-0.06 0.96)	U=563, $p=0.042$, $d=0.29$, $E=3$, $\mu = 0.51$ (0.06 0.98)	36.26)=	E=0, μ =0.28 (-0.25 0.81)		$\mu = 0.45 \ (-0.02 \ 0.88)$, , , ,	U=506, $p=0.193$, $d=0.18$, $E=0$,	$\mu = 0.27 \ (\text{-}0.15 \ 0.67)$	U=588, $p=0.027$, $d=0.34$, $E=2$,	$\mu = 0.52 \ (0.16 \ 0.9)$	U=624, $p=0.012$, $d=0.42$, $E=3$,	$\mu = 0.74 \; (0.31 \; 1.14)$	U=663, p=0.002, d=0.5, E=3, μ =0.83 (0.48 1.33)
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	3	t(32.47)=-1.94, p=0.079, d=-0.51, E=0, μ =-0.49 (-1 0.02)	t(32.65)=-1.94, p=0.079, d=-0.51, E=0, μ =-0.49 (-1 0.02)	$t(34.25)=-1.46$, $p=0.15$, $d=-0.38$, $E=0. \mu = -0.38$ (-0.89 0.14)	t(36.33)=-1.63, p=0.117, d=-0.43,	$t=0, \mu =-0.42$ (-0.34 0.1) t(35.61)=-1.62, p=0.117, d=-0.42,	E=0, μ =-0.42 (-0.93 0.1)	U=511, p=0.915, d=0.19, E=0, μ =0.35 (-0.15 0.76)	t(34.81)=0.29, p=0.938, d=0.08,	_	t(36.62) = 0.29, $p = 0.938$, $d = 0.08$, $F = 0$, $u = 0.08$ (-0.45 0.61)	t(34.2)=0.96, $p=0.915$, $d=0.25$,	E=0, μ =0.26 (-0.28 0.79)	t(31.05)=0.58, $p=0.915$, $d=0.15$,	E=0, μ =0.15 (-0.37 0.68)	t(36.67)=0.53, p=0.915, d=0.14, E=0. u = 0.14 (-0.39 0.67)	U=382, $p=0.915$, $d=0.08$, $E=0$,	μ =-0.14 (-0.61 0.32)	U=428, $p=0.949$, $d=0.02$, $E=0$,	$\mu = 0.02 (-0.48 0.56)$	$E=0, \mu = -0.08 (-0.61 0.44)$	t(36.67)=0.12, p=0.949, d=0.03,	E=0, μ =0.03 (-0.5 0.56)	t(33.42)=0.04, p=0.969, d=0.01,	$E=0, \mu = 0.01 (-0.52 \ 0.54)$	t(36.82) = 1.17, p = 0.915, d = 0.31,	E=0, μ =0.31 (-0.22 0.83)	t(35.13)=2.54, $p=0.324$, $d=0.66$, E=0, $\mu = 0.63$ (0.13 1.13)
t(36.84)=-2.57, p=0.015, d=-0.68, E=1, μ =-0.64 (-1.15 -0.14) t(25.4)=-2.18, p=0.034, d=-0.57.	E=1, $\mu = -0.55$ (-1.05 -0.04)	U=195, p=0.001, d=0.46, E=1, μ =-0.78 (-1.16 -0.33)	t(33.16)=-2.75, p=0.01, d=-0.72, E=1, μ =-0.68 (-1.17 -0.18)	t(35.83) = -2.32, $p = 0.025$, $d = -0.61$, E=1. $u = -0.58$ (-1.09 -0.08)	t(36.28) = -2.9, $p=0.008$, $d=-0.76$, $m=1$, $m=7$, $t=0.74$, $t=0.003$,	$t_{c=1}, \mu = -0.11 (-1.2, -0.22)$ t(37) = -2.99, p = 0.007, d = -0.79,	23 -0.24)	U=445, p=0.875, d=0.05, E=0, $\mu = 0.07$ (-0.3 0.46)	U=446, $p=0.875$, $d=0.05$, $E=0$,		$U=399$, $p=0.875$, $d=0.04$, $E=0$, $\mu =-0.07$ (-0.45 0.36)	U=450, $p=0.875$, $d=0.06$, $E=0$,	$\mu = 0.12$ (-0.4 0.63)	U=453, $p=0.875$, $d=0.07$, $E=0$,		U=392, p=0.875, d=0.06, E=0, $u = -0.1$ (-0.6 0.29)	U=429, $p=0.896$, $d=0.02$, $E=0$,	$\mu = 0.02 \ (-0.47 \ 0.4)$	U=395, $p=0.875$, $d=0.05$, $E=0$,	$\mu = -0.08 \ (-0.4 \ 0.32)$	ц—0.00,	U=498, $p=0.875$, $d=0.16$, $E=0$,	$\mu = 0.29$ (-0.18 0.7)	U=394, $p=0.875$, $d=0.05$, $E=0$,	$\mu = -0.12 \ (-0.55 \ 0.43)$	U=492, $p=0.875$, $d=0.15$, $E=0$,	$\mu = 0.29 \ (-0.26 \ 0.84)$	U=500, p=0.875, d=0.16, E=0, $\mu = 0.28$ (-0.17 0.72)
P4-PZ P3-PZ		T6-02	T_{5-O1}	P4-02	P3-01	01-02		F8-F4	F7-F3		F4-C4	F3-C3		F4-FZ		FZ-CZ	F3-FZ		T4-C4	ۍ E	r)_r1	C4-CZ		C3-CZ		CZ-PZ		C4-P4
σσ	3	σ	σ	σ	σ	σ		β	β	,	θ	β		β		θ	β		β	Q	J.	β		β		β		β

A.3 Results of statistical tests for epoc	\mathbf{h}	2
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β	C3-P3	U=464, p=0.875, d=0.09, E=0, u = 0.17 (-0.26 0.69)	$\begin{array}{cccc} t(36.94){=}1.04, & p{=}0.915, & d{=}0.27, \\ F{=}0. & u = 0.27 & (-0.25 & 0.8) \end{array}$	U=612, $p=0.012$, $d=0.39$, $E=3$, $\mu = 0.66$ (0.23 1.09)	U=583, p=0.031, d=0.33, E=3, u = 0.68 (0.17 1.08)	U=561, $p=0.038$, $d=0.29$, $E=2$, u=0.4 (0.04 0.73)
β	T4-T6	U=352, $p=0.875$, $d=0.14$, $E=0$,	t(35.21)=0.85, p=0.915, d=0.22, p=0.22, p=0.22, q=0.22, q=0.		U=530, p=0.088, d=0.22, E=0,	U=538, p=0.081, d=0.24, E=0,
β	T3-T5	_	t(33.73)=0.38, $p=0.938$, $d=0.1$,		$\mu = 0.3$ (-0.3 (-0.3 -0.3) U=569, $p=0.031$, $d=0.3$, $E=2$,	
a	D4 D7	4-0 04	$-0.43 \ 0.63$	$\mu = 0.58 (0.09 1)$	$\mu = 0.5 \ (0.07 \ 1.01)$	$\mu = 0.34 (0.06 0.66)$
Q.	74-77	$\mu = 0.09 \ (-0.37 \ 0.63)$	$E=0, \mu = 0.17 (-0.36 \ 0.69)$	$\mu = 0.59 \ (0.16 \ 1.11)$	$\mu = 0.6 \ (0.11 \ 1.09)$	$\mu = 0.48 (0.14 \ 0.8)$
β	P3-PZ	U=471, $p=0.875$, $d=0.1$, $E=0$,	U=464, $p=0.915$, $d=0.09$, $E=0$,	U=583, $p=0.027$, $d=0.33$, $E=3$,	U=570, $p=0.031$, $d=0.31$, $E=3$,	
			$\mu = 0.15 \ (-0.32 \ 0.63)$	μ =0.7 (0.18 1.13)	$\mu=$ 0.61 (0.13 1.09)	
β	T6-O2	U=366, p=0.875, d=0.11, E=0, 012 (-0.43 0.10)	U=428, $p=0.949$, $d=0.02$, $E=0$, u=0.03 (-0.04.051)	U=580, p=0.028, d=0.33, E=3,	U=538, $p=0.074$, $d=0.24$, $E=0$, $u=0.31$ (.0.06.0.60)	U=525, $p=0.109$, $d=0.21$, $E=0$, $u=0.16$ (-0.04.04)
β	T_{5-01}	$\mu = -0.12$ (-0.12 (-0.12) U=342, $p=0.875$, $d=0.16$, $E=0$,	$\mu = 0.03 (-0.13 \pm 0.01)$ t(26.1) = 0.53, p = 0.915, d = 0.14,	=618,	=539,	=535.
-		$(-0.54 \ 0.14)$	$(-0.38 \ 0.66)$	0.29 1.25)	(-0.05 0.78)	3 (-0.01 0.39)
β	P4-O2	U=403, $p=0.875$, $d=0.03$, $E=0$,	t(31.27)=1.27, $p=0.915$, $d=0.33$,	U=611, $p=0.012$, $d=0.39$, $E=3$,	U=569, $p=0.031$, $d=0.3$, $E=2$,	U=526, $p=0.109$, $d=0.22$, $E=0$,
		$\mu = -0.04 \ (-0.43 \ 0.32)$	E=0, μ =0.33 (-0.19 0.85)	$\mu=$ 0.77 (0.27 1.2)	$\mu = 0.45 \ (0.07 \ 0.92)$	$\mu = 0.15 \ (-0.02 \ 0.36)$
β	P3-01	U=368, $p=0.875$, $d=0.11$, $E=0$,	t(34.59)=1.2, p=0.915, d=0.31,	t(33.3)=2.18, $p=0.049$, $d=0.58$,	U=550, $p=0.054$, $d=0.27$, $E=0$,	U=556, $p=0.044$, $d=0.28$, $E=2$,
		$\mu =$ -0.17 (-0.53 0.26)	E=0, μ =0.31 (-0.21 0.83)	$E=3, \ \mu=0.56 \ (0.05 \ 1.07)$	$\mu = 0.46 \ (0.02 \ 0.94)$	$\mu = 0.23 \ (0.01 \ 0.49)$
β	01 - 02	U=409, $p=0.896$, $d=0.02$, $E=0$,	t(32.53)=1.47, p=0.915, d=0.38,	t(36.64)=2.03, p=0.064, d=0.53,	U=564, $p=0.036$, $d=0.29$, $E=3$,	U=523, $p=0.111$, $d=0.21$, $E=0$,
		$\mu = -0.06 \ (-0.51 \ 0.42)$	E=0, μ =0.38 (-0.14 0.89)	$E=0, \mu = 0.52 (0.01 \ 1.03)$	$\mu=$ 0.55 (0.07 1.04)	$\mu = 0.16 \; (-0.04 \; 0.49)$
۲	F8-F4	U=508, p=0.815, d=0.18, E=0,	U=505, p=0.546, d=0.17, E=0,	=613,	U=671, $p=0.001$, $d=0.51$, $E=2$,	=579,
				$(0.27 \ 1.14)$	$0.42 \ 1)$	$(0.12 \ 0.81)$
۲	F7-F3	U=500, p=0.815, d=0.16, E=0,	U=529, $p=0.351$, $d=0.22$, $E=0$,			
		(1)	$\mu = 0.44 \ (-0.09 \ 0.89)$	$\mu = 0.53 \ (0.16 \ 0.89)$	$\mu = 0.41 \ (0.17 \ 0.69)$	$\mu = 0.39 \ (0.12 \ 0.62)$
Х	F4-C4	U=496, $p=0.815$, $d=0.16$, $E=0$,	U=518, $p=0.427$, $d=0.2$, $E=0$,			
		$-0.07 \ 0.26)$		$\mu=$ 0.59 (0.24 0.95)	$\mu = 0.38 \ (0.19 \ 0.64)$	$\mu = 0.24 \ (0.08 \ 0.42)$
7	F3-C3	U=495, $p=0.815$, $d=0.15$, $E=0$,	U=546, $p=0.231$, $d=0.26$, $E=0$,	U=656, $p=0.004$, $d=0.48$, $E=3$,	$U=683$, $p_i0.001$, $d=0.54$, $E=2$,	U=617, $p=0.029$, $d=0.4$, $E=2$,
		$\mu = 0.09 \ (-0.06 \ 0.24)$	$\mu = 0.33 \ (0 \ 0.71)$	$\mu = \textbf{0.68} ~ \textbf{(0.33 ~ 1.01)}$	$\mu = 0.47 \ (0.27 \ 0.71)$	$\mu = 0.26 \ (0.08 \ 0.45)$
Y	F4-FZ	U=552, $p=0.815$, $d=0.27$, $E=0$,	U=555, $p=0.231$, $d=0.28$, $E=0$,	=617,	=636, 2.27	=591,
	20 29	$\frac{\mu}{11} = 0.13 (0.01 0.21) (0.$	$\mu = 0.3 (0.02 0.38)$	$\mu = 0.50 (0.25 0.30) 0.11 \mu = 0.51 0.12$	$\mu = 0.31 (0.13 0.00) \mu = 0.32 \mu = 0.00$	00 00 F
7	F 4-04	p=0.513, d=0.2, (-0.03 0.19)	p=0.231, (0 0.45)	u = 0.41 (0.07 0.64)	p=0.003, d=0.43, (0.14 0.53)	p=0.002, (0.02 0.23)
λ	F3-FZ	U=520, $p=0.815$, $d=0.2$, $E=0$,	U=556, $p=0.231$, $d=0.28$, $E=0$,	=617,	U=649, $p=0.001$, $d=0.47$, $E=2$,	U=568, $p=0.06$, $d=0.3$, $E=0$,
		$\mu = 0.12 \ (-0.03 \ 0.29)$	$\mu = 0.33 \; (0.03 \; 0.61)$	$\mu=$ 0.57 (0.23 0.88)	$\mu = 0.47 \ (0.21 \ 0.71)$	$\mu = 0.21 \ (0.03 \ 0.41)$
λ	T4-C4	U=399, p=0.96, d=0.04, E=0, $\mu = -$	$U=418$, $p=0.982$, $d=0$, $E=0$, $\mu =0$	U=575, $p=0.032$, $d=0.32$, $E=3$,	U=622, $p=0.004$, $d=0.41$, $E=2$,	U=540, $p=0.12$, $d=0.25$, $E=0$,
		0.03 (-0.19 0.13)	(-0.33 0.3)	$\mu=$ 0.29 (0.07 0.59)	$\mu = 0.28 \ (0.11 \ 0.51)$	$\mu = 0.12 \ (-0.01 \ 0.25)$
٨	T3-C3	U=445, $p=0.96$, $d=0.05$, $E=0$,	U=560, $p=0.231$, $d=0.29$, $E=0$,	U=605, $p=0.011$, $d=0.38$, $E=2$,	U=634, $p=0.003$, $d=0.44$, $E=2$,	U=590, $p=0.035$, $d=0.35$, $E=2$,
		$\mu = 0.03 \ (-0.16 \ 0.23)$	\sim	$\mu = 0.5 \ (0.18 \ 0.96)$	$\mu = 0.51 \ (0.24 \ 0.81)$	$\mu = 0.29 \ (0.08 \ 0.49)$
λ	C4-CZ	U=470, $p=0.96$, $d=0.1$, $E=0$,	U=463, $p=0.784$, $d=0.09$, $E=0$,			
		(-0.07 0.18)	31)	: (-0.01 0.63)	$(0.14 \ 0.57)$	$(0.02 \ 0.27)$
×	C3-CZ	U=461, $p=0.96$, $d=0.08$, $E=0$, $U=0.01$, $D=0.08$, $U=0.01$	U=451, $p=0.878$, $d=0.06$, $E=0$, $U=2000$, $C=0$, $U=0$			=582, -0.15
		$\mu = 0.04 (-0.08 \ 0.14)$	$\mu = 0.09 (-0.22 \ 0.4)$	$\mu = 0.52 \ (0.24 \ 0.92)$	$(80.0 \text{ ct.} 0.13) \text{ bc.} 0 = \pi$	$\mu = 0.15 \ (0.04 \ 0.36)$

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N	-PZ	CZ-PZ U=479, p=0.96, d=0.12, E=0,	U=466, $p=0.784$, $d=0.09$, $E=0$,	U=550, $p=0.059$, $d=0.27$, $E=0$,	U=594, $p=0.012$, $d=0.36$, $E=2$,	U=508, $p=0.268$, $d=0.18$, $E=0$,
	4	$\mu = 0.05 \ (-0.07 \ 0.19)$	$\mu = 0.12 \ (-0.26 \ 0.48)$	$\mu = 0.4 \; (0.01 \; 0.71)$	$\mu = 0.34 \ (0.11 \ 0.65)$	$\mu = 0.07 \; (-0.03 \; 0.19)$
C4-P4		U=439, $p=0.96$, $d=0.04$, $E=0$,	U=492, $p=0.616$, $d=0.15$, $E=0$,	U=542, $p=0.066$, $d=0.25$, $E=0$,	U=584, $p=0.018$, $d=0.34$, $E=2$,	U=482, $p=0.436$, $d=0.13$, $E=0$,
	4	$\mu = 0.02 \ (-0.11 \ 0.15)$	$\mu = 0.2 (\text{-}0.13 0.56)$	μ =0.37 (-0.02 0.79)	$\mu = 0.4 \ (0.1 \ 0.78)$	$\mu = 0.12 \ (\text{-}0.14 \ 0.41)$
C3-P3		U=440, $p=0.96$, $d=0.04$, $E=0$,	U=477, $p=0.676$, $d=0.12$, $E=0$,	U=557, $p=0.05$, $d=0.28$, $E=0$,	U=583, $p=0.018$, $d=0.33$, $E=2$,	U=505, $p=0.273$, $d=0.17$, $E=0$,
	1	$\mu = 0.03 \ (-0.14 \ 0.17)$	$\mu = 0.13 \ (-0.2 \ 0.43)$	$\mu = 0.45 \ (0.04 \ 0.77)$	$\mu = 0.44 \ (0.1 \ 0.76)$	$\mu = 0.17 \ (\text{-}0.07 \ 0.4)$
T4-T6		U=420, p=1, d=0, E=0, $\mu = 0$ (-	U=450, $p=0.878$, $d=0.06$, $E=0$,	U=550, $p=0.059$, $d=0.27$, $E=0$,	U=547, $p=0.062$, $d=0.26$, $E=0$,	U=528, $p=0.167$, $d=0.22$, $E=0$,
)	$0.22\ 0.15)$	$\mu = 0.06 \ (-0.19 \ 0.32)$	$\mu = 0.3 \; (0.01 \; 0.58)$	$\mu = 0.21 \ (0 \ 0.43)$	$\mu = 0.1 \ (-0.03 \ 0.23)$
T_{3-T_5}		U=428, $p=0.994$, $d=0.02$, $E=0$,	U=484, $p=0.638$, $d=0.13$, $E=0$,	U=568, $p=0.037$, $d=0.3$, $E=2$,	U=566, $p=0.033$, $d=0.3$, $E=2$,	U=541, $p=0.12$, $d=0.25$, $E=0$,
	-	$\mu = 0.01 \ (-0.18 \ 0.18)$	μ =0.19 (-0.2 0.62)	$\mu = 0.48 \ (0.07 \ 0.9)$	$\mu = 0.31 \ (0.05 \ 0.61)$	$\mu = 0.18 \ (-0.01 \ 0.35)$
1-I	Z	P4-PZ U=434, p=0.96, d=0.03, E=0,	U=424, $p=0.982$, $d=0.01$, $E=0$,	U=541, $p=0.066$, $d=0.25$, $E=0$,	U=561, $p=0.038$, $d=0.29$, $E=2$,	U=482, $p=0.436$, $d=0.13$, $E=0$,
	-	$\mu = 0.02 \ (-0.09 \ 0.16)$	$\mu = 0.01 \ (-0.26 \ 0.28)$	μ =0.39 (-0.02 0.73)	$\mu = 0.35 \ (0.05 \ 0.65)$	$\mu = 0.08 \; (-0.07 \; 0.22)$
-	PZ 1	P3-PZ U=423, p=1, d=0.01, E=0, $\mu = 0$	U=499, $p=0.572$, $d=0.16$, $E=0$,	U=565, $p=0.039$, $d=0.3$, $E=2$,	U=581, $p=0.018$, $d=0.33$, $E=2$,	U=518, $p=0.214$, $d=0.2$, $E=0$,
)	(-0.1 0.11)	$\mu = 0.17 \; (-0.12 \; 0.48)$	$\mu = 0.56 \ (0.07 \ 0.97)$	$\mu = 0.31 \ (0.06 \ 0.62)$	$\mu = 0.08 \ (\text{-}0.02 \ 0.2)$
- <u>-</u>	02	T6–O2 D=403, p=0.96, d=0.03, E=0, $\mu = -$	U=406, p=0.96, d=0.03, E=0, μ =-	U=543, $p=0.066$, $d=0.25$, $E=0$,	U=524, $p=0.116$, $d=0.21$, $E=0$,	U=450, $p=0.678$, $d=0.06$, $E=0$,
)	0.02 (-0.15 0.09)	$0.03 \ (-0.36 \ 0.21)$	μ =0.28 (-0.02 0.52)	$\mu = 0.13 \ (-0.03 \ 0.32)$	$\mu = 0.02 \; (-0.06 \; 0.11)$
2	T5-01 1	U=399, p=0.96, d=0.04, E=0, $\mu =$ -	U=401, $p=0.938$, $d=0.04$, $E=0$,	U=529, $p=0.092$, $d=0.22$, $E=0$,	U=523, $p=0.116$, $d=0.21$, $E=0$,	U=457, $p=0.628$, $d=0.08$, $E=0$,
)	0.01 (-0.12 0.1)	$\mu = -0.04 \; (-0.25 \; 0.18)$	$\mu = 0.22 \ (\text{-}0.03 \ 0.47)$	$\mu = 0.13$ (-0.04 0.35)	$\mu = 0.02 \ (\text{-}0.06 \ 0.11)$
1-(D2 1	P4-O2 U=368, p=0.96, d=0.11, E=0, $\mu = -$	$U=422$, p=0.982, d=0, E=0, $\mu = 0$	U=538, $p=0.07$, $d=0.24$, $E=0$,	U=545, $p=0.063$, $d=0.26$, $E=0$,	U=464, $p=0.576$, $d=0.09$, $E=0$,
)	0.04 (-0.14 0.05)	(-0.18 0.19)	$\mu = 0.27 \; (\text{-}0.01 \; 0.53)$	$\mu = 0.15 \ (0 \ 0.32)$	$\mu = 0.02 \ (-0.04 \ 0.09)$
10	P3-01 [U=378, p=0.96, d=0.09, E=0, $\mu =$ -	U=483, $p=0.638$, $d=0.13$, $E=0$,	U=582, $p=0.028$, $d=0.33$, $E=2$,	U=541, $p=0.069$, $d=0.25$, $E=0$,	U=472, $p=0.516$, $d=0.11$, $E=0$,
)	0.03 (-0.14 0.08)	$\mu = 0.09 \ (-0.13 \ 0.32)$	$\mu = 0.37 \ (0.09 \ 0.65)$	$\mu = 0.17 \ (\text{-}0.01 \ 0.41)$	$\mu = 0.03 \ (-0.06 \ 0.12)$
Ĩ	02 1	O1-O2 U=399, p=0.96, d=0.04, E=0, $\mu = -$	U=398, $p=0.938$, $d=0.04$, $E=0$,	U=580, $p=0.028$, $d=0.33$, $E=2$,	U=503, $p=0.201$, $d=0.17$, $E=0$,	U=405, $p=0.823$, $d=0.03$, $E=0$,
	_	0.01 (-0.11 0.08)	$\mu = -0.04 \; (-0.3 \; 0.21)$	$\mu = 0.42 \ (0.1 \ 0.72)$	$\mu = 0.11$ (-0.06 0.35)	$\mu = -0.01 \ (-0.08 \ 0.08)$

The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were observed (E), and group difference estimate (95% CI). Reliable differences (significant in all three epochs) are
 Table A.15: Results from epoch 2 comparing unweighted edge betweenness.
 highlighted with bold text.

$\begin{array}{c c} \delta & U = 507, \ p = 0.18, \ d = 0.18, \\ \hline T = 5, \ E = 0, \ \mu = 0.3, \ (0.14, 0.63) \\ \hline \theta & U = 489, \ p = 0.28, \ d = 0.14, \\ T = 0, \ E = 0, \ \mu = 0.18, \ (0.18, 0.54) \\ \hline U = 569, \ h = 0.02, \ d = 0.3 \end{array}$		θ	σ	β	λ
$\begin{array}{c c} 0 & T=5, E=0, \mu = 0\\ \theta & U=489, p=0.2\\ T=0, E=0, \mu = 0\\ 11=569, n=0 \end{array}$	18, d=0.18,	U=574, $p=0.016$, $d=0.31$,	t(33.13)=3.63, p=0.001, d=0.95,	$U=650$, p $_{1}0.001$, d $=0.47$,	U=506, p=0.185, d=0.18,
θ U=489, p=0.5 T=0, E=0, $\mu = 0.1$).3 (-0.14 0.63)	T=13, E=1, $\mu = 0.56 \ (0.09 \ 0.96)$	T=19, E=2, $\mu = 0.86 \ (0.38 \ 1.33)$	$T=18, E=3, \mu = 0.85 (0.4 1.24)$	T=9, E=0, $\mu = 0.2$ (-0.08 0.47)
T=0, E=0, $\mu = 0$	89, d=0.14,	U=498, p=0.23, d=0.16,	U=536, $p=0.072$, $d=0.24$,	U=570, p=0.019, d=0.31,	U=549, $p=0.045$, $d=0.26$,
11=569. n=0	.18 (-0.18 0.54)	T=0, E=0, $\mu = 0.28$ (-0.17 0.72)	T=5, E=0, $\mu = 0.43$ (-0.04 0.9)	T=19, E=1, $\mu = 0.51 \ (0.08 \ 0.93)$	T=11, E=1, $\mu = 0.33$ (0.01 0.64)
	U=569, $p=0.02$, $d=0.3$,	U=539, $p=0.065$, $d=0.24$,	U=555, $p=0.036$, $d=0.28$,	U=599, $p=0.005$, $d=0.37$,	U=627, $p=0.001$, $d=0.42$,
T=20, E=1, $\mu = 0.34 \ (0.04 \ 0.65)$	0.34(0.040.65)	T=8, E=0, $\mu = 0.44$ (-0.01 0.82)	T=13, E=1, $\mu = 0.49 \ (0.03 \ 0.93)$	T=19, E=1, $\mu = 0.59 \ (0.16 \ 1.01)$	T=18, E=1, $\mu = 0.38 \ (0.16 \ 0.58)$
\square_a U=561, p=0.028, d=0.29,	128, d=0.29,	U=527, $p=0.098$, $d=0.22$,	U=541, $p=0.06$, $d=0.25$,	t(31.53)=2.25, $p=0.029$, $d=0.59$,	U=572, p=0.018, d=0.31,
μ T=14, E=1, μ = 0.39 (0.04 0.72)	0.39 (0.04 0.72)	T=4, E=0, $\mu = 0.34$ (-0.07 0.71)	T=6, E=0, $\mu = 0.41$ (-0.01 0.79)	T=15, E=1, $\mu = 0.56 \ (0.06 \ 1.07)$	T=16, E=1, $\mu = 0.31 \ (0.06 \ 0.48)$
\int_{∞} t(35.3)=-1, p=0.321, d=-0.26,	.321, d=-0.26,	U=509, $p=0.17$, $d=0.18$,	U=569, $p=0.02$, $d=0.3$,	U=559, $p=0.03$, $d=0.28$,	U=488, $p=0.296$, $d=0.14$,
T=6, E=0, $\mu = -0.26$ (-0.79 0.26)		T=3, E=0, $\mu = 0.23$ (-0.12 0.65)	T=15, E=2, $\mu = 0.35 \ (0.06 \ 0.65)$	T=15, E=1, $\mu = 0.28 \ (0.04 \ 0.53)$	T=1, E=0, $\mu = 0.23$ (-0.24 0.71)

of thresholds where significant differences were observed (T), number of epochs where significant differences were **Table A.16:** Results from epoch 2 comparing unweighted global vulnerability. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number observed (E), and group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	δ	θ	σ	β	~
δ		t(37)=-4.64, pi0.001, d=-1.22,	t(36.96) = -1.31, p = 0.194, d = -0.35,	t(33.86) = -1.24, p = 0.219, d = -0.33,	t(36.99) = -1.78, p = 0.08, d = -0.47, c = 0.00, d = -0.47, c = 0.00, c =
	T=19, E=3, $\mu = -0.94(-1.4 - 0.48)$	T=16, E=3, $\mu = -1.04(-1.49 - 0.59)$	T=3, E=0, $\mu = -0.34(-0.87\ 0.18)$	$T=2, E=0, \mu = -0.32(-0.84 \ 0.2)$	T=8, E=0, $\mu = -0.46(-0.97 \ 0.06)$
Ч	t(35.35)=1.21, p=0.232, d=0.32, d=0.	U=315, $p=0.104$, $d=0.21$,	U=492, $p=0.268$, $d=0.15$,	U=348, $p=0.268$, $d=0.15$,	U=344, $p=0.242$, $d=0.16$,
2	T=4, E=0, $\mu = 0.32(-0.21 \ 0.84)$	T=1, E=0, $\mu = -0.35(-0.87 \ 0.08)$	T=0, E=0, $\mu = 0.18(-0.14 \ 0.51)$	T=0, E=0, $\mu = -0.23(-0.77\ 0.27)$	T=2, E=0, $\mu = -0.22(-0.66\ 0.17)$
ć	U=505, $p=0.19$, $d=0.17$,	t(35.45)=-1.09, $p=0.281$, $d=-0.29$,	U=511, $p=0.16$, $d=0.19$,	t(34.49)=-0.74, $p=0.461$, $d=-0.2$,	U=386, $p=0.605$, $d=0.07$,
3	T=7, E=0, $\mu = 0.35(-0.14 \ 0.88)$	T=5, E=0, $\mu = -0.29(-0.81 \ 0.24)$	T=5, E=0, $\mu = 0.28(-0.13 \ 0.62)$	T=0, E=0, $\mu = -0.2(-0.73\ 0.33)$	T=0, E=0, $\mu = -0.13(-0.63 \ 0.35)$
æ	t(30.07) = -1.04, $p = 0.301$, $d = -0.27$,	t(36.97)=-0.74, $p=0.462$, $d=-0.19$,	U=453, $p=0.616$, $d=0.07$,	t(34.58)=2.73, $p=0.008$, $d=0.72$,	t(37)=-2.34, $p=0.023$, $d=-0.61$,
2	T=6, E=0, $\mu = -0.27(-0.79 \ 0.25)$	T=0, E=0, $\mu = -0.19(-0.72 \ 0.33)$	T=1, E=0, $\mu = 0.03(-0.07 \ 0.12)$	T=10, E=1, $\mu = 0.68(0.18 \ 1.19)$	T=12, E=2, $\mu = -0.59(-1.1 - 0.08)$
i	U=370, p=0.444, d=0.1,	t(36.76)=0.65, p=0.516, d=0.17,	U=456, $p=0.583$, $d=0.07$,	$t(34.2)=-3.94$, $p_i0.001$, $d=-1.04$,	t(36.54)=-1.63, p=0.109, d=-0.43,
-	T=6, E=0, $\mu = -0.12(-0.51 \ 0.21)$	T=0, E=0, $\mu = 0.17(-0.36 \ 0.7)$	T=1, E=0, $\mu = 0.13(-0.34 \ 0.6)$	T=14, E=3, $\mu = -0.93(-1.4 - 0.45)$	T=7, E=0, $\mu = -0.42(-0.94 \ 0.1)$

Table A.17: Results from epoch 2 comparing unweighted local vulnerability. The results are reported as follows:
statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number
of thresholds where significant differences were observed (T), number of epochs where significant differences were
observed (E), and group difference estimate (95% CI). Reliable differences (significant in all three epochs) are
highlighted with bold text.

		0.660	. d=-0.19,	$0.71 \ 0.34)$, $d=0.35$, $t(36.83)=-1.74$, $p=0.088$, $d=-0.46$,	$(17\ 0.87)$ T=4, E=0, $\mu = -0.45\ (-0.96\ 0.07)$	=0.4, $t(36.56)=-1.08$, $p=0.283$, $d=-0.28$,	0.23 1.1) T=4, E=0, $\mu = -0.28$ (-0.81 0.24)	, $d=-0.51$, $U=662$, $p_10.001$, $d=0.49$,	1.01 0.02) T=19 , E=3 , $\mu = 0.25$ (0.12 0.43)
β	t(34.9)=-0.48, $p=0.633$, $d=-0.13$,	T=0, E=0, $\mu = -0.13$ (-0.66 0.41)	t(36.55)=-0.72, p=0.476, d=-0.19,	T=0, E=0, $\mu = -0.19 (-0.71 \ 0.34)$	t(33.16)=1.35, p=0.182, d=0.35, t=0.35, t=0.3	T=6, E=0, $\mu = 0.35$ (-0.17 0.87)	U=617, p=0.002, d=0.4,	T=12, E=1, $\mu = 0.66 \ (0.23 \ 1.1)$	t(36.12)=-1.94, p=0.058, d=-0.51, t=-0.51, t=-	T=8, E=0, $\mu = -0.49$ (-1.01 0.02)
σ	t(36.84)=-0.99, p=0.325, d=-0.26,	T=2, E=0, $\mu = -0.26$ (-0.78 0.26)	t(34.46)=0.86, $p=0.392$, $d=0.23$,	T=1, E=0, $\mu = 0.23$ (-0.3 0.76)	U=520, p=0.122, d=0.2,	T=7, E=0, $\mu = 0.43$ (-0.13 0.95)	t(36.22)=2.16, p=0.035, d=0.57, t=0.035, d=0.57, t=0.57, t=0	T=11, E=1, $\mu = 0.55 \ (0.04 \ 1.06)$	U=304, $p=0.072$, $d=0.24$,	T=6, E=0, $\mu = -0.39$ (-0.81 0.04)
θ	t(34.75)=-1.66, $p=0.104$, $d=-0.44$,	T=6, E=0, $\mu = -0.43$ (-0.95 0.09)	U=365, p=0.399, d=0.11,	T=0, E=0, $\mu = -0.18$ (-0.79 0.24)	t(28.77)=-1.36, p=0.18, d=-0.36,	T=3, E=0, $\mu = -0.36$ (-0.89 0.17)	U=529, $p=0.092$, $d=0.22$,	T=6, E=0, $\mu = 0.35$ (-0.07 0.83)	U=320, p=0.122, d=0.2,	T=0, E=0, $\mu = -0.36 (-0.8 \ 0.08)$
δ	U=247, $p=0.007$, $d=0.35$,	T=14, E=1, $\mu = -0.67$ (-1.12 -0.16) T=6, E=0, $\mu = -0.43$ (-0.95 0.09)	t(34.18)=-1.47, p=0.148, d=-0.38,	T=4, E=0, $\mu = -0.38$ (-0.89 0.14)	t(34.6)=-1.41, p=0.164, d=-0.37,	T=5, E=0, $\mu = -0.36$ (-0.88 0.15)	t(35.19)=-2.09, p=0.042, d=-0.55,	T=10, E=1, $\mu = -0.53$ (-1.05 -0.02)	U=307, $p=0.08$, $d=0.23$,	T=9, E=0, $\mu = -0.36$ (-0.76 0.03)

of thresholds where significant differences were observed (T), number of epochs where significant differences were Table A.18: Results from epoch 2 comparing weighted edge betweenness. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number observed (E), and group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		Ŷ	θ	σ	β	~
	ч	$U=608$, $p_i0.001$, $d=0.47$,	U=618, p;0.001, d=0.49,	$U=681.5$, p $_{1}0.001$, d $=0.55$,	$U=671, p_{i}0.001, d=0.51,$	$U=639$, $p_i0.001$, $d=0.45$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	0	$T=20, E=3, \mu = 0 (0 0.01)$	$T=14, E=3, \mu = 0.03 (0 0.14)$	T=19, E=3, $\mu = 0.45$ (0.21 0.91)	$T=18, E=3, \mu = 0.25 (0.14 0.55)$	T=19, E=3, $\mu = 0.95$ (0.38 1.38)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	d	$U=683.5$, p $_{1}0.001$, d $=0.54$,	U=556.5, p=0.003, d=0.39,	U=448, p=0.176, d=0.18,	U=478.5, p=0.367, d=0.12,	U=480, p=0.357, d=0.12,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	5	T=10, E=3, $\mu = 0.56$ (0.3 1)	$T=10, E=3, \mu = 0 (0 0)$	T=4, E=0, $\mu = 0 \ (0 \ 0)$	T=1, E=0, $\mu = 0.07$ (-0.02 0.24)	T=1, E=0, $\mu = 0.13$ (-0.2 0.38)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	ć	U=504.5, $p=0.065$, $d=0.24$,	U=461, p=0.265, d=0.15,	U=458, p=0.354, d=0.12,	U=442, p=0.738, d=0.04,	U=350, p=0.282, d=0.14,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	3	T=10, E=2, $\mu = 0 \ (0 \ 0)$	T=1, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0$ (0 0)	T=2, E=0, $\mu = 0.03$ (-0.15 0.27)	T=1, E=0, $\mu = -0.14$ (-0.44 0.15)
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	0	$U=686$, p $_{1}0.001$, d $=0.54$,	t $(36.24)=0.53$, p=0.6, d=0.14,	U=389.5, p=0.51, d=0.09,	U=455, $p=0.589$, $d=0.07$,	U=176, p;0.001, d=0.5,
$\begin{array}{ c c c c c c c } U = 381, \ p = 0.552, \ d = 0.08, \\ T = 1, \ E = 0, \ \mu = -0.05 \ (-0.22 \ 0.12) \\ T = 14, \ E = 3, \ \mu = -0.65 \ (-1.04 \ -0.27) \\ \end{array}$	2	T=19, E=3, $\mu = 0.71$ (0.36 1.13)	T=0, E=0, μ = 0.14 (-0.39 0.67)	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0$ (-0.02 0.04)	T=18, E=3, $\mu = -0.77$ (-1.13 -0.28)
T=1, E=0, $\mu = -0.05$ (-0.22 0.12) T=14, E=3, $\mu = -0.65$ (-1.04 -0.27)	č	U=628, $p=0.001$, $d=0.42$,	U=354, $p=0.311$, $d=0.13$,	U=381, $p=0.552$, $d=0.08$,	U=207, $p=0.001$, $d=0.44$,	t(32)=-3.69, p=0.001, d=-0.96,
		T=18, E=3, $\mu = 1.05$ (0.45 1.45)	T=6, E=0, $\mu = -0.23$ (-0.7 0.18)	T=1, E=0, $\mu = -0.05$ (-0.22 0.12)	$T=14, E=3, \mu = -0.65$ (-1.04 -0.27)	T=17, E=3, $\mu = -0.87$ (-1.34 -0.4)

Table A.19: Results from epoch 2 comparing weighted global vulnerability. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	δ	θ	σ	β	κ
ч	U=389, $p=0.638$, $d=0.06$,	U=387, $p=0.616$, $d=0.07$,	U=467, p=0.472, d=0.1,	$U=645$, p $_{1}0.001$, d $=0.46$,	t(36.04)=1.44, p=0.154, d=0.38,
0	T=3, E=0, $\mu = 0 \ (0 \ 0)$	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=3, E=0, $\mu = 0 \ (0 \ 0)$	T=19, E=3, $\mu = 0.19$ (0.06 0.48)	T=2, E=0, $\mu = 0.37$ (-0.14 0.89)
9	U=377, $p=0.511$, $d=0.09$,	U=483, p=0.333, d=0.13,	U=388, p=0.627, d=0.07,	U=386, $p=0.605$, $d=0.07$,	U=475, p=0.399, d=0.11,
2	T=3, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0.17)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = -0.01$ (-0.06 0.03)	T=0, E=0, μ = 0.22 (-0.31 0.74)
ć	U=483, $p=0.333$, $d=0.13$,	U=388, p=0.627, d=0.07,	U=400, p=0.763, d=0.04,	U=388, $p=0.627$, $d=0.07$,	U=355, p=0.318, d=0.13,
3	T=5, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=2, E=0, $\mu = -0.22$ (-0.74 0.3)
a	U=644, p;0.001, d=0.46,	U=379, $p=0.531$, $d=0.08$,	U=459, $p=0.552$, $d=0.08$,	U=458, $p=0.562$, $d=0.08$,	U=176, p;0.001, d=0.5,
2	T=10, E=3, $\mu = 0.4$ (0.03 0.62)	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=18, E=3, $\mu = -0.64$ (-0.96 -0.3)
i	U=532, $p=0.083$, $d=0.23$,	U=446, $p=0.694$, $d=0.05$,	U=396, $p=0.717$, $d=0.05$,	t(35.65)=-3.68, $p=0.001$, $d=-0.96$,	$U=185, p_{1}0.001, d=0.48,$
-	T=4, E=0, $\mu = 0.35$ (-0.03 0.83)	T=0, E=0, $\mu = 0.13$ (-0.28 0.6)	T=0, E=0, $\mu = -0.08$ (-0.51 0.28)	T=20, E=3, $\mu = -0.87$ (-1.34 -0.4)	T=18, E=3, $\mu = -0.96$ (-1.5 -0.38)

statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were **Table A.20:** Results from epoch 2 comparing weighted local vulnerability. The results are reported as follows: observed (E), and group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

		c		c		
	0	A	σ	8	λ	
	$U=644$, p $_{1}0.001$, d $=0.46$,	$U=657$, p $_{1}0.001$, d $=0.48$,	U=213, p=0.001, d=0.42,	$U=176$, p $_{1}0.001$, d $=0.5$,	U=456, p=0.583, d=0.07,	
Ë	=17, E=3, $\mu = 0.79$ (0.36 1.22)	$\mathbf{T}{=}17, \mathbf{E}{=}3, \mu = 0.79 \left(0.36 1.22 \right) \left \begin{array}{c} \mathbf{T}{=}18, \mathbf{E}{=}3, \mu = 0.86 \left(0.46 1.29 \right) \end{array} \right $	T=14, E=3, $\mu = -0.76$ (-1.13 -0.39)	$T=14, E=3, \mu = -0.7$ (-0.97 -0.4)	T=0, E=0, μ = 0.1 (-0.28 0.47)	
÷.	$(28.75)=3.75, p_i0.001, d=0.98,$	t(28.75)=3.75, p 10.001 , d=0.98, $t(36.76)=3.51$, p=0.001, d=0.92, $t(28.75)=3.75$, p=0.001, d=0.92, $t(28.75)=3.51$, p=0.001, d=0.92, p=0.001, d=0.92, $t(28.75)=3.51$, p=0.001, d=0.92, p=0.92, p=	U=263, p=0.014, d=0.32,	$t(33.55)=-5.08$, $p_{1}0.001$, $d=-1.34$,	U=349, p=0.275, d=0.15,	_
H	T=19, E=3, $\mu = 0.88$ (0.41 1.35)	T=15, E=3, $\mu = 0.84$ (0.36 1.32)	T=12, E=2, $\mu = -0.57$ (-0.91 -0.13)	T=16, E=3, $\mu = -1.12$ (-1.56 -0.68)	T=0, E=0, $\mu = -0.15$ (-0.46 0.13)	
-	$t(36.95)=3.9, p_10.001, d=1.02,$	t(34.18)=3.25, $p=0.002$, $d=0.86$,	U=212, p=0.001, d=0.42,	$t(28.29)=-5.33$, $p_{1}0.001$, $d=-1.41$,	U=349, $p=0.275$, $d=0.15$,	
H	T=19, E=3, $\mu = 0.92$ (0.45 1.38)	T=14, E=3, $\mu = 0.79$ (0.3 1.28)	T=14, E=3, $\mu = -0.82$ (-1.29 -0.34)	T=15, E=3, $\mu = -1.16$ (-1.6 -0.72)	T=5, E=0, $\mu = -0.21$ (-0.62 0.14)	
4	$t(33.58)=3.73$, $p_i0.001$, $d=0.97$,	U=610, p=0.003, d=0.39,	U=271, $p=0.02$, $d=0.3$,	$U=177$, $p_i0.001$, $d=0.5$,	U=320, p=0.122, d=0.2,	_
H	T=18, E=3, $\mu = 0.88$ (0.41 1.35)	T=11, E=3, $\mu = 0.7$ (0.24 1.19)	T=12, E=1, $\mu = -0.5$ (-0.84 -0.07)	T=14, E=3, $\mu = -0.87$ (-1.24 -0.51)	T=6, E=0, $\mu = -0.26$ (-0.59 0.05)	
	U=547, $p=0.048$, $d=0.26$,	t(32.94)=1.24, p=0.222, d=0.33,	t(33.97) = -0.65, $p = 0.521$, $d = -0.17$,	$t(32.39)=-3.72$, $p_{1}0.001$, $d=-0.98$,	t(35.36)=-3.19, p=0.002, d=-0.83,	_
	T=10, E=1, $\mu = 0.48 \ (0 \ 1.06)$	T=4, E=0, $\mu = 0.33$ (-0.2 0.85)	T=0, E=0, $\mu = -0.17$ (-0.69 0.36)	T=16, E=3, $\mu = -0.89$ (-1.37 -0.41)	T=16, E=3, $\mu = -0.89$ (-1.37 -0.41) T=11, E=3, $\mu = -0.77$ (-1.26 -0.29)	

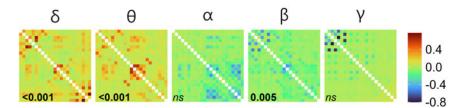


Figure A.12: Difference of average connectivity matrices (AD – HC) measured with CS in epoch 3. For visualisation purposes, the values were min-max normalised. Digits in black denote a *p*-value testing for the difference in global coupling (p < 0.05 in bold, in italics otherwise).

A.4 Results for epoch 3

In-this-section,-we-only-report-the-results-of-the-statistical-comparisons-and-corresponding-figures-using-data-from-the-third-epoch.-

The comparisons of average coupling computed with CS and CBS are shown in Tables A.21 and A.22, respectively. Additionally, the corresponding figures of connectivity matrices computed with CS and CBS are shown in Figures A.12 and A.13.

The comparisons of node strength computed with CS and CBS are shown in Table A.23 and Figure A.14, and Table A.24 and Figure A.15, respectively.

Results-of-comparisons-of-the-unweighted-multilayer-network-metrics-are-reportedin-Tables-A.25,-A.26- and-A.27- for-edge-betweenness,-global-vulnerability- and-localvulnerability,-respectively.- The-corresponding-figures-are;- edge-betweenness- (Figure-A.16),-global-vulnerability-(Figure-A.17)-and-local-vulnerability-(Figure-A.18).-

Results of comparisons of the weighted multilayer network metrics are reported in Tables A.28, A.29 and A.30 for edge betweenness, global vulnerability and local vulnerability, respectively. The corresponding figures are; edge betweenness (Figure A.19), global vulnerability (Figure A.20) and local vulnerability (Figure A.21). **Table A.21:** Comparisons of the mean of adjacency matrix constructed with CS in epoch 3. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number of epochs where significant differences were observed (E), difference estimate μ with 95% confidence interval. Reliable differences (significant in all three epochs) are highlighted with bold text.

Frequency-band-	Test-	Difference-estimate-(95%-CI)-
α	t(34.87) = -2.12, p = 0.049, d = -0.55, E = 1	$\mu = -0.54 (-1.04 - 0.03)$
β	U=231, $p=0.005$, $d=0.39$, $E=3$	$\mu = -0.72 (-1.19 - 0.2)$
δ	t(34.62)=4.82, p;0.001, d=1.26, E=3	$\mu = 1.07 \cdot (0.62 \cdot 1.51)$
γ	U=355, p=0.318, d=0.13, E=0	$\mu = -0.27 (-0.85 \cdot 0.31)$
θ	t(32.41)=4.93, p;0.001, d=1.3, E=3	$\mu = 1.1 \cdot (0.65 \cdot 1.54)$

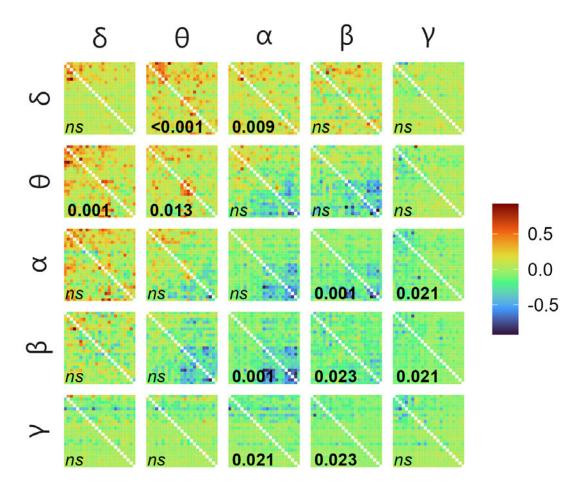


Figure A.13: Difference of average connectivity matrices (AD – HC) measured with CBS in epoch 3 with input frequency on the vertical facets and output frequency on the horizontal. For visualisation purposes, the values were min-max normalised. Digits in white denote a *p*-value testing for the difference in global coupling (p < 0.05 in bold, in italics otherwise).

	δ	θ	σ	β	λ
L L	t(36.7)=3.5, p=0.005, d=0.92,	$t(36.86) = 4.74$, $p_{10.001}$, $d = 1.24$,	t(36.86) = 4.74, p;0.001, d=1.24, $t(32.33) = 3.21$, p=0.009, d=0.84,	t(35.67)=0.47, p=0.763, d=0.12,	U=435, p=0.857, d=0.03,
0	$E=2, -\mu = -0.84(0.36-1.32)$	E=3, $\mu = 1.06$ (0.61 1.51)	$E=3, \ \mu = 0.77(0.29 \ 1.26)$	$E=0.7\mu = -0.12(-0.4-0.65)$	$E=0, -\mu = -0.04(-0.52-0.51)$
<	t(36.75)=3.97, p=0.001, d=1.04, t(36.48)=3.03, p=0.013, d=0.8,	t(36.48)=3.03, p=0.013, d=0.8,	t(34.96)=0.4, p=0.783, d=0.11,	t(30.99)=-2.9, p=0.017, d=-0.76,	U=376, p=0.626, d=0.09,
ь	E=3, $\mu = 0.93(0.46 \ 1.4)$	E=3, $\mu = 0.74(0.25 \ 1.24)$	$E=1, -\mu = -0.11(-0.42, -0.63)$	$E=1, \mu = -0.71(-1.2-0.22)$	$E=1, -\mu = -0.17(-0.66-0.29)$
ć	t(36.28)=2.49, p=0.026, d=0.65, t=0.026, t=0.05, t=0.05, t=0.05, t=0.026,	t(36.75)=0.8, p=0.559, d=0.21,	t(36.79)=-2.57, fp=0.023, d=-0.67,	t(37)=-4.15, $p=0.001$, $d=-1.09$,	t(36.81)=-2.72, $p=0.021$, $d=-0.71$,
3	$E=2, -\mu = -0.62(0.12-1.12)$	$E=1, -\mu = -0.21(-0.31-0.74)$	$E=1, 7\mu = -0.64(-1.14-0.14)$	E=3, $\mu = -0.96(-1.42 - 0.5)$	$E=3, \ \mu = -0.68(-1.17 \ -0.18)$
0	t(33.54)=-0.09, p=0.928, d=-0.02,	t(29.57)=-2.26, rp=0.044, rd=-0.59,	t(37) = -4.04, $p = 0.001$, $d = -1.06$,	t(36.54)=-2.63, p=0.023, d=-0.69, t(36.29)=-2.77, p=0.021, d=-0.72, t(36.54)=-2.63, b=0.021, d=-0.72, t(36.54)=-2.63, b=0.021, d=-0.72, t(36.54)=-2.63, b=0.021, d=-0.72, t(36.54)=-2.63, b=0.021, d=-0.72, t(36.54)=-2.77, b=0.021, d=-0.72, d	t(36.29)=-2.77, p=0.021, d=-0.72,
0	$E=0, \tau \mu = -0.02(-0.55-0.5)$	$E=1, -\mu = -0.57(-1.07 - 0.06)$	E=3, $\mu = -0.94(-1.41 - 0.47)$	E=3, $\mu = -0.66(-1.16 - 0.16)$	E=3, $\mu = -0.68(-1.18 - 0.19)$
	U=399, p=0.817, d=0.04,	t(36.58) = -1.13, rp = 0.368, rd = -0.3, r	t(36.98) = -2.69, $p = 0.021$, $d = -0.71$,	t(36.98) = -2.69, $p = 0.021$, $d = -0.71$, $ t(35.97) = -2.58$, $p = 0.023$, $d = -0.68$,	U=313, p=0.144, d=0.22,
2	$E=0, \mu=-0.07(-0.63-0.37)$	$E=0, \mu = -0.29(-0.82 - 0.23)$	E=3, $\mu = -0.67(-1.17 - 0.17)$	$E=3, \mu = -0.64(-1.14 - 0.14)$	$E=1, \tau \mu = -0.39(-0.91-0.08)$
	Table A.22: Con	marisons of the mean of	adiacency matrix constru	Table A.22: Comparisons of the mean of adiacency matrix constructed with CBS in enoch 3. The results are	. The results are

Table A.22: Comparisons of the mean of adjacency matrix constructed with CBS in epoch 3. The results are
reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric
alternative), number of epochs where significant differences were observed (E), difference estimate μ with 95%
confidence interval. Reliable differences (significant in all three epochs) are highlighted with bold text.

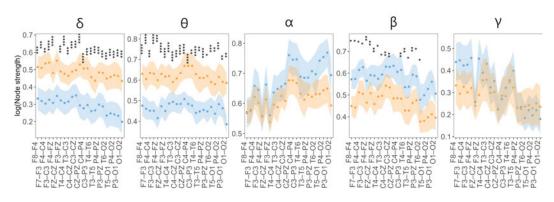


Figure A.14: Node strength (min-max normalised) measured with CS in epoch 3 of HC (blue) and AD (orange): mean with 95% confidence intervals. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "**", $p \le 0.01$ "**", and $p \le 0.05$ "*".

Table A.23: Comparisons of node strength measured with CS in epoch 3. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number
of epochs where significant differences were observed (E), and difference estimate μ with 95% confidence interval (CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

channel	¢	θ	σ	β	7
Ц 10 11 12	t(36.96)=-4.06, p<0.001, d=-1.07,	t(36.99)=-4.51, p<0.001, d=-1.18,	t(33.69)=-0.12, p=0.947, d=-0.03,	t(36.56)=4, $p=0.004$, $d=1.05$,	t(37)=1.81, $p=0.347$, $d=0.48$,
F 0-F 4	E=3, $\mu = -0.94$ (-1.41 -0.48)	E=3, $\mu = -1.02$ (-1.48 -0.57)	$E=0, \mu = -0.03$ (-0.56 0.49)	E=3, $\mu = 0.94 \ (0.47 \ 1.4)$	$E=0, \ \mu = 0.47$ (-0.05 0.98)
F7_F3	t(36.99)=-4.21, p<0.001, d=-1.11,	t(36.67)=-3.91, p<0.001, d=-1.03,	t(36.71)=0.15, p=0.947, d=0.04,	t(35.89)=3.78, $p=0.004$, $d=0.99$,	t(36.95)=2.67, p=0.115, d=0.7,
-	$E=3, \ \mu = -0.97 \ (-1.43 \ -0.51)$	$E=3, \ \mu = -0.92 \ (-1.39 \ -0.45)$	$E=0, \mu = 0.04 (-0.49 0.57)$	$E=3, \ \mu = 0.9 \ (0.42 \ 1.37)$	$E=0, \mu = 0.66 (0.17 1.16)$
F4-C4	t(36.95)=-5.09, p<0.001, d=-1.34,	t(32.04)=-5.41, p<0.001, d=-1.43,	t(30.83)=1, p=0.39, d=0.26,	U=563, $p=0.027$, $d=0.29$,	t(36.63)=1.65, p=0.399, d=0.43,
	$E=3, \mu = -1.11 (-1.55 -0.68)$	$E=3, \mu = -1.17 (-1.6 - 0.73)$	$E=0, \mu = 0.26$ (-0.26 0.78)	$E=3, \ \mu = 0.6 \ (0.06 \ 1.17)$	$E=0, \mu = 0.43$ (-0.09 0.94)
F3-C3	t(36.75)=-4.88, pi0.001, d=-1.28,		t(36.93)=1.18, p=0.349, d=0.31,	U=608, $p=0.008$, $d=0.38$,	U=536, $p=0.347$, $d=0.24$,
2) 2) 2	$E=2, \ \mu = -1.08$ (-1.52 -0.64)	$E=3, \ \mu = -1.09 \ (-1.54 \ -0.64)$	$E=0, \mu = 0.31 (-0.21 0.83)$	E=3, $\mu = 0.74 \ (0.21 \ 1.17)$	$E=0, \mu = 0.5$ (-0.04 1.11)
F.4-F.Z.	t(36.65)=-3.93, p<0.001, d=-1.03,	t(36.94)=-5.59, p<0.001, d=-1.47,	t(29.33)=0.07, $p=0.947$, $d=0.02$,	t(37)=2.88, $p=0.01$, $d=0.76$,	t(36.59)=2.35, p=0.171, d=0.62,
	E=3, $\mu = -0.92$ (-1.39 -0.45)	E=3, $\mu = -1.19$ (-1.61 -0.76)	$E=0, \ \mu = 0.02$ (-0.51 0.54)	$E=3, \ \mu = 0.71 \ (0.22 \ 1.21)$	$E=0, \mu = 0.59 (0.09 1.1)$
FZCZ.	t(36.56)=-4.7, p<0.001, d=-1.23,	t(36.28)=-4.48, p<0.001, d=-1.18,	t(34.16)=1.25, p=0.333, d=0.33,	t(33.61)=2.31, p=0.027, d=0.61,	U=450, $p=0.967$, $d=0.06$,
	$E=3, \ \mu = -1.05 \ (-1.5 \ -0.6)$	$E=3, \ \mu = -1.02 \ (-1.48 \ -0.56)$	$E=0, \mu = 0.32 (-0.2 0.84)$	$E=2, \mu = 0.59 (0.08 1.1)$	$E=0, \ \mu = 0.11 \ (-0.5 \ 0.62)$
F3-FZ	t(36.98) = -3.91, p < 0.001, d = -1.03,		t(32.14)=0.71, p=0.554, d=0.19,	t(35.75)=3.62, p=0.004, d=0.95,	t(35.6)=2.92, p=0.115, d=0.76,
	$E=3, \mu = -0.92 (-1.39 - 0.45)$	$E=3, \ \mu = -1.09 \ (-1.53 \ -0.65)$	$E=0, \ \mu = 0.18 \ (-0.34 \ 0.71)$	$E=3, \mu = 0.87 (0.39 1.35)$	$E=0, \mu = 0.72 (0.22 1.21)$
T4-C4	t(34.8)=-3.92, p<0.001, d=-1.02,	t(35.28)=-3.45, p=0.001, d=-0.91,	t(31.06)=1.12, p=0.363, d=0.29,	t(36.97)=2.06, p=0.044, d=0.54,	t(34.44)=0.57, $p=0.964$, $d=0.15$,
	$E=3, \mu = -0.91 (-1.38 - 0.45)$	$E=3, \mu = -0.83 (-1.32 - 0.35)$	$E=0, \mu = 0.29$ (-0.23 0.81)	$E=2, \ \mu = 0.53 \ (0.02 \ 1.04)$	$E=0, \mu = 0.15$ (-0.38 0.68)
$T_{3-C_{3}}$	t(36.63) = -3.51, p = 0.001, d = -0.92,		t(34.74)=1.9, p=0.131, d=0.5,	t(35.43) = 2.63, p = 0.016, d = 0.69,	U=485, $p=0.914$, $d=0.13$,
	$E=3, \mu = -0.84 (-1.32 - 0.36)$	$E=3, \mu = -0.64 (-1.15 - 0.14)$	$E=0, \mu = 0.49$ (-0.03 1.01)	$E=3, \mu = 0.66 \ (0.16 \ 1.16)$	$E=0, \mu = 0.31 (-0.3 \ 0.87)$
C4-CZ	t(35.21) = -3.41, $p = 0.001$, $d = -0.89$,	t(34.33) = -3.79, p = 0.001, d = -1,	t(31.98)=1.02, $p=0.39$, $d=0.27$,	t(34.91)=2.53, p=0.018, d=0.67,	U=458, p=0.964, d=0.08,
	$E=3, \mu = -0.82 \ (-1.3 \ -0.34)$	$E=3, \mu = -0.9 \ (-1.38 \ -0.42)$	$E=0, \mu = 0.27$ (-0.25 0.79)	$E=3, \mu = 0.64 \ (0.13 \ 1.14)$	$E=0, \mu = 0.12$ (-0.38 0.57)
C3-CZ	t(32.98) = -3.64, $p = 0.001$, $d = -0.95$, F = 3, $u = -0.86$, $(-1.33, -0.38)$	t $f(36.99) = -4.57$, $p < 0.001$, $d = -1.2$, $F = 3 \mu = -1.03 \ (-1.49 \ -0.58)$	t(31.5)=1.94, $p=0.131$, $d=0.51$, F=0, $u=0.49$ (-0.02.1)	t(36.31)=2.55, p=0.017, d=0.67, E=3, u=0.64 (0.14.1.14)	U=477, p=0.964, d=0.12, F=0, $u=0.23$ (-0.33 0.7)
	11-151 b/0 001 d-0.55	+(34.48)4.390.001	+(369)-235 -0.023 4-0.62	+(35.42)-3.54.5-0.04.4-0.03	11-441 967 4-0.04
CZ-PZ	$E=3, \mu = -1.17$ (-1.66 -0.66)	$E=3, \mu = -1.02 (-1.48 - 0.55)$	$\mathbf{E}=0, \ \mu = 0.59 \ (0.09 \ 1.1)$	$E=3, \mu = 0.85 (0.37 1.33)$	$\mathbf{E}=0, \ \mu = 0.07 \ (-0.46 \ 0.53)$
C4_P4	U=156, p<0.001, d=0.54,	U=141, p<0.001, d=0.57,	t(35.22)=1.94, $p=0.131$, $d=0.51$,	t(36.99)=2.89, p=0.01, d=0.76,	U=403, $p=0.967$, $d=0.03$,
F 1_FO	E=3, $\mu = -1.18$ (-1.68 -0.67)	E=3, $\mu = -1.24$ (-1.65 -0.72)	$E=0, \ \mu = 0.49 \ (-0.02 \ 1)$	E=3, $\mu = 0.71 \ (0.22 \ 1.21)$	$E=0, \ \mu = -0.06$ (-0.7 0.43)
C3-P3	U=181, $p<0.001$, $d=0.49$, $R=3$, $\mu=-1$, 11 , ℓ_1 , κ_4 , -0 , κ)	t(28.76) = -5.3, p < 0.001, d = -1.4, F = 3, n = -1.16 (-1.6 -0.73)	t(36.97)=2.2, p=0.093, d=0.58, p=0.58, p=0.5	t(36.91)=2.91, p=0.01, d=0.77, p=0.21, n=0.77, p=0.21, n=0.72, n=0.7	U=457, $p=0.964$, $d=0.08$, $E=0.13$ (-0.13 (-0.13 0 ee)
	+(35.96)4.11 + -0.01 - 41.08	+(34.50) - 4.35 1.10 $(-1.0 - 0.12)$	11 - 522 $2 - 0.00$ 1.00	+(35,30)-3, 7, 5-0, 01, 4-0, 71	+(34 08) - 0.15 - 0.10 (-0.10 0.00)
T4-T6	$E(33.390) = -4.11, P < 0.001, G = -1.00, E = 3, \mu = -0.95 (-1.41 -0.49)$	$E(34.39) = -4.33, P < 0.001, G = -1.13, E = 3, \mu = -1 (-1.46 - 0.54)$	$\mathbf{E} = 0.22$, $\mathbf{p} = 0.169$, $\mathbf{q} = 0.21$, $\mathbf{E} = 0.4$ (-0.09 0.98)	$\mathbf{E}=1, \ \mu=0.68$ (0.18 1.18)	$\mathbf{E} = 0, \mu = 0.04$ (-0.49 0.57)
и Е е	t(36.16)=-3.5, p=0.001, d=-0.92,	t(28.56)=-3.72, p=0.001, d=-0.98,	t(36.99)=1.78, $p=0.143$, $d=0.47$,	t(34.46)=2.58, $p=0.017$, $d=0.68$,	U=510, $p=0.542$, $d=0.18$,
01_01	$E=3, \ \mu = -0.84 \ (-1.32 \ -0.36)$	$E=3, \ \mu = -0.89 \ (-1.37 \ -0.41)$	$E=0, \mu = 0.46$ (-0.06 0.97)	E=3, $\mu = 0.65 \ (0.14 \ 1.15)$	$E=0, \mu = 0.34$ (-0.18 0.9)
P4-PZ	t(35.71) = -4.11, $p < 0.001$, $d = -1.07$,		t(34.46)=1.84, $p=0.137$, $d=0.48$,	t(34.29)=3.48, p=0.004, d=0.92, p=0.02, p=0.	U = 421, $p = 0.994$, $d = 0$,
	$E=3, \mu = -0.33$ (-1.41 -0.43) +(25 74)- 4 30 $\times >0.001$ A- 1 15	(00.0-00.1+1) 1111 $(-1.00-0.0+1+2)$	$E = 0, \mu = 0.41$ (-0.04 0.86)	$E=3, \mu = 0.04$ (0.30 1.32)	$\mathbf{L} = 0, \ \mu = 0.01 \ (-0.34 \ 0.31)$
P3-PZ	$E=3, \mu = -1 (-1.45 - 0.54)$	E=3, $\mu = -1.05$ (-1.5 -0.61)	$\mathbf{E}=1, \ \mu=0.74 \ (0.25 \ 1.23)$	$E=3, \mu = 0.73 (0.24 1.23)$	$\mathbf{E}=0, \ \mu=0.09 \ (-0.39 \ 0.53)$
CO at	U=179, $p<0.001$, $d=0.49$,	t(30.88)=-3.19, p=0.003, d=-0.85,	U=570, $p=0.073$, $d=0.31$,	t(32.84)=2.29, p=0.027, d=0.6,	U=369, p=0.964, d=0.08,
70-0T	E=3, $\mu = -1.18$ (-1.58 -0.66)	E=3, $\mu = -0.79$ (-1.29 -0.29)	$E=0, \ \mu = 0.55 \ (0.09 \ 1.02)$	$E=1, \ \mu = 0.57 \ (0.07 \ 1.08)$	$E=0, \ \mu = -0.13 \ (-0.75 \ 0.29)$
T5-01	U=167, $p<0.001$, $d=0.51$,	t(35.61)=-3.52, p=0.001, d=-0.93,	t(34.7)=3.24, p=0.016, d=0.86,	t(36)=3.27, p=0.006, d=0.87,	U=394, $p=0.967$, $d=0.03$,
	E=3, $\mu = -1.11$ (-1.63 -0.58)	$E=3, \mu = -0.85 (-1.34 - 0.37)$	$E=1, \mu = 0.79$ (0.3 1.28)	$E=2, \ \mu = 0.8 \ (0.31 \ 1.29)$	$E=0, \ \mu = -0.04 \ (-0.61 \ 0.39)$
P4-O2	U=164, p<0.001, d=0.5, W=2, $U=1.46$ (1.50 (5.00)	f(32.71) = -3.17, p = 0.003, d = -0.84, p = 0.003, d = -0.84, p = 0.003, d = -0.84, d = 0.84, d = 0.003, d = -0.84, d = 0.84,	t(36)=3.23, p=0.016, d=0.86, p=-1, z=-0.70, 0, 1, 26, p=-1, z=-0.70, 0, 1, 26, 0, 0, 1, 26, 0, 0, 1, 26, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,	t(35.38)=2.7, p=0.014, d=0.72, p=0.014, d=0.72, p=0.72, p=0.	U=387, p=0.967, d=0.04, E-0 = = 0.067 (0.61 0.03)
	$E=3, \mu = -1.18 (-1.09 -0.09)$	$E=3, \mu = -0.78 (-1.28 -0.29)$	$\mathbf{E} = \mathbf{I}, \ \mu = 0.79 \ (0.3 \ \mathbf{I}, \mathbf{Z6})$	$E=3, \mu = 0.08 (0.17 1.18)$	$\mathbf{E} = 0, \ \mu = -0.00 \ (-0.01 \ 0.32)$
P3-01	U=155, p < 0.001, d = 0.53, E=3, u = -1.17 (-1.67 -0.68)	F(26.51) = -2.89, $p = 0.006$, $d = -0.77$, F = 3, $u = -0.73$ (-1.23 -0.22)	t(35.96) = 3.66, p = 0.013, d = 0.97, E = 1, u = 0.88 (0.4 1.36)	t(34.03)=3.57, $p=0.004$, $d=0.95$, $E=3$, $u=0.86$ (0.38 1.35)	U=390, $p=0.994$, $d=0$, $E=0$, $u = -0.01$ (-0.59 0.37)
	U=118, p<0.001, d=0.6,		t(32.21)=3.07, p=0.017, d=0.82,	t(33.58)=3.11, p=0.008, d=0.83,	U=345, p=0.964, d=0.07,
20-10	$E=3, \ \mu = -1.25 \ (-1.61 \ -0.85)$	E=3, $\mu = -1.29$ (-1.7 -0.88)	$E=1, \mu = 0.76$ (0.26 1.26)	$E=1, \mu = 0.77 (0.27 1.27)$	$E=0, \ \mu = -0.1 \ (-0.57 \ 0.27)$

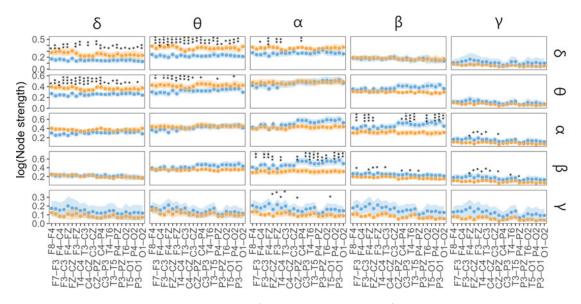


Figure A.15: Node strength (min-max normalised) measured with CBS in epoch 3 of HC (blue) and AD (orange): mean with 95% confidence intervals. The input frequency is on the vertical facets, and the output frequency is on the horizontal. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

Table A.24: Comparisons of node strength measured with CBS in epoch 3. The results are reported as follows:
statistics value (degrees of freedom), p-value of the test, Cohen's d effect size (or nonparametric alternative), number
of epochs where significant differences were observed (E), and difference estimate μ with 95% confidence interval
(CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

r.c.r.J		4	4		9	
110.11		0		α	d.	1
δ	F8-F4	U=237, $p=0.007$, $d=0.37$, $E=2$,	$t(35.41) = -4.39$, $p_i 0.001$, $d = -1.15$,	t(36.81)=-2.75, p=0.017, d=-	U=347, $p=0.527$, $d=0.15$, $E=0$,	U=419, p=1, d=0, E=0, $\mu = 0$
		μ =-0.77 (-1.43 -0.24)	E=3, μ =-1 (-1.45 -0.54)	0.72, E=2, μ =-0.68 (-1.18 -	μ =-0.19 (-0.58 0.23)	(-0.26 0.23)
				0.18)		
δ	F7-F3	$U=210$, $p=0.003$, $d=0.43$, $E=3$, $\dots = 0.80$ (1.4, 0.25)	$t(34.06) = -3.99, p_i 0.001, d = -1.05, p_{-2} \dots - 0.04 (1.14, 0.47)$	t(37)=-3.14, $p=0.009$, $d=-0.82$, r=2 $= -0.77$ ($1.2r$ 0.28)	U=343, $p=0.527$, $d=0.16$, $E=0$, $u=0.24$ (0.6 0.9)	U=408, $p=0.981$, $d=0.02$, $E=0$, $u=0.02$, $f=0$, $f=0$, $f=0$
s	F4-C4	$\mu = -0.00 (-1.1 - 0.00)$ 11=208. n=0.003. d=0.43. E=3.	t(36.96) = -4.3 $n(0.001 d = -1.13)$	t(36.72)=-3.73, n=0.003, d=-0.98.	$\mu = 0.22$ (200 0.2) 11=306. $\mu = 0.497. d = 0.23. F = 0.$	11=454. p=0.981. d=0.07. F=0.
>	4) 4	$\mu = -0.74 (-1.32 - 0.34)$		$E=3, \mu =-0.89 (-1.36 - 0.41)$	$\mu = -0.35$ (-0.7 0.04)	$\mu = 0.04$ (-0.1 0.16)
δ	F3-C3	U=224, $p=0.005$, $d=0.4$, $E=2$,	$t(36.92) = -4.33, p_i 0.001, d = -1.14,$	t(32.71)=-2.55, p=0.023, d=-	U=294, p=0.497, d=0.26, E=0,	U=439, p=0.981, d=0.04, E=0,
		μ =-0.73 (-1.24 -0.25)	E=3, μ =-0.99 (-1.45 -0.53)	0.67, E=2, μ =-0.63 (-1.13 -	μ =-0.3 (-0.64 0)	$\mu=0.02$ (-0.12 0.12)
				0.13)		
δ	F4-FZ	U=180, $p=0.002$, $d=0.49$, $E=2$,	$t(36.1) = -5.42$, $p_i 0.001$, $d = -1.43$,	t(35.97)=-4.74, p;0.001, d=-	U=346, $p=0.527$, $d=0.15$, $E=0$,	U=463, $p=0.981$, $d=0.09$, $E=0$,
		μ =-0.8 (-1.38 -0.43)	E=3, μ =-1.17 (-1.6 -0.73)	1.24, E=2, μ =-1.06 (-1.5 -0.61)	μ =-0.22 (-0.65 0.18)	μ =0.03 (-0.1 0.14)
8	FZ-CZ	U=222, p=0.004, d=0.4, E=3, μ =-	$t(36.92) = -4.33, p_i 0.001, d = -1.14,$	t(36.78)=-2.8, p=0.016, d=-	U=372, $p=0.592$, $d=0.1$, $E=0$,	U=440, $p=0.981$, $d=0.04$, $E=0$,
		0.72 (-1.3 -0.26)	E=3, μ =-0.99 (-1.45 -0.53)	0.74, E=2, μ =-0.69 (-1.19 -0.2)	μ =-0.19 (-0.61 0.22)	μ =0.02 (-0.12 0.09)
δ	F3-FZ	U=204, $p=0.003$, $d=0.44$, $E=3$,	$t(33.05)=-4.53$, $p_i0.001$, $d=-1.19$,	t(36.98) = -3.19, $p = 0.009$, $d = -0.84$,	U=355, $p=0.563$, $d=0.13$, $E=0$,	U=435, $p=0.981$, $d=0.03$, $E=0$,
		μ =-0.77 (-1.28 -0.37)	E=3, μ =-1.03 (-1.49 -0.58)	E=3, μ =-0.78 (-1.26 -0.29)	μ =-0.18 (-0.61 0.27)	μ =0.01 (-0.15 0.14)
δ	T4-C4	U=250, $p=0.013$, $d=0.35$, $E=3$,	t(36.93)=-3.08, $p=0.004$, $d=-0.81$,	t(32.23)=-1.65, p=0.122, d=-	U=362, $p=0.573$, $d=0.12$, $E=0$,	U=410, $p=0.981$, $d=0.02$, $E=0$,
		μ =-0.57 (-1.05 -0.14)	E=3, μ =-0.75 (-1.24 -0.26)	0.43, E=0, μ =-0.42 (-0.93 0.09)	μ =-0.23 (-0.68 0.25)	μ =-0.01 (-0.18 0.12)
δ	T3-C3	U=276, $p=0.029$, $d=0.29$, $E=3$,	t(37)=-2.55, $p=0.014$, $d=-0.67$,	U=306, $p=0.094$, $d=0.23$, $E=0$,	U=375, $p=0.596$, $d=0.09$, $E=0$,	U=445, $p=0.981$, $d=0.05$, $E=0$,
		μ =-0.54 (-1.06 -0.06)	E=3, μ =-0.64 (-1.14 -0.14)	μ =-0.36 (-0.92 0.04)	μ =-0.18 (-0.59 0.27)	μ =0.04 (-0.17 0.16)
δ	C4-CZ	U=256, $p=0.016$, $d=0.34$, $E=3$,	$t(36.89) = -4.23, p_i 0.001, d = -1.11,$	t(28.21)=-2.59, $p=0.023$, $d=-0.67$,	U=349, $p=0.527$, $d=0.15$, $E=0$,	U=411, $p=0.981$, $d=0.02$, $E=0$,
		μ =-0.59 (-1.05 -0.14)	E=3, μ =-0.97 (-1.44 -0.51)	E=3, μ =-0.64 (-1.13 -0.14)	μ =-0.31 (-0.75 0.21)	μ =-0.01 (-0.14 0.13)
δ	C3-CZ	U=285, $p=0.039$, $d=0.28$, $E=3$,	t(35.34)=-2.71, p=0.01, d=-	t(30.17)=-1.5, p=0.146, d=-	U=404, $p=0.848$, $d=0.03$, $E=0$,	U=468, $p=0.981$, $d=0.1$, $E=0$,
		$\mu = -0.42 \ (-0.88 \ -0.04)$	0.71, E=2, μ =-0.67 (-1.17 -	0.39, E=0, μ =-0.38 (-0.9 0.13)	μ =-0.05 (-0.43 0.4)	μ =0.05 (-0.11 0.19)
			0.17)			
δ	CZ-PZ	U=211, $p=0.003$, $d=0.43$, $E=3$,	$t(29.77) = -4.87$, $p_i 0.001$, $d = -1.29$,	t(36.97)=-4.32, $p=0.001$, $d=-1.13$,	U=398, $p=0.81$, $d=0.04$, $E=0$,	U=405, $p=0.981$, $d=0.03$, $E=0$,
		$\mu = -0.79 \ (-1.22 \ -0.33)$	E=3, μ =-1.09 (-1.54 -0.64)	E=3, $\mu =$ -0.99 (-1.45 -0.53)	μ =-0.08 (-0.52 0.4)	μ =-0.01 (-0.12 0.08)
δ	C4-P4	U=199, $p=0.002$, $d=0.45$, $E=3$,	$t(32.96) = -4.59$, $p_i 0.001$, $d = -1.21$,	t(36.64)=-3.52, p=0.004, d=-	U=341, $p=0.527$, $d=0.16$, $E=0$,	U=385, $p=0.981$, $d=0.07$, $E=0$,
		$\mu = -0.73 \; (-1.15 \; -0.33)$	E=3, μ =-1.04 (-1.5 -0.59)	0.92, E=2, μ =-0.84 (-1.32 -	μ =-0.23 (-0.6 0.21)	μ =-0.03 (-0.2 0.1)
				0.36)		
δ	C3-P3	U=233, $p=0.006$, $d=0.38$, $E=3$,	U=190, pi0.001, d=0.47, E=3, μ =-	t(36.16)=-2.95, p=0.014, d=-	U=423, $p=0.969$, $d=0.01$, $E=0$,	$U=420, p=1, d=0, E=0, \mu = 0$
		$\mu =$ -0.67 (-1.15 -0.21)	0.93 (-1.41 -0.51)	0.77, E=2, μ =-0.72 (-1.21 -	$\mu=$ 0.01 (-0.39 0.42)	(-0.2 0.14)
				0.23)		
ş	T4-T6	U=265, p=0.02, d=0.32, E=3, μ =- 0.54 (-0.99 -0.14)	t(34.98) = -3.25, $p = 0.003$, $d = -0.86$, E=3, $\mu = -0.79$ (-1.28 -0.3)	$t(34.95)=-2.82$, $p=0.016$, $d=-0.74$, $E=2$, $\mu =-0.69$ (-1.19 -0.2)	U=316, p=0.497, d=0.21, E=0, μ =-0.29 (-0.64 0.07)	U=394, p=0.981, d=0.05, E=0, $\mu =$ -0.02 (-0.15 0.09)

δ	T3-T5	U=288, p=0.04, d=0.27, E=3, $\mu = -$	t(36.51)=-2.56, p=0.014, d=-0.67,	t(35.53)=-1.3, p=0.2, d=-0.34,	U=388, $p=0.721$, $d=0.07$, $E=0$,	U=429, $p=0.981$, $d=0.02$, $E=0$,
			E=3, μ =-0.64 (-1.15 -0.14)	E=0, μ =-0.34 (-0.86 0.18)	μ =-0.12 (-0.5 0.36)	μ =0.01 (-0.17 0.16)
δ	P4-PZ	U=198, $p=0.002$, $d=0.45$, $E=3$,	$t(37) = -4.16$, $p_i 0.001$, $d = -1.09$, $E = 3$,	t(25.06)=-1.95, p=0.074, d=-	U=359, $p=0.573$, $d=0.12$, $E=0$,	U=408, $p=0.981$, $d=0.02$, $E=0$,
		μ =-0.74 (-1.2 -0.31)	μ =-0.96 (-1.43 -0.5)	0.51, $E=0$, $\mu =-0.49$ (-1 0.02)	μ =-0.18 (-0.61 0.27)	μ =-0.01 (-0.2 0.12)
δ	P3-PZ	U=287, p=0.04, d=0.27, E=3, $\mu = -$	t(35.97)=-3.39, $p=0.002$, $d=-0.89$,	U=324, $p=0.146$, $d=0.2$, $E=0$,	U=469, $p=0.592$, $d=0.1$, $E=0$,	U=432, $p=0.981$, $d=0.02$, $E=0$,
		0.52 (-1.01 -0.01)	E=3, μ =-0.81 (-1.3 -0.33)	μ =-0.38 (-0.87 0.13)	μ =0.16 (-0.27 0.64)	μ =0.01 (-0.11 0.13)
δ	T6-O2	U=228, $p=0.005$, $d=0.39$, $E=3$,	$U=175$, $p_i0.001$, $d=0.5$, $E=2$,	U=259, $p=0.022$, $d=0.33$, $E=2$,	U=307, $p=0.497$, $d=0.23$, $E=0$,	U=348, $p=0.981$, $d=0.15$, $E=0$,
		$\mu = -0.58 \ (-0.85 \ -0.23)$	μ =-0.79 (-1.12 -0.44)	μ =-0.54 (-0.93 -0.13)	μ =-0.2 (-0.46 0.02)	μ =-0.04 (-0.14 0.03)
δ	T5-01	U=267, p=0.02, d=0.31, E=3, $\mu = -$	t(33.99)=-3.42, p=0.002, d=-0.9,	t(34.13)=-2.17, p=0.047, d=-	U=349, $p=0.527$, $d=0.15$, $E=0$,	U=374, $p=0.981$, $d=0.09$, $E=0$,
		0.58 (-1.01 -0.1)	E=3, μ =-0.83 (-1.31 -0.34)	0.57, E=2, μ =-0.55 (-1.05 -	μ =-0.2 (-0.53 0.16)	μ =-0.02 (-0.16 0.06)
				0.04)		
δ	P4-O2	U=258, $p=0.016$, $d=0.33$, $E=3$,	U=211, $p=0.001$, $d=0.43$, $E=3$,	U=268, $p=0.027$, $d=0.31$, $E=2$,	U=345, $p=0.527$, $d=0.15$, $E=0$,	U=399, $p=0.981$, $d=0.04$, $E=0$,
		$\mu = -0.44 \ (-0.77 \ -0.09)$	μ =-0.72 (-1.19 -0.3)	μ =-0.55 (-0.98 -0.07)	$\mu=$ -0.15 (-0.42 0.12)	μ =-0.01 (-0.12 0.06)
δ	P3-O1	U=264, p=0.02, d=0.32, E=3, $\mu = -$	t(28.68) = -3.16, $p = 0.003$, $d = -0.84$,	t(37)=-2.42, p=0.027, d=-0.63,	U=370, $p=0.592$, $d=0.1$, $E=0$,	U=398, $p=0.981$, $d=0.04$, $E=0$,
		0.57 (-1.11 -0.11)	E=3, μ =-0.78 (-1.28 -0.28)	E=2, μ =-0.61 (-1.11 -0.1)	μ =-0.14 (-0.56 0.27)	μ =-0.01 (-0.15 0.06)
8	O1-O2	U=199, $p=0.002$, $d=0.45$, $E=3$,	U=144, p;0.001, d=0.56, E=3, $\mu = -$	U=195, $p=0.003$, $d=0.46$, $E=3$,	U=315, $p=0.497$, $d=0.21$, $E=0$,	U=348, $p=0.981$, $d=0.15$, $E=0$,
		μ =-0.56 (-0.9 -0.27)	0.92 (-1.33 -0.52)	μ =-0.75 (-1.1 -0.33)	μ =-0.24 (-0.51 0.06)	μ =-0.04 (-0.15 0.03)
θ	F8-F4	t(36.96) = -3.54, p = 0.002, d = -0.93,	t(36.9)=-2.92, p=0.012, d=-0.77,	t(36.26)=-1.29, p=0.828, d=-	U=487, $p=0.348$, $d=0.14$, $E=0$,	U=422, $p=0.982$, $d=0$, $E=0$,
		E=3, $\mu = -0.85$ (-1.33 -0.37)	E=3, μ =-0.72 (-1.21 -0.23)	0.34, E=0, μ =-0.33 (-0.85 0.19)	$\mu=$ 0.25 (-0.21 0.83)	$\mu=0.01$ (-0.36 0.34)
θ	F7-F3	$t(36.58) = -4.43, p_i 0.001, d = -1.17,$	t(35.49)=-3.33, $p=0.009$, $d=-0.88$,	t(36.86)=-1.78, p=0.621, d=-	t(36.99)=0.88, p=0.421,	U=476, $p=0.899$, $d=0.11$, $E=0$,
		E=3, μ =-1.01 (-1.47 -0.55)	E=3, μ =-0.81 (-1.29 -0.32)	0.47, E=0, μ =-0.46 (-0.97 0.06)	d=0.23, E=0, μ =0.23 (-0.3	μ =0.12 (-0.18 0.43)
					0.76)	
θ	F4-C4	$t(34.27) = -4.51$, $p_i 0.001$, $d = -1.19$,	t(35.56) = -3.78, $p = 0.005$, $d = -0.99$,	t(36.89)=-1.34, p=0.828, d=-	U=514, $p=0.216$, $d=0.19$, $E=0$,	U=527, $p=0.899$, $d=0.22$, $E=0$,
		E=3, μ =-1.03 (-1.49 -0.57)	E=3, μ =-0.9 (-1.37 -0.42)	0.35, E=0, μ =-0.35 (-0.87 0.17)	$\mu=$ 0.38 (-0.12 0.87)	μ =0.22 (-0.05 0.5)
θ	F3-C3	t(36.97)=-3.73, $p=0.001$, $d=-0.98$,	t(35.95)=-3.12, $p=0.009$, $d=-0.82$,	t(37)=-0.87, $p=0.828$, $d=-0.23$,	U=490, $p=0.341$, $d=0.14$, $E=0$,	U=530, $p=0.899$, $d=0.22$, $E=0$,
		E=3, μ =-0.88 (-1.36 -0.41)	E=3, μ =-0.76 (-1.26 -0.27)	E=0, μ =-0.23 (-0.75 0.3)	$\mu=$ 0.28 (-0.19 0.77)	μ =0.21 (-0.03 0.41)
θ	F4-FZ	$t(34.48) = -4.57$, $p_i 0.001$, $d = -1.2$,	t(36.46) = -4.14, $p = 0.003$, $d = -1.09$,	t(36.88)=-2.95, p=0.108, d=-	t(36.87)=-0.48, p=0.66, d=-	U=496, $p=0.899$, $d=0.16$, $E=0$,
		E=3, $\mu = -1.04$ (-1.49 -0.58)	E=3, μ =-0.96 (-1.43 -0.5)	0.77, $E=0, \mu =-0.72$ (-1.22 -	0.13, E=0, μ =-0.13 (-0.66 0.4)	μ =0.14 (-0.11 0.41)
				0.23)		
θ	FZ-CZ	t(36.82)=-3.46, $p=0.002$, $d=-0.91$,	U=297, $p=0.081$, $d=0.25$, $E=0$,	t(36.18)=-1.04, p=0.828, d=-	t(33.16)=1.62, p=0.195,	U=508, $p=0.899$, $d=0.18$, $E=0$,
		E=3, μ =-0.83 (-1.31 -0.35)	μ =-0.44 (-0.93 0.03)	0.27, E=0, μ =-0.27 (-0.79 0.25)	d=0.42, E=0, μ =0.42 (-0.1 0.93)	μ =0.11 (-0.06 0.26)
θ	F3-FZ	$t(33.35)=-4.27, p_i0.001, d=-1.13,$	U=213, $p=0.008$, $d=0.42$, $E=3$,	t(36.56)=-1.9, p=0.621, d=-	U=430, $p=0.883$, $d=0.02$, $E=0$,	U=492, $p=0.899$, $d=0.15$, $E=0$,
		E=3, μ =-0.99 (-1.45 -0.52)	μ =-0.72 (-1.21 -0.31)	0.5, E=0, μ =-0.49 (-1 0.03)	$\mu=0.01$ (-0.36 0.47)	μ =0.14 (-0.11 0.36)
θ	T4-C4	t(36.99)=-2.31, $p=0.031$, $d=-0.61$,	t(36.99)=-1.78, p=0.103, d=-	t(32.91)=-0.22, $p=0.997$, $d=-$	t(31.2)=1.46, $p=0.216$, $d=0.38$,	U=451, $p=0.946$, $d=0.06$, $E=0$,
		E=3, μ =-0.58 (-1.09 -0.08)	0.47, E=0, μ =-0.46 (-0.97 0.06)	0.06, E=0, μ =-0.06 (-0.58 0.47)	E=0, $\mu = 0.37$ (-0.14 0.89)	μ =0.06 (-0.28 0.33)
θ	T3-C3	t(35.94)=-2.18, $p=0.036$, $d=-0.57$,	U=360, $p=0.357$, $d=0.12$, $E=0$,	t(36.88)=0, p=0.997, d=0,	U=551, $p=0.096$, $d=0.27$, $E=0$,	U=485, $p=0.899$, $d=0.13$, $E=0$,
		E=3, μ =-0.55 (-1.07 -0.04)	μ =-0.25 (-0.73 0.29)	$E=0, \ \mu=0$ (-0.53 0.53)	$\mu=$ 0.5 (0.01 0.97)	μ =0.15 (-0.16 0.4)
θ	C4-CZ	t(36.98)=-3.03, p=0.006, d=-0.8,		t(29.25)=-0.23, p=0.997, d=-	U=491, $p=0.341$, $d=0.15$, $E=0$,	U=451, $p=0.946$, $d=0.06$, $E=0$,
		E=3, $\mu = -0.74$ (-1.23 -0.25)	μ =-0.33 (-0.79 0.2)	0.06, E=0, μ =-0.06 (-0.58 0.46)	$\mu=0.26$ (-0.19 0.8)	μ =0.04 (-0.2 0.25)

θ	C3-CZ	t(36.99)=-2.3, p=0.031, d=-0.6,	t(37)=-2.18, p=0.06, d=-0.57,	t(33.05)=-0.57, p=0.938, d=-	t(34.17)=1.41, p=0.225,	U=478, $p=0.899$, $d=0.12$, $E=0$,
		E=3, μ =-0.58 (-1.09 -0.07)	E=0, μ =-0.55 (-1.06 -0.04)	0.15, E=0, μ =-0.15 (-0.67 0.38)	d=0.37, E=0, μ =0.36 (-0.15	μ =0.11 (-0.12 0.36)
					0.88)	
θ	CZ-PZ	U=175, p _i 0.001, d=0.5, E=3, μ =-	U=223, p=0.009, d=0.4, E=3, $\mu = -$	t(36.36)=-0.26, p=0.997, d=-	U=618, $p=0.013$, $d=0.4$, $E=1$,	U=480, $p=0.899$, $d=0.12$, $E=0$,
		0.88 (-1.38 -0.44)	0.8 (-1.23 -0.3)	0.07, E=0, μ =-0.07 (-0.6 0.46)	$\mu=$ 0.66 (0.24 1.3)	$\mu = 0.08$ (-0.1 0.25)
θ	C4-P4	U=181, pi0.001, d=0.49, E=3, $\mu = -$	U=231, $p=0.009$, $d=0.39$, $E=3$,	t(36.87)=-0.19, p=0.997, d=-	U=611, $p=0.013$, $d=0.39$, $E=2$,	U=403, $p=0.946$, $d=0.03$, $E=0$,
		0.84 (-1.32 -0.37)	μ =-0.7 (-1.2 -0.27)	0.05, E=0, μ =-0.05 (-0.58 0.48)	$\mu=0.67~(0.24~1.28)$	μ =-0.03 (-0.28 0.19)
θ	C3-P3	U=230, $p=0.005$, $d=0.39$, $E=3$,	t(29.99)=-3.11, p=0.009, d=-0.82,	t(36.02)=-0.74, $p=0.828$, $d=-$	U=610, $p=0.013$, $d=0.39$, $E=1$,	U=416, p=0.982, d=0.01, E=0,
		$\mu = -0.79 \ (-1.28 \ -0.28)$	E=3, μ =-0.77 (-1.27 -0.27)	0.19, E=0, μ =-0.19 (-0.72 0.33)	$\mu=$ 0.64 (0.17 1.16)	μ =-0.01 (-0.24 0.19)
θ	T4-T6	t(34.38)=-2.76, p=0.012, d=-	t(35.43)=-2.63, p=0.023, d=-0.69,	t(34.88)=-0.1, p=0.997, d=-	U=536, $p=0.148$, $d=0.24$, $E=0$,	U=442, $p=0.946$, $d=0.04$, $E=0$,
		0.73, E=2, μ =-0.69 (-1.19 -	E=3, μ =-0.66 (-1.16 -0.16)	0.03, E=0, μ =-0.03 (-0.55 0.5)	$\mu=$ 0.55 (-0.06 1.28)	$\mu=$ 0.04 (-0.24 0.26)
		0.19)				
θ	T3-T5	t(35.99)=-2.17, p=0.036, d=-0.57,	t(28.64)=-1.69, p=0.118, d=-	t(36.81)=0.73, p=0.828,	U=605, $p=0.014$, $d=0.38$, $E=1$,	U=449, $p=0.946$, $d=0.06$, $E=0$,
		E=3, $\mu =$ -0.55 (-1.06 -0.04)	0.45, E=0, μ =-0.44 (-0.97 0.08)	d=0.19, E=0, μ =0.19 (-0.34	$\mu=$ 0.7 (0.22 1.23)	μ =0.07 (-0.21 0.36)
				0.72)		
θ	P4-PZ	t(36.01)=-3.53, p=0.002, d=-0.93,	U=264, $p=0.028$, $d=0.32$, $E=3$,	t(31.7)=-0.02, $p=0.997$, $d=0$,	U=534, $p=0.148$, $d=0.23$, $E=0$,	U=439, p=0.946, d=0.04, E=0,
		E=3, μ =-0.85 (-1.33 -0.37)	μ =-0.6 (-1.05 -0.11)	E=0, $\mu = 0$ (-0.53 0.52)	$\mu=$ 0.51 (-0.06 0.99)	$\mu = 0.04$ (-0.28 0.34)
θ	P3-PZ	t(36.17)=-2.07, p=0.044, d=-0.54,	t(36.1)=-1.95, p=0.081, d=-	t(31.87)=0.85, p=0.828,	U=591, $p=0.024$, $d=0.35$, $E=1$,	U=443, p=0.946, d=0.05, E=0,
		E=3, $\mu =$ -0.53 (-1.04 -0.02)	0.51, E=0, μ =-0.5 (-1.02 0.01)	d=0.22, E=0, μ =0.22 (-0.3	$\mu=$ 0.7 (0.15 1.2)	$\mu=$ 0.05 (-0.23 0.33)
				0.74)		
θ	T6-O2	U=250, $p=0.012$, $d=0.35$, $E=2$,	t(36.99)=-2.08, p=0.069, d=-	t(32.29)=0.8, p=0.828, d=0.21,	U=580, $p=0.031$, $d=0.33$, $E=1$,	U=377, $p=0.946$, $d=0.09$, $E=0$,
		μ =-0.57 (-0.98 -0.17)	0.55, E=0, μ =-0.53 (-1.04 -	$\mathbf{E}{=0,\ \mu=0.21}$ (-0.31 0.73)	$\mu=$ 0.43 (0.07 0.96)	μ =-0.04 (-0.2 0.07)
			0.02)			
θ	T5-01	t(34.07)=-2.2, p=0.036, d=-0.58,	t(35.44)=-1.29, p=0.221, d=-	t(32.26)=0.86, p=0.828,	t(32.37)=4.41, p=0.001,	U=423, $p=0.982$, $d=0.01$, $E=0$,
		E=3, μ =-0.56 (-1.08 -0.05)	0.34, E=0, μ =-0.34 (-0.86 0.19)	d=0.22, E=0, μ =0.22 (-0.3	d=1.15, E=1, μ =1 (0.54	μ =0.01 (-0.21 0.21)
				0.75)	1.45)	
θ	P4-O2	U=269, $p=0.026$, $d=0.31$, $E=3$,	t(31.59)=-1.86, p=0.093, d=-	t(36.93)=0.16, p=0.997,	U=581, $p=0.031$, $d=0.33$, $E=1$,	U=438, $p=0.946$, $d=0.04$, $E=0$,
		$\mu =$ -0.51 (-1.02 -0.09)	0.49, E=0, μ =-0.48 (-1 0.04)	d=0.04, E=0, μ =0.04 (-0.49	$\mu=$ 0.53 (0.13 1.06)	μ =0.02 (-0.14 0.16)
				0.57)		
θ	P_{3-01}	t(26.77)=-2.42, $p=0.027$, $d=-0.64$,	t(33.27)=-1.33, p=0.217, d=-	t(36.61)=0.89, p=0.828,	U=685, p;0.001, d=0.54, E=1,	U=435, $p=0.946$, $d=0.03$, $E=0$,
		E=3, μ =-0.62 (-1.13 -0.1)	0.35, E=0, μ =-0.35 (-0.88 0.18)	d=0.23, E=0, μ =0.23 (-0.29	$\mu=1~(0.56~1.46)$	$\mu=$ 0.03 (-0.22 0.18)
θ	01-02		U=242, $p=0.012$, $d=0.36$, $E=3$,	t(35.23)=-0.48, p=0.966, d=-	U=517, $p=0.216$, $d=0.2$, $E=0$,	U=362, p=0.899, d=0.12, E=0,
		$\mu =$ -0.75 (-1.16 -0.4)	μ =-0.69 (-1.13 -0.21)	0.13, E=0, μ =-0.13 (-0.65 0.4)	μ =0.38 (-0.1 0.91)	μ =-0.08 (-0.36 0.09)
σ	F8-F4	t(36.89)=-2.64, p=0.031, d=-	t(36.91)=-1.7, p=0.433, d=-	t(35.69)=0.84, p=0.466,	U=592, $p=0.011$, $d=0.35$, $E=2$,	U=541, $p=0.093$, $d=0.25$, $E=0$,
		0.69, E=2, μ =-0.66 (-1.16 -	0.45, E=0, μ =-0.44 (-0.95 0.08)	d=0.22, E=0, μ =0.22 (-0.3	$\mu=0.71~(0.18~1.15)$	$\mu=$ 0.24 (-0.02 0.53)
		0.16)		0.74)		
σ	F7-F3			=0.23,	U=572, $p=0.022$, $d=0.31$, $E=2$,	U=551, $p=0.093$, $d=0.27$, $E=0$,
		0.99, E=2, μ =-0.89 (-1.37 -	0.63, E=0, μ =-0.61 (-1.11 -0.1)	d=0.06, E=0, μ =0.06 (-0.47	$\mu=$ 0.53 (0.12 0.94)	$\mu=$ 0.28 (0.02 0.6)
		0.42)		0.6)		

A.4 Results for epoch 3

ъ	F4-C4	t(36.97)=-3.71, p=0.006, d=- 0.97, E=2, μ =-0.88 (-1.35 -0.4)	$t(36.96)=-1.8$, $p=0.433$, $d=-0.47$, $E=0$, $\mu =-0.46$ (-0.98 0.05)	U=512, p=0.207, d=0.19, E=0, μ =0.33 (-0.15 0.85)	t(36.15)=2.37, p=0.025, d=0.62, E=2, μ =0.6 (0.09 1.11)	U=606, p=0.026, d=0.38, E=3, $\mu = 0.42 (0.13 \ 0.78)$
σ	F3-C3	t(31.82)=-2.86, p=0.023, d=- 0.75, E=2, μ =-0.7 (-1.19 -0.21)	$t(36.98)=-1.39$, $p=0.656$, $d=-0.36$, $E=0$, $\mu=-0.36$ (-0.88 0.16)	t ((36.82)=1.05, p=0.358, d=0.28, E=0, μ =0.28 (-0.25 0.8) 0.8)	U=603, p=0.007, d=0.37, E=3, μ =0.72 (0.24 1.25)	U=597, p=0.031, d=0.36, E=3, μ =0.37 (0.13 0.66)
σ	F4-FZ	t(36.84)=-3.53, p=0.006, d=- 0.93, E=2, μ =-0.85 (-1.33 - 0.37)	t(36.5)=-3.11, p=0.069, d=- 0.82, E=0, μ =-0.76 (-1.25 - 0.27)	t (36.92)=-0.51, p=0.668, d=- 0.13, E=0, μ =-0.14 (-0.66 0.39)	t(36.79)=1.77, p=0.082, d=0.46, E=0, μ =0.45 (-0.06 0.97)	U=633, p=0.016, d=0.44, E=3, μ =0.41 (0.15 0.68)
σσ	FZ-CZ F3-FZ	t(36.32)=-2.26, p=0.072, d=- 0.59, E=0, μ =-0.57 (-1.07 - 0.06) t(37)=-2.19, p=0.075, d=-0.58,	t(36.51)=-0.69, $p=0.854$, $d=-0.18, E=0, \mu=-0.18 (-0.71 0.34)t(36.91)=-1.94$, $p=0.433$, $d=-$	t(36.86)=1.42, p=0.207, d=0.37, E=0, μ =0.37 (-0.15 0.89) t(36.97)=-0.19, p=0.851, d=-	U=610, p=0.005, d=0.39, E=2, $\mu = 0.66 (0.24 1.14)$ t(36.06)=2.5, p=0.021, d=0.66,	$\begin{array}{llllllllllllllllllllllllllllllllllll$
5 6	T4-C4	$E=0, \mu=-0.56 (-1.07 - 0.05), \mu=0.04$ t(31.89)=-0.29, p=0.774, d=- 0.08, E=0, μ =-0.08 (-0.6 0.45)	p=0.5(-1.010) p=0.854 0.14(-0.670)	$\frac{p-0.05}{p} (-0.58 \text{ (} -0.58 \text{ (} -0.58 \text{ (} -0.58 \text{ (} -0.58 \text{ (} -0.42 \text{ (} -0$	$ \begin{array}{l} \textbf{E}=2,\ \mu=0.66\ (0.15\ 1.23) \\ \mu=0.66\ (0.15\ 1.23) \\ \mu=0.66\ (0.15\ 1.23) \\ \end{array} $	Precost dread, (0.1 0.65) , p=0.093, d=0.25,] ; (-0.02 0.67)
σσ	T3-C3 C4-CZ	$\begin{array}{l} U{=}356, \ p{=}0.413, \ d{=}0.13, \ E{=}0, \\ \mu ={-}0.27 \ ({-}0.8 \ 0.26) \\ t(29.63){=}{-}2.04, \ p{=}0.089, \ d{=}{-} \\ 0.53, \ E{=}0, \ \mu \ {=}{-}0.52 \ ({-}1.02 \ {-} \\ 0.01) \end{array}$	$ \begin{array}{l} {\rm t}(34.8)\!=\!0.26,{\rm p}\!=\!0.919,{\rm d}\!=\!0.07,\\ {\rm E}\!=\!0,\mu=\!0.07(\!-\!0.470.6)\\ {\rm U}\!=\!426,{\rm p}\!=\!0.932,{\rm d}\!=\!0.01,{\rm E}\!=\!0,\\ \mu=\!0.05(\!-\!0.540.55)\\ \end{array} $	$\begin{array}{l} \mathrm{U}{=}536, \ \mathrm{p}{=}0.027, \ \mathrm{d}{=}0.34, \ \mathrm{E}{=}1, \\ \mu = 0.64 \ (0.19 \ 1.07) \\ \mathrm{U}{=}552, \ \mathrm{p}{=}0.071, \ \mathrm{d}{=}0.27, \ \mathrm{E}{=}0, \\ \mu = 0.43 \ (0.02 \ 0.92) \end{array}$	$ \begin{array}{l} \textbf{U=611, p=0.005, d=0.39, E=2,} \\ \mu=0.68 \; (0.25 \; 1.19) \\ \textbf{U=548, p=0.049, d=0.26, E=2,} \\ \mu=0.5 \; (0\; 1.03) \end{array} $	$\begin{array}{l} \mathrm{U}{=}538, \ \mathrm{p}{=}0.094, \ \mathrm{d}{=}0.24, \ \mathrm{E}{=}0, \\ \mu = 0.3 \ (-0.04 \ 0.59) \\ \mathrm{U}{=}506, \ \mathrm{p}{=}0.203, \ \mathrm{d}{=}0.18, \ \mathrm{E}{=}0, \\ \mu = 0.16 \ (-0.09 \ 0.45) \end{array}$
σσ	C3-CZ CZ-PZ	$\begin{array}{rllllllllllllllllllllllllllllllllllll$	t (35.2)=-0.89, p=0.854, d=- 0.23, E=0, μ =-0.23 (-0.75 0.29) t (36.6)=-0.73, p=0.854, d=- 0.19, E=0, μ =-0.19 (-0.72 0.34)	t (36.2)=1.43, p=0.207, d=0.37, E=0, μ =0.37 (-0.15 0.89) U=619, p=0.013, d=0.41, E=1, μ =0.74 (0.28 1.3)	$\begin{aligned} \mathbf{t}(36.09) = 2.14, \ \mathbf{p} = 0.04, \ \mathbf{d} = 0.56, \\ \mathbf{E} = 2, \ \mu = 0.54 \ (0.03 \ 1.05) \\ \mathbf{U} = 715, \ \mathbf{p} 0.001, \ \mathbf{d} = 0.6, \ \mathbf{E} = 3, \\ \mu = 1.02 \ (0.56 \ 1.49) \end{aligned}$	$\begin{array}{l} \textbf{U=546, p=0.093, d=0.26, E=0,}\\ \mu=0.24 \ (0 \ 0.51) \\ \textbf{U=586, p=0.036, d=0.34, E=3,}\\ \mu=0.29 \ (0.06 \ 0.56) \end{array}$
σσ	C4-P4 C3-P3	t(32.52)=-3.17, p=0.013, d=- 0.84, E=2, μ =-0.78 (-1.27 - 0.29) t(36.96)=-2.1, p=0.084, d=- 0.55, E=0, μ =-0.54 (-1.05 - 0.03)	t (36.99)=-1.18, p=0.802, d=- 0.31, E=0, μ =-0.31 (-0.83 0.22) t (36.16)=-0.62, p=0.854, d=- 0.16, E=0, μ =-0.16 (-0.69 0.37)		$ \begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{split} & \textbf{U}{=500}, \ \textbf{p}{=0.218}, \ \textbf{d}{=0.16}, \ \textbf{E}{=0}, \\ & \mu = 0.17 \ \textbf{(-0.11} \ 0.42) \\ & \textbf{U}{=537}, \ \textbf{p}{=0.094}, \ \textbf{d}{=0.24}, \ \textbf{E}{=0}, \\ & \mu = 0.2 \ \textbf{(-0.02} \ 0.44) \end{split}$
5 б	T4-T6	U=304, p=0.118, d=0.24, E=0, μ =-0.43 (-0.96 0.06) +(38.77)0.50 p=0.614 d=-	$t(36.95)=-0.65$, $p=0.854$, $d=-0.17$, $E=0$, $\mu=-0.17$ (-0.7 0.36)	t(34.54)=2.35, p=0.052, d=0.61, E=0, μ =0.59 (0.09 1.09)	$\begin{array}{cccc} U=651, & p=0.001, & d=0.47, & E=3, \\ \mu=0.9 & (0.45 \ 1.43) & & & \\ 11-656 & 5-0 & 001 & d=0.48 & F=2 \end{array}$	U=514, p=0.178, d=0.19, E=0, μ =0.22 (-0.08 0.48) U=554 p=0.03 d=0.27 E=0
σα	P4-PZ	u(30.12) = -0.03, $p=0.014$, $d=-0.15, E=0, \mu = -0.15 (-0.68 0.37)t(31.06)=-1.69, p=0.148, d=-0.44, E=0, \mu = -0.43 (-0.94 0.08)$	$E=0, \mu=0.07$ (-0.46 0.61) t(36.59)=-0.38, p=0.9, d=-0.1, E=0, $\mu=-0.1$ (-0.63 0.43)	$\mu(07) = 2.4$, $\mu = 0.004$, $\mu = 0.32$, E=0, $\mu = 0.56$ (0.05 1.07) U=578, $\mu = 0.034$, $d = 0.32$, E=1, $\mu = 0.64$ (0.13 1.17)	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{l} \mu = 0.34, \ p = 0.093, \ d = 0.24, \ p = 0.4, \\ \mu = 0.31 \ (0.01 \ 0.69) \\ \mu = 0.35, \ p = 0.093, \ d = 0.26, \ E = 0, \\ \mu = 0.35 \ (0 \ 0.72) \end{array}$
σ	P3-PZ	U=398, p=0.774, d=0.04, E=0, μ =-0.11 (-0.64 0.42)	t(37)=0.54, p=0.854, d=0.14, E=0, μ =0.14 (-0.39 0.67)	U=609, p=0.017, d=0.39, E=1, $\mu = 0.69 (0.23 1.24)$	t(36.72)=3.79, p=0.001, d=1, E=3, $\mu = 0.9 \ (0.42 \ 1.37)$	U=566, p=0.075, d=0.3, E=0, $\mu = 0.39$ (0.06 0.81)

б	T_{6-O2}	U=298, $p=0.103$, $d=0.25$, $E=0$,	t(35.21)=-0.13, p=0.932, d=-	U=604, $p=0.017$, $d=0.38$, $E=1$,	U=671, pi0.001, d=0.51, E=3,	U=501, $p=0.218$, $d=0.17$, $E=0$,
		μ =-0.42 (-0.83 0.01)	0.04, E=0, μ =-0.04 (-0.56 0.49)	$\mu=$ 0.79 (0.27 1.35)	$\mu = 0.88 \ (0.42 \ 1.37)$	μ =0.11 (-0.09 0.32)
σ	T5-O1	t(36.82)=-1.47, p=0.211, d=-	t(37)=0.43, p=0.9, d=0.11,	t(33.5)=3.44, $p=0.013$, $d=0.9$,	$t(35.83) = 4.96, p_i 0.001, d = 1.3,$	U=552, $p=0.093$, $d=0.27$, $E=0$,
		0.39, E=0, μ =-0.38 (-0.9 0.14)	$\mathbf{E}{=}0,\ \mu={0.11}$ (-0.42 0.64)	$\mathbf{E}{=}1,\ \mu = 0.82$ (0.34 1.3)	E=3, $\mu = 1.09 \ (0.65 \ 1.53)$	μ =0.26 (0.03 0.57)
σ	P4-O2	U=358, $p=0.413$, $d=0.13$, $E=0$,	t(36.78)=-0.11, p=0.932, d=-	t(36.6)=2.3, p=0.052, d=0.6,	U=643, $p=0.001$, $d=0.46$, $E=3$,	U=542, $p=0.093$, $d=0.25$, $E=0$,
		μ =-0.24 (-0.71 0.27)	0.03, E=0, μ =-0.03 (-0.56 0.5)	$\mathbf{E}{=}0,\ \mu={0.58}\ (0.08\ 1.09)$	$\mu = 0.93 \ (0.4 \ 1.4)$	μ =0.19 (-0.01 0.44)
σ	P3-O1	t(35.2)=-0.77, p=0.511, d=-	t(37)=0.74, p=0.854, d=0.19,	t(34.05)=3.3, $p=0.013$, $d=0.86$,	$U=714$, $p_i0.001$, $d=0.6$, $E=3$,	U=523, $p=0.142$, $d=0.21$, $E=0$,
		0.2, E=0, μ =-0.2 (-0.73 0.33)	$\mathbf{E}{=}0,\ \mu={0.19}$ (-0.33 0.72)	$\mathbf{E}{=}1,\ \mu={0}{.}79\ (0{.}31\ 1{.}28)$	$\mu = 1.15 \ (0.69 \ 1.62)$	μ =0.17 (-0.04 0.41)
σ	01-02	U=231, $p=0.013$, $d=0.39$, $E=2$,	t(36.88)=-0.77, p=0.854, d=-	U=515, $p=0.207$, $d=0.19$, $E=0$,	U=571, $p=0.022$, $d=0.31$, $E=3$,	U=512, $p=0.179$, $d=0.19$, $E=0$,
		$\mu =$ -0.68 (-1.09 -0.23)	0.2, E=0, μ =-0.2 (-0.73 0.32)	μ =0.35 (-0.13 0.95)	$\mu = 0.5 \ (0.07 \ 1.03)$	μ =0.16 (-0.05 0.44)
β	F8-F4	U=403, $p=0.962$, $d=0.03$, $E=0$,	U=440, $p=0.798$, $d=0.04$, $E=0$,	U=596, $p=0.007$, $d=0.36$, $E=2$,	U=531, $p=0.123$, $d=0.23$, $E=0$,	U=558, $p=0.05$, $d=0.28$, $E=0$,
		$\mu=$ -0.05 (-0.56 0.37)	μ =0.1 (-0.41 0.68)	$\mu=$ 0.76 (0.22 1.28)	$\mu=$ 0.27 (-0.06 0.67)	$\mu=$ 0.29 (0.03 0.58)
β	F7-F3	U=333, $p=0.947$, $d=0.18$, $E=0$,	U=391, $p=0.723$, $d=0.06$, $E=0$,	t(35.5)=1.88, $p=0.066$, $d=0.49$,	U=538, $p=0.103$, $d=0.24$, $E=0$,	U=573, $p=0.048$, $d=0.31$, $E=3$,
		μ =-0.27 (-0.77 0.17)	μ =-0.13 (-0.64 0.44)	$E=0, \ \mu=0.48$ (-0.03 1)	$\mu=$ 0.36 (-0.03 0.73)	$\mu = 0.33 (0.06 0.66)$
β	F4-C4	U=343, $p=0.947$, $d=0.16$, $E=0$,	t(32.08)=1.1, p=0.353, d=0.29,	U=617, $p=0.003$, $d=0.4$, $E=3$,	U=516, $p=0.151$, $d=0.2$, $E=0$,	U=602, $p=0.028$, $d=0.37$, $E=3$,
		$\mu=$ -0.25 (-0.69 0.14)	$\mathbf{E}{=}0,\ \mu={}0{.}29$ (-0.23 0.8)	$\mu = 0.72 \ (0.27 \ 1.18)$	$\mu=$ 0.27 (-0.1 0.68)	$\mu = 0.36 (0.09 0.77)$
β	F3-C3	U=352, $p=0.947$, $d=0.14$, $E=0$,	t(31.61)=1.21, p=0.334,	U=618, $p=0.003$, $d=0.4$, $E=3$,	U=575, $p=0.041$, $d=0.32$, $E=3$,	U=594, $p=0.029$, $d=0.36$, $E=3$,
		μ =-0.22 (-0.61 0.2)	d=0.32, E=0, μ =0.31 (-0.21	$\mu = 0.77 \; (0.33 \; 1.24)$	$\mu = 0.42 \ (0.07 \ 0.84)$	$\mu = 0.34 \; (0.12 \; 0.64)$
			0.83)			
β	F4-FZ	U=409, $p=0.962$, $d=0.02$, $E=0$,	t(36.08)=-0.19, p=0.847, d=-	t(36.99)=2.39, p=0.022,	U=598, $p=0.024$, $d=0.36$, $E=3$,	U=618, $p=0.028$, $d=0.4$, $E=3$,
		$\mu=$ -0.05 (-0.51 0.33)	0.05, E=0, μ =-0.05 (-0.58 0.48)	d=0.63, E=2, μ =0.6 (0.1	$\mu = 0.51 \ (0.17 \ 0.92)$	$\mu = 0.38 (0.15 0.65)$
				1.11)		
β	FZ-CZ	U=337, $p=0.947$, $d=0.17$, $E=0$,	t(30.79)=1.16, p=0.34, d=0.3,	U=596, $p=0.007$, $d=0.36$, $E=3$,	U=554, $p=0.061$, $d=0.27$, $E=0$,	U=575, $p=0.048$, $d=0.32$, $E=3$,
		μ =-0.3 (-0.77 0.12)	$\mathbf{E}{=}0,\ \mu={0.3}$ (-0.22 0.82)	$\mu = 0.67 \; (0.21 \; 1.14)$	$\mu=$ 0.45 (0.02 0.81)	$\mu = 0.24 (0.04 0.49)$
β	F3-FZ	U=402, $p=0.962$, $d=0.04$, $E=0$,	U=453, $p=0.708$, $d=0.07$, $E=0$,	t(37)=2.13, p=0.039, d=0.56,	U=602, $p=0.024$, $d=0.37$, $E=3$,	U=601, $p=0.028$, $d=0.37$, $E=3$,
		$\mu=$ -0.06 (-0.53 0.4)	$\mu=$ 0.13 (-0.33 0.57)	$\mathbf{E}{=}2,\ \mu={0.54}\ (0.03\ 1.05)$	$\mu = 0.56 \ (0.16 \ 0.99)$	$\mu = 0.35 \ (0.09 \ 0.68)$
β	T4-C4	U=427, $p=0.962$, $d=0.01$, $E=0$,	U=508, $p=0.288$, $d=0.18$, $E=0$,	U=615, $p=0.003$, $d=0.4$, $E=2$,	U=523, $p=0.143$, $d=0.21$, $E=0$,	U=551, $p=0.05$, $d=0.27$, $E=0$,
		$\mu=$ 0.03 (-0.45 0.48)	$\mu = 0.43$ (-0.18 0.96)	$\mu = 0.81 \; (0.32 \; 1.21)$	$\mu=$ 0.37 (-0.09 0.82)	$\mu=$ 0.26 (0.01 0.58)
β	T3-C3	U=441, p=0.962, d=0.04, E=0,	t(36.94) = 1.55, p = 0.242,	U=630, $p=0.002$, $d=0.43$, $E=3$,	U=487, $p=0.303$, $d=0.14$, $E=0$,	U=555, $p=0.05$, $d=0.28$, $E=0$,
		μ =0.06 (-0.39 0.53)	d=0.41, E=0, μ =0.4 (-0.12	μ =0.77 (0.35 1.22)	$\mu=0.23$ (-0.17 0.67)	$\mu=0.32~(0.02~0.58)$
			0.92)			
θ	C4-CZ	U=357, p=0.947, d=0.13, E=0,		U=603, $p=0.006$, $d=0.37$, $E=2$,	U=522, $p=0.143$, $d=0.21$, $E=0$,	U=528, $p=0.095$, $d=0.22$, $E=0$,
			$\mu=$ 0.27 (-0.18 0.87)	$\mu=0.69~(0.23~1.12)$	$\mu=0.37$ (-0.12 0.85)	$\mu = 0.2$ (-0.03 0.46)
β	C3-CZ		Шđ	U=593, $p=0.008$, $d=0.35$, $E=2$,	U=516, $p=0.151$, $d=0.2$, $E=0$,	U=567, $p=0.05$, $d=0.3$, $E=0$,
		$\mu=$ -0.09 (-0.59 0.48)	$d=0.23, E=0, \mu = 0.23$ (-0.29	$\mu=$ 0.64 (0.17 1.05)	$\mu=$ 0.32 (-0.12 0.77)	$\mu = 0.3 (0.03 0.65)$
			0.76)			
θ	CZ-PZ		U=582, $p=0.052$, $d=0.33$, $E=0$,		U=619, $p=0.024$, $d=0.41$, $E=3$,	U=589, $p=0.031$, $d=0.35$, $E=3$,
		$\mu=$ 0.22 (-0.25 0.66)	$\mu=$ 0.6 (0.12 1.11)	$\mu = 0.96 \; (0.53 \; 1.45)$	$\mu = 0.59 \ (0.2 \ 1.01)$	$\mu = 0.24 \ (0.07 \ 0.58)$
β	C4-P4	U=411, $p=0.962$, $d=0.02$, $E=0$,	U=570, $p=0.063$, $d=0.31$, $E=0$,		U=561, $p=0.054$, $d=0.29$, $E=0$,	U=530, $p=0.095$, $d=0.22$, $E=0$,
		μ =-0.05 (-0.46 0.38)	$\mu=$ 0.57 (0.1 1.1)	μ =0.95 (0.56 1.44)	$(0.06 \ 0.82$	μ =0.16 (-0.03 0.49)
β	C3-P3	U=469, $p=0.947$, $d=0.1$, $E=0$,			U=572, $p=0.041$, $d=0.31$, $E=3$,	=557,
		$\mu = 0.14$ (-0.27 0.62)	$\mu = 0.59 \ (0.11 \ 1.12)$	$\mu = 0.88 \ (0.45 \ 1.32)$	$\mu = 0.48 \ (0.08 \ 0.91)$	$\mu=0.21~(0.02~0.52)$

A.4 Results for epoch 3

β	T4-T6	U=407, p=0.962, d=0.03, E=0,	U=544, p=0.139, d=0.25, E=0,	U=664, pi0.001, d=0.5, E=3,	U=510, p=0.173, d=0.18, E=0,	U=552, p=0.05, d=0.27, E=0,
Q	П3_П5		11-5850 053 4-0 34 E-0		HI-621 -0113 4-0 21 E-0	
2	01_01	$\mu = 0.16 (-0.21 \ 0.67)$	$\mu = 0.68 (0.2 \ 1.24)$	P-0.002, u-0.42, (0.35 1.29)	$\mu = 0.35$ (-0.1 0.77)	
β	P4-PZ	U=421, $p=0.994$, $d=0$, $E=0$,	U=571, $p=0.063$, $d=0.31$, $E=0$,	U=642, $p=0.001$, $d=0.45$, $E=3$,	t(34.95)=2.45, $p=0.041$, $d=0.64$,	U=570, $p=0.049$, $d=0.31$, $E=3$,
		$\mu=0$ (-0.46 0.5)	μ =0.58 (0.1 1.08)	$\mu = 0.82 \ (0.39 \ 1.29)$	E=3, $\mu = 0.61$ (0.11 1.11)	$\mu = 0.37 \ (0.05 \ 0.75)$
β	P3-PZ	U=487, p=0.947, d=0.14, E=0,	U=582, $p=0.052$, $d=0.33$, $E=0$,	$U=665$, $p_i0.001$, $d=0.5$, $E=3$,	U=599, $p=0.024$, $d=0.37$, $E=3$,	U=599, $p=0.028$, $d=0.37$, $E=3$,
		$\mu=$ 0.21 (-0.23 0.63)	$\mu=$ 0.67 (0.14 1.24)	$\mu = 0.93 \ (0.4 \ 1.37)$	$\mu = 0.7 \ (0.2 \ 1.2)$	$\mu = 0.39 \ (0.12 \ 0.8)$
θ	T_{6-O2}	U=311, $p=0.947$, $d=0.22$, $E=0$,	U=539, $p=0.149$, $d=0.24$, $E=0$,	$U=659$, $p_i0.001$, $d=0.49$, $E=3$,	U=563, $p=0.054$, $d=0.29$, $E=0$,	U=528, $p=0.095$, $d=0.22$, $E=0$,
		μ =-0.24 (-0.52 0.05)	$\mu=$ 0.45 (-0.02 0.99)	$\mu = 0.88 \ (0.4 \ 1.52)$	$\mu=$ 0.35 (0.05 0.67)	μ =0.11 (-0.02 0.31)
θ	T5-O1	U=357, $p=0.947$, $d=0.13$, $E=0$,	t(33.87)=2.77, p=0.052,	$U=663$, $p_i0.001$, $d=0.5$, $E=3$,	U=591, $p=0.028$, $d=0.35$, $E=2$,	U=556, $p=0.05$, $d=0.28$, $E=0$,
		μ =-0.15 (-0.5 0.2)	d=0.72, E=0, μ =0.68 (0.19	μ =0.99 (0.5 1.53)	$\mu=$ 0.49 (0.14 0.88)	$\mu = 0.19 (0.01 0.43)$
			1.18)			
β	P4-O2	U=382, $p=0.962$, $d=0.08$, $E=0$,	U=515, $p=0.251$, $d=0.19$, $E=0$,	U=647, $p=0.001$, $d=0.46$, $E=3$,	U=559, $p=0.054$, $d=0.28$, $E=0$,	U=556, $p=0.05$, $d=0.28$, $E=0$,
		μ =-0.12 (-0.43 0.24)	$\mu = 0.44$ (-0.13 0.97)	$\mu = 0.86 \; (0.38 \; 1.41)$	$\mu=$ 0.4 (0.04 0.78)	$\mu=0.17~(0.01~0.43)$
β	P3-O1	U=412, $p=0.962$, $d=0.02$, $E=0$,	t(31.08)=3.11, p=0.052,	$U=691$, $p_i0.001$, $d=0.55$, $E=3$,	U=600, $p=0.024$, $d=0.37$, $E=2$,	U=557, $p=0.05$, $d=0.28$, $E=0$,
		$\mu=$ -0.02 (-0.43 0.39)	d=0.81, E=0, μ =0.75 (0.27	$\mu = 1.06 \ (0.63 \ 1.51)$	$\mu=$ 0.64 (0.21 1.06)	$\mu=$ 0.2 (0.01 0.51)
			1.24)			
β	01-02	U=379, $p=0.962$, $d=0.08$, $E=0$,	t(23.97) = 1.64, p = 0.226,	U=599, $p=0.007$, $d=0.37$, $E=2$,	U=573, $p=0.041$, $d=0.31$, $E=3$,	U=536, $p=0.083$, $d=0.24$, $E=0$,
		μ =-0.12 (-0.5 0.25)	d=0.43, E=0, μ =0.42 (-0.09	$\mu = 0.66 \; (0.22 \; 1.19)$	$\mu = 0.43 \ (0.1 \ 0.89)$	$\mu=$ 0.15 (-0.02 0.39)
			0.93)			
¢	F8-F4	U=439, $p=0.982$, $d=0.04$, $E=0$,	U=464, $p=0.894$, $d=0.09$, $E=0$,	U=556, $p=0.072$, $d=0.28$, $E=0$,	U=542, $p=0.084$, $d=0.25$, $E=0$,	U=525, $p=0.226$, $d=0.21$, $E=0$,
		$\mu=$ 0.06 (-0.29 0.31)	μ =0.12 (-0.28 0.52)	$\mu = 0.33 \; (0.04 \; 0.64)$	$\mu=$ 0.23 (-0.01 0.5)	μ =0.17 (-0.04 0.4)
¢	F7-F3	U=432, $p=0.982$, $d=0.02$, $E=0$,	U=420, p=1, d=0, E=0, $\mu = 0$	U=518, $p=0.142$, $d=0.2$, $E=0$,	U=576, $p=0.056$, $d=0.32$, $E=0$,	U=541, $p=0.198$, $d=0.25$, $E=0$,
		$\mu=0.02$ (-0.2 0.22)	(-0.39 0.37)	μ =0.21 (-0.06 0.58)	$\mu = 0.36 \ (0.08 \ 0.69)$	μ =0.19 (-0.01 0.38)
7	F4-C4	U=469, $p=0.982$, $d=0.1$, $E=0$,	U=504, $p=0.894$, $d=0.17$, $E=0$,	U=593, $p=0.038$, $d=0.35$, $E=3$,	U=562, $p=0.064$, $d=0.29$, $E=0$,	U=565, $p=0.136$, $d=0.3$, $E=0$,
		$\mu=$ 0.05 (-0.11 0.21)	μ =0.19 (-0.09 0.5)	$\mu = 0.44 \ (0.13 \ 0.78)$	$\mu=$ 0.3 (0.03 0.65)	$\mu=$ 0.18 (0.02 0.49)
7	F3-C3	U=481, $p=0.982$, $d=0.12$, $E=0$,	U=543, $p=0.894$, $d=0.25$, $E=0$,	U=606, $p=0.026$, $d=0.38$, $E=3$,	U=586, $p=0.053$, $d=0.34$, $E=0$,	U=583, $p=0.136$, $d=0.33$, $E=0$,
		$\mu=$ 0.08 (-0.08 0.21)	μ =0.27 (-0.02 0.57)	$\mu = 0.37 \ (0.11 \ 0.68)$	$\mu=$ 0.3 (0.08 0.58)	$\mu=$ 0.18 (0.05 0.34)
¢	F4-FZ	U=505, $p=0.982$, $d=0.17$, $E=0$,	U=486, $p=0.894$, $d=0.13$, $E=0$,	U=640, $p=0.011$, $d=0.45$, $E=3$,	U=599, $p=0.053$, $d=0.37$, $E=0$,	U=573, $p=0.136$, $d=0.31$, $E=0$,
		$\mu=$ 0.1 (-0.05 0.28)	μ =0.16 (-0.17 0.48)	$\mu = 0.54 \; (0.25 \; 0.89)$	$\mu=0.32~(0.1~0.6)$	μ =0.18 (0.03 0.38)
7	FZ-CZ	U=475, $p=0.982$, $d=0.11$, $E=0$,	U=511, $p=0.894$, $d=0.19$, $E=0$,	U=584, $p=0.043$, $d=0.34$, $E=3$,	U=589, $p=0.053$, $d=0.35$, $E=0$,	U=545, $p=0.198$, $d=0.26$, $E=0$,
		$\mu=$ 0.04 (-0.09 0.17)	μ =0.13 (-0.05 0.34)	$\mu = 0.29 \ (0.05 \ 0.56)$	$\mu=$ 0.22 (0.04 0.47)	$\mu = 0.08 \ (0 \ 0.19)$
¢	F_{3-FZ}	U=472, $p=0.982$, $d=0.11$, $E=0$,	U=513, $p=0.894$, $d=0.19$, $E=0$,	U=620, $p=0.018$, $d=0.41$, $E=3$,	U=594, $p=0.053$, $d=0.36$, $E=0$,	U=566, $p=0.136$, $d=0.3$, $E=0$,
		$\mu=$ 0.05 (-0.11 0.2)	μ =0.2 (-0.06 0.45)	$\mu = 0.5 \ (0.22 \ 0.81)$	$\mu = 0.35 \ (0.08 \ 0.65)$	$\mu=$ 0.17 (0.03 0.37)
¢	T4-C4	U=471, $p=0.982$, $d=0.1$, $E=0$,	U=469, $p=0.894$, $d=0.1$, $E=0$,	U=582, $p=0.043$, $d=0.33$, $E=3$,	U=543, $p=0.084$, $d=0.25$, $E=0$,	U=514, $p=0.248$, $d=0.19$, $E=0$,
		$\mu=$ 0.08 (-0.13 0.26)	μ =0.09 (-0.23 0.44)	$\mu = 0.4 \ (0.11 \ 0.73)$	$\mu=$ 0.22 (-0.01 0.59)	μ =0.11 (-0.05 0.3)
7	T3-C3	U=454, $p=0.982$, $d=0.07$, $E=0$,	U=499, $p=0.894$, $d=0.16$, $E=0$,	U=540, $p=0.086$, $d=0.25$, $E=0$,	U=544, $p=0.084$, $d=0.25$, $E=0$,	U=525, $p=0.226$, $d=0.21$, $E=0$,
		$\mu=$ 0.04 (-0.15 0.21)	μ =0.15 (-0.12 0.44)	μ =0.27 (-0.02 0.6)	$\mu=$ 0.25 (0 0.53)	μ =0.14 (-0.03 0.34)
7	C4-CZ	U=415, $p=0.982$, $d=0.01$, $E=0$, H=-0.01 (-0.17 0.15)	U=414, $p=0.974$, $d=0.01$, $E=0$, $U=-0.01$, $f=0$, $D=0.01$	U=456, $p=0.583$, $d=0.07$, $E=0$, $\mu = 0.08$ (-0.18 0.33)	U=520, p=0.128, d=0.2, E=0, 0.18 (_0.06.0.47)	U=504, $p=0.28$, $d=0.17$, $E=0$, $\mu = 0.07$ (20.05.0.21)
				(cc:c st:c-) cc:c- #		

Ľ	C3-CZ	U=474, $p=0.982$, $d=0.11$, $E=0$,	U=466, $p=0.894$, $d=0.09$, $E=0$,	U=539, $p=0.086$, $d=0.24$, $E=0$,	U=565, $p=0.064$, $d=0.3$, $E=0$,	U=551, $p=0.192$, $d=0.27$, $E=0$,
		$\mu=$ 0.06 (-0.09 0.23)	$\mu=$ 0.09 (-0.16 0.32)	μ =0.25 (-0.03 0.55)	$\mu=$ 0.25 (0.03 0.63)	$\mu=$ 0.12 (0 0.42)
~	CZ-PZ		U=471, $p=0.894$, $d=0.1$, $E=0$,	U=566, $p=0.069$, $d=0.3$, $E=0$,	U=579, $p=0.056$, $d=0.32$, $E=0$,	$U{=}517, \ p{=}0.248, \ d{=}0.2, \ E{=}0,$
		$\mu=0$ (-0.16 0.22)	μ =0.09 (-0.14 0.34)	$\mu=$ 0.29 (0.03 0.57)	$\mu=$ 0.21 (0.03 0.51)	μ =0.06 (-0.02 0.16)
~	C4-P4	U=414, $p=0.982$, $d=0.01$, $E=0$,	U=428, $p=0.974$, $d=0.02$, $E=0$,	U=534, $p=0.094$, $d=0.23$, $E=0$,	U=535, $p=0.09$, $d=0.23$, $E=0$,	U=473, $p=0.457$, $d=0.11$, $E=0$,
		μ =-0.01 (-0.15 0.14)	$\mu =$ 0.02 (-0.25 0.24)	$\mu=$ 0.23 (-0.03 0.49)	$\mu=$ 0.16 (-0.03 0.48)	μ =0.05 (-0.1 0.2)
~	C3-P3	U=434, $p=0.982$, $d=0.03$, $E=0$,	U=447, p=0.923, d=0.06, E=0,	U=552, $p=0.074$, $d=0.27$, $E=0$,	U=561, p=0.064, d=0.29, E=0,	U=513, $p=0.248$, $d=0.19$, $E=0$,
		μ =0.01 (-0.21 0.18)	μ =0.03 (-0.2 0.27)	$\mu=$ 0.23 (0.01 0.52)	$\mu=$ 0.21 (0.02 0.54)	μ =0.09 (-0.04 0.24)
."	T_{4-T6}	U=451, $p=0.982$, $d=0.06$, $E=0$,	U=456, $p=0.894$, $d=0.07$, $E=0$,	U=557, $p=0.072$, $d=0.28$, $E=0$,	U=518, $p=0.13$, $d=0.2$, $E=0$,	U=498, $p=0.311$, $d=0.16$, $E=0$,
		$\mu=$ 0.04 (-0.14 0.21)	μ =0.08 (-0.22 0.36)	$\mu=$ 0.32 (0.02 0.64)	$\mu=$ 0.17 (-0.06 0.47)	μ =0.08 (-0.08 0.25)
	T_{3-T_5}	U=439, $p=0.982$, $d=0.04$, $E=0$,	U=462, $p=0.894$, $d=0.09$, $E=0$,	U=539, $p=0.086$, $d=0.24$, $E=0$,	U=538, $p=0.086$, $d=0.24$, $E=0$,	U=534, $p=0.222$, $d=0.23$, $E=0$,
		$\mu=$ 0.02 (-0.17 0.22)	$\mu =$ 0.09 (-0.24 0.44)	μ =0.31 (-0.01 0.71)	$\mu=$ 0.27 (-0.03 0.57)	μ =0.15 (-0.02 0.41)
I	P4-PZ	U=431, p=0.982, d=0.02, E=0,	U=449, $p=0.923$, $d=0.06$, $E=0$,	U=510, $p=0.173$, $d=0.18$, $E=0$,	U=546, $p=0.084$, $d=0.26$, $E=0$,	U=506, $p=0.28$, $d=0.18$, $E=0$,
		$\mu=$ 0.01 (-0.11 0.18)	$\mu =$ 0.04 (-0.21 0.36)	$\mu=$ 0.26 (-0.11 0.7)	$\mu=$ 0.3 (0 0.71)	μ =0.1 (-0.05 0.27)
ł	P3-PZ	U=463, $p=0.982$, $d=0.09$, $E=0$,	U=474, p=0.894, d=0.11, E=0,	U=562, $p=0.069$, $d=0.29$, $E=0$,	U=570, $p=0.063$, $d=0.31$, $E=0$,	U=524, $p=0.226$, $d=0.21$, $E=0$,
		μ =0.04 (-0.09 0.25)	μ =0.12 (-0.16 0.43)	$\mu=$ 0.3 (0.04 0.71)	$\mu=$ 0.31 (0.06 0.65)	μ =0.1 (-0.03 0.27)
."	T6-02	U=406, $p=0.982$, $d=0.03$, $E=0$,	U=382, $p=0.894$, $d=0.08$, $E=0$,	U=525, $p=0.12$, $d=0.21$, $E=0$,	U=523, $p=0.126$, $d=0.21$, $E=0$,	U=466, $p=0.504$, $d=0.09$, $E=0$,
		μ =-0.01 (-0.22 0.09)	μ =-0.05 (-0.3 0.13)	$\mu=$ 0.17 (-0.02 0.4)	$\mu=$ 0.1 (-0.02 0.31)	μ =0.02 (-0.06 0.1)
. "	T5-01	U=398, $p=0.982$, $d=0.04$, $E=0$,	U=403, $p=0.967$, $d=0.03$, $E=0$,	U=549, $p=0.074$, $d=0.26$, $E=0$,	U=539, $p=0.086$, $d=0.24$, $E=0$,	U=483, $p=0.403$, $d=0.13$, $E=0$,
		μ =-0.02 (-0.16 0.13)	μ =-0.02 (-0.3 0.25)	$\mu=$ 0.21 (0.01 0.5)	μ =0.17 (-0.01 0.42)	μ =0.05 (-0.06 0.19)
н	P4-O2	U=398, $p=0.982$, $d=0.04$, $E=0$,	U=403, $p=0.967$, $d=0.03$, $E=0$,	U=564, $p=0.069$, $d=0.29$, $E=0$,	U=548, $p=0.084$, $d=0.26$, $E=0$,	U=495, $p=0.317$, $d=0.15$, $E=0$,
		μ =-0.02 (-0.14 0.09)	μ =-0.02 (-0.24 0.15)	$\mu=$ 0.25 (0.03 0.5)	$\mu=0.14~(0~0.38)$	μ =0.04 (-0.04 0.15)
H	P3-01	U=388, $p=0.982$, $d=0.07$, $E=0$,	U=433, $p=0.974$, $d=0.03$, $E=0$,	U=550, $p=0.074$, $d=0.27$, $E=0$,	U=550, $p=0.084$, $d=0.27$, $E=0$,	U=474, p=0.457, d=0.11, E=0,
		μ =-0.01 (-0.16 0.1)	μ =0.02 (-0.19 0.24)	$\mu=$ 0.21 (0 0.45)	$\mu=$ 0.16 (0 0.43)	μ =0.03 (-0.06 0.13)
<u> </u>	01-02	U=392, $p=0.982$, $d=0.06$, $E=0$,	U=374, $p=0.894$, $d=0.09$, $E=0$,	U=538, $p=0.086$, $d=0.24$, $E=0$,	U=522, $p=0.126$, $d=0.21$, $E=0$,	U=439, $p=0.775$, $d=0.04$, $E=0$,
		μ =-0.02 (-0.18 0.11)	μ =-0.06 (-0.42 0.14)	μ =0.24 (-0.02 0.7)	$\mu=$ 0.12 (-0.03 0.35)	μ =0.01 (-0.07 0.11)

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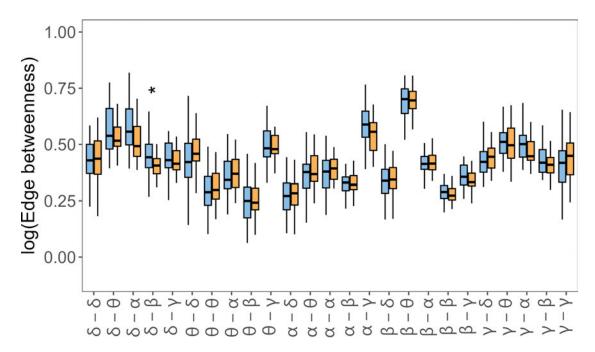


Figure A.16: Importance of each type of frequency coupling of HC (blue) and AD (orange) measured by edge betweenness in epoch 3. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.001$ "***", $p \leq 0.001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

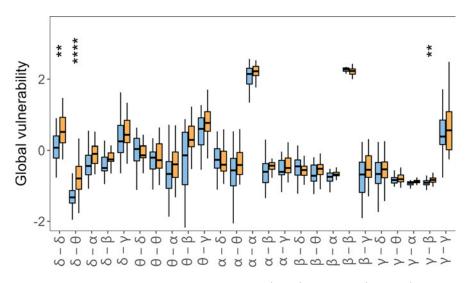


Figure A.17: Global vulnerability of HC (blue) and AD (orange) in epoch 3. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.0001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "**", $p \le 0.01$ "**", and $p \le 0.05$ "*".

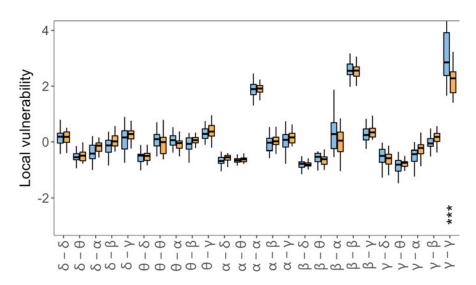


Figure A.18: Local vulnerability of HC (blue) and AD (orange) in epoch 3. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.001$ "***", $p \le 0.001$ "***", $p \le 0.01$ "**", $p \le 0.01$ "**", and $p \le 0.05$ "*".

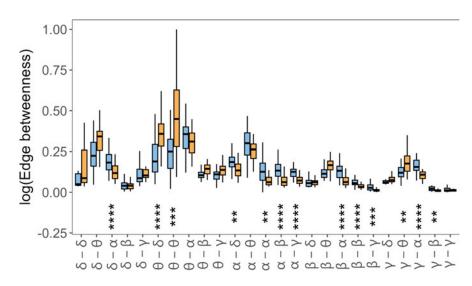


Figure A.19: Importance of each type of frequency coupling of HC (blue) and AD (orange) measured by weighted edge betweenness in epoch 3. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.0001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "**".

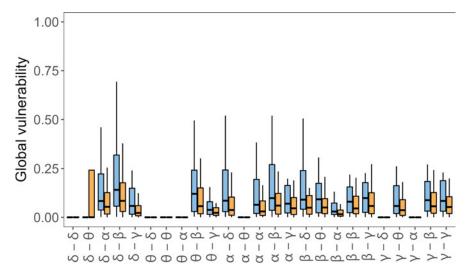


Figure A.20: Weighted global vulnerability of HC (blue) and AD (orange) in epoch 3. Significant differences ($p \leq 0.05$) observed in at least ten thresholded networks are encoded by asterisks.

The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \leq 0.0001$ "***", $p \leq 0.001$ "**", and $p \leq 0.05$ "*".

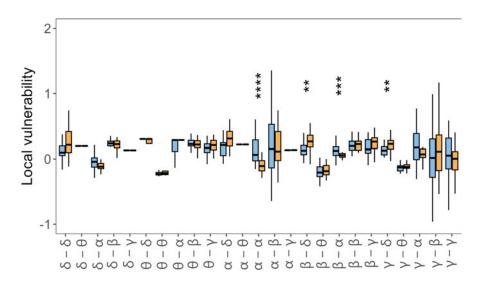


Figure A.21: Weighted local vulnerability of HC (blue) and AD (orange) in epoch 3. Significant differences ($p \le 0.05$) observed in at least ten thresholded networks are encoded by asterisks. The number of asterisks corresponds to the p-value (FDR corrected), i.e. $p \le 0.0001$ "***", $p \le 0.001$ "***", $p \le 0.001$ "**", $p \le 0.01$ "**", and $p \le 0.05$ "*".

The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted
 Table A.25: Results from epoch 3 comparing unweighted edge betweenness.
 with bold text.

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		δ	θ	σ	β	~
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	4	t(32.85)=-0.35, p=0.726, d=-0.09,	U=464, p=0.501, d=0.09,	U=539, $p=0.065$, $d=0.24$,	U=565, p=0.024, d=0.3,	U=479, p=0.365, d=0.12,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0	T=0, E=0, $\mu = -0.09$ (-0.62 0.43)	T=0, E=0, μ	T=2, E=0, $\mu = 0.44$ (-0.05 0.87)	$T=15, E=3, \mu = 0.49 (0.07 0.99)$	T=2, E=0, $\mu = 0.16$ (-0.22 0.5)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	9	t(31.84)=-0.92, p=0.364, d=-0.24,		t(36.82) = -0.81, $p = 0.423$, $d = -0.21$,	t(36.9)=-0.34, $p=0.735$, $d=-0.09$,	U=436, $p=0.811$, $d=0.03$,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	5	T=0, E=0, $\mu = -0.24$ (-0.76 0.28)	T=0, E=0, μ	T=0, E=0, $\mu = -0.21$ (-0.74 0.31)	T=0, E=0, $\mu = -0.09$ (-0.62 0.44)	T=0, E=0, $\mu = 0.05$ (-0.35 0.44)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	6	t(36.51)=-0.56, p=0.579, d=-0.15,	t(36.91) = -1.2, p = 0.235, d = -0.32, d =	t(32.72)=-0.93, p=0.356, d=-0.24,	t(33.58)=0.46, $p=0.651$, $d=0.12$,	t(36.14)=1.75, p=0.087, d=0.46,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3	T=0, E=0, $\mu = -0.15$ (-0.67 0.38)	T=0, E=0, $\mu = -0.31$ (-0.84 0.21)	T=0, E=0, $\mu = -0.24$ (-0.76 0.28)	T=0, E=0, μ = 0.12 (-0.41 0.64)	T=9, E=0, $\mu = 0.45$ (-0.07 0.96)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	a	t(35.71)=-0.42, p=0.674, d=-0.11,	t(34.17)=-0.95, p=0.345, d=-0.25,	t(33.59) = -0.12, p = 0.903, d = -0.03,	U=469, $p=0.453$, $d=0.1$,	U=516, $p=0.138$, $d=0.2$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	2	T=0, E=0, $\mu = -0.11$ (-0.64 0.42)	T=0, E=0, $\mu = -0.25$ (-0.77 0.27)	T=0, E=0, $\mu = -0.03$ (-0.56 0.49)	T=0, E=0, $\mu = 0.14$ (-0.22 0.53)	T=7, E=0, $\mu = 0.22$ (-0.05 0.55)
	i	U=360, p=0.357, d=0.12,	U=449, $p=0.66$, $d=0.06$,	U=530, $p=0.088$, $d=0.22$,	U=473, $p=0.417$, $d=0.11$,	t(36.95)=-1.15, p=0.255, d=-0.3,
	-	T=0, E=0, $\mu = -0.14$ (-0.46 0.19)	T=0, E=0, μ = 0.1 (-0.35 0.5)	T=8, E=0, $\mu = 0.29$ (-0.06 0.65)	T=0, E=0, μ = 0.17 (-0.18 0.56)	T=5, E=0, $\mu = -0.3$ (-0.82 0.22)

> Table A.26:
> Results from epoch 3 comparing unweighted global vulnerability.
> The results are reported as follows:
> statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	δ	θ	σ	β	×
4	t(33.04)=-3.27, p=0.002, d=-0.86,	$U=169, p_{1}0.001, d=0.51,$	t(35.18)=-3.15, p=0.003, d=-0.82,	U=264, p=0.015, d=0.32,	U=321, $p=0.126$, $d=0.2$,
0	T=16, E=3, $\mu = -0.8(-1.29 - 0.31)$	T=17, E=3, $\mu = -0.92(-1.38 - 0.49)$	T=14, E=1, $\mu = -0.76(-1.25 - 0.28)$	T=13, E=1, $\mu = -0.65(-0.97 - 0.18)$	T=6, E=0, $\mu = -0.3(-0.82 \ 0.09)$
9	t(35.29)=1.13, p=0.263, d=0.3,	U=411, $p=0.896$, $d=0.02$,	t(34.97)=-2.11, p=0.04, d=-0.55,	U=272, p=0.021, d=0.3,	U=316, $p=0.108$, $d=0.21$,
5	T=3, E=0, $\mu = 0.29(-0.23 \ 0.82)$	T=0, E=0, $\mu = -0.05(-0.59 \ 0.41)$	T=11, E=1, $\mu = -0.53(-1.04 - 0.03)$	T=12, E=1, $\mu = -0.63(-1.2 - 0.1)$	T=0, E=0, $\mu = -0.32(-0.77 \ 0.07)$
	t(31.62)=1.23, p=0.224, d=0.32,	U=319, $p=0.118$, $d=0.21$,	U=314, p=0.101, d=0.22,	U=268, p=0.018, d=0.31,	U=323, $p=0.134$, $d=0.2$,
3	T=6, E=0, $\mu = 0.32(-0.2 \ 0.84)$	T=1, E=0, $\mu = -0.35(-0.87 \ 0.11)$	T=7, E=0, $\mu = -0.31(-0.71\ 0.07)$	T=15, E=1, $\mu = -0.55(-1.01 - 0.09)$	T=5, E=0, $\mu = -0.31(-0.79 \ 0.1)$
a	U=512, p=0.156, d=0.19,	t(35.23)=-1.92, p=0.06, d=-0.5,	U=282, p=0.032, d=0.28,	U=532, p=0.083, d=0.23,	t(36.84)=-2.19, p=0.033, d=-0.57,
2	T=6, E=0, $\mu = 0.32(-0.09 \ 0.8)$	T=9, E=0, $\mu = -0.49(-1 \ 0.02)$	T=11, E=1, $\mu = -0.33(-0.7 - 0.06)$	T=8, E=0, $\mu = 0.38(-0.04\ 0.87)$	T=11, E=2, $\mu = -0.55(-1.06 - 0.05)$
1	t(36.99)=-0.6, p=0.549, d=-0.16,	t(36.84) = -1.12, p = 0.265, d = -0.29,	U=272, p=0.021, d=0.3,	t(33.74)=-3.15, p=0.003, d=-0.82,	U=360, p=0.357, d=0.12,
	$T=0, E=0, \mu = -0.16(-0.69 \ 0.37)$	$T=0, E=0, \mu = -0.29(-0.82 \ 0.23)$	T=13, E=1, $\mu = -0.36(-0.76 - 0.05)$	T=10, E=3, $\mu = -0.76(-1.25 - 0.28)$	T=1, E=0, $\mu = -0.2(-0.58 \ 0.24)$

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β 7	-0.71, $t(34.69)=-2.65$, $p=0.01$, $d=-0.69$, $U=336$, $p=0.195$, $d=0.17$,	-0.18) T=14, E=1, $\mu = -0.66$ (-1.15 -0.16) T=2, E=0, $\mu = -0.26$ (-0.81 0.1)	0.47, U=299, p=0.06, d=0.25, t(36.96)=-1.43, p=0.157, d=-0.38, t=0.38, t=0.	$1.98) \qquad T=9, E=0, \ \mu=-0.53 \ (-1.05 \ 0.03) \qquad T=4, E=0, \ \mu=-0.37 \ (-0.89 \ 0.15)$	0.31, $t(36.81)=-1.33$, $p=0.189$, $d=-0.35$, $U=301$, $p=0.065$, $d=0.24$,	0.21) T=3, E=0, $\mu = -0.35$ (-0.87 0.17) T=8, E=0, $\mu = -0.43$ (-0.94 0.03)	$t_{\rm c}$ t $t_{\rm c}(36.58)=0.26$, $p=0.795$, $d=0.07$, $t_{\rm c}(36.81)=-1.76$, $p=0.083$, $d=-0.46$, $t_{\rm c}(36.81)=-1.76$, $p=0.083$, $d=-0.46$, $t_{\rm c}(36.81)=-1.76$, $t_{\rm c}(36.51)=-1.76$,	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2, t(32.6)=-1.98, p=0.053, d=-0.52, U=630, p=0.001, d=0.43,	1.11) T=8, E=0, $\mu = -0.5$ (-1.01 0.01) T=12, E=3, $\mu = 0.28$ (0.11 0.49)
σ	t(35.06)=-2.72, $p=0.009$, $d=-0.71$,	T=12, E=1, $\mu = -0.67$ (-1.17 -0.18)	t(36.64)=1.78, $p=0.081$, $d=0.47$,	T=6, E=0, $\mu = 0.46$ (-0.06 0.98)	t(33.04)=-1.19, $p=0.24$, $d=-0.31$,	T=6, E=0, $\mu = -0.31$ (-0.83 0.21)	U=527, p=0.098, d=0.22,	T=4, E=0, $\mu = 0.41$ (-0.07 0.97)	U=264, $p=0.015$, $d=0.32$,	T=12, E=1, $\mu = -0.6$ (-1 -0.11)
θ	t(33.67)=-1.38, $p=0.174$, $d=-0.36$,	T=2, E=0, $\mu = -0.36$ (-0.89 0.16)	t(33.16)=1.79, p=0.08, d=0.47,	T=4, E=0, $\mu = 0.46$ (-0.06 0.98)	t(37)=-1.27, $p=0.209$, $d=-0.33$,	T=0, E=0, $\mu = -0.33$ (-0.85 0.19)	t(35.31)=1.78, p=0.08, d=0.47,	T=7, E=0, $\mu = 0.46$ (-0.06 0.98)	t(35.53)=-0.95, $p=0.345$, $d=-0.25$,	T=0, E=0, $\mu = -0.25$ (-0.77 0.27)
δ	t(32.88)=0.57, p=0.569, d=0.15,	T=0, E=0, $\mu = 0.15$ (-0.37 0.67)	t(36.88) = -0.99, p = 0.327, d = -0.26,	T=4, E=0, $\mu = -0.26$ (-0.78 0.27)	t(34.25)=-2.05, $p=0.045$, $d=-0.54$,	T=10, E=1, $\mu = -0.52$ (-1.03 -0.01)	U=447, $p=0.682$, $d=0.06$,	T=0, E=0, μ = 0.11 (-0.4 0.46)	t(36.34) = 1.21, p = 0.233, d = 0.32,	$T=0, E=0, \mu = 0.31 (-0.21 0.84)$

Table A.28: Results from epoch 3 comparing weighted edge betweenness. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were observed (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		δ	θ	σ	β	λ
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	x	U=595, $p=0.005$, $d=0.37$,	$U=651, p_{1}0.001, d=0.5,$	$U=677$, p $_{1}0.001$, d $=0.53$,	$U=697.5$, p $_{1}0.001$, d $=0.57$,	t(24.74)=3.38, $p=0.002$, $d=0.88$,
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	0	T=13, E=3, $\mu = 0.13$ (0 0.31)		T=13, E=3, $\mu = 0.6$ (0.2 1.16)	T=19, E=3, $\mu = 0.3$ (0.15 0.61)	T=16, E=3, $\mu = 0.8$ (0.32 1.28)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	0	U=658, p;0.001, d=0.49,	U=570, p=0.019, d=0.31,	U=477.5, p=0.093, d=0.22,	U=396, $p=0.579$, $d=0.07$,	t(36.87)=-0.96, $p=0.341$, $d=-0.25$,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	ь	T=12, E=3, $\mu = 0.82$ (0.35 1.3)	T=11, E=3, $\mu = 0.62$ (T=4, E=0, $\mu = 0 \ (0 \ 0)$	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = -0.25$ (-0.78 0.27)
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	ć	U=520, $p=0.076$, $d=0.23$,	U=344, p=0.159, d=0.19,	U=437, p=0.75, d=0.04,	U=397.5, p=0.664, d=0.06,	U=333, p=0.18, d=0.18,
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3	T=7, E=0, $\mu = 0 \ (0 \ 0.01)$	T=6, E=0, $\mu = 0$ (-0.04 0)	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=4, E=0, $\mu = -0.05$ (-0.16 0.03)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	q	$U=675$, p $_{1}0.001$, d $=0.52$,	U=456, p=0.583, d=0.07,	U=350, p=0.179, d=0.18,	U=381, p=0.548, d=0.08,	$U=176$, $p_i0.001$, $d=0.5$,
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2	T=19, E=3, $\mu = 0.54$ (0.29 0.98)	T=0, E=0, μ = 0.09 (-0.35 0.38)	T=3, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = -0.01$ (-0.05 0.01)	T=19, E=3, $\mu = -0.75$ (-1.12 -0.34)
T=5. $\mathbb{R}=0$. $u = -0.23$ (-0.59 0.1) T=2. $\mathbb{R}=0$. $u = -0.08$ (-0.26 0.06)	i	U=613, $p=0.002$, $d=0.39$,	U=336, p=0.195, d=0.17,	U=350, p=0.282, d=0.14,	U=171, p _i 0.001, d=0.51,	$t(36.92)=-3.88$, $p_10.001$, $d=-1.02$,
	<i>k</i>	$T=14, E=3, \mu = 0.9 (0.4 1.42)$	T=5, E=0, $\mu = -0.23$ (-0.59 0.1)	T=2, E=0, $\mu = -0.08$ (-0.26 0.06)	T=18, E=3, $\mu = -0.74$ (-1.36 -0.35)	T=19, E=3, $\mu = -0.91$ (-1.38 -0.44)

Table A.29: Results from epoch 3 comparing weighted global vulnerability. The results are reported as follows: statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

				0	
	0	۵	σ	d	Å
x	U=466, p=0.482, d=0.09,	U=451, p=0.638, d=0.06,	U=514, $p=0.147$, $d=0.19$,	U=626, $p=0.001$, $d=0.42$,	U=581, $p=0.012$, $d=0.33$,
0	T=1, E=0, $\mu = 0 \ (0 \ 0)$	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=4, E=0, $\mu = 0 \ (0 \ 0)$	T=17, E=3, $\mu = 0.23$ (0.02 0.95)	T=15, E=2, $\mu = 0.68 (0.2 \ 1.12)$
0	U=453, $p=0.616$, $d=0.07$,	U=441, p=0.752, d=0.04,	U=399, $p=0.752$, $d=0.04$,	U=440, $p=0.763$, $d=0.04$,	t(32.07)=0.4, p=0.69, d=0.1,
ь	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0.1$ (-0.42 0.63)
ć	U=517, $p=0.134$, $d=0.2$,	U=404, p=0.811, d=0.03,	U=389, $p=0.638$, $d=0.06$,	U=404, $p=0.811$, $d=0.03$,	t(30.11) = -1.11, p = 0.275, d = -0.29,
3	T=2, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0$ (-0.12 0.01)	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=2, E=0, $\mu = -0.29$ (-0.8 0.23)
æ	$U=659$, p $_{1}0.001$, d $=0.49$,	U=390, p=0.649, d=0.06,	U=451, $p=0.638$, $d=0.06$,	U=365, p=0.399, d=0.11,	$U=135$, $p_i0.001$, $d=0.58$,
2	T=10, E=3, $\mu = 0.65$ (0.03 1.1)	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=0, E=0, $\mu = 0 \ (0 \ 0)$	T=20, E=3, $\mu = -0.95$ (-1.32 -0.55)
õ	U=453, $p=0.616$, $d=0.07$,	U=442, $p=0.74$, $d=0.04$,	U=388, $p=0.627$, $d=0.07$,	t(36.03)=-4.75, p _i 0.001, d=-1.24,	$U=176$, p $_{1}0.001$, d $=0.5$,
-	T=1, E=0, $\mu = 0.15 (-0.41 \ 0.7)$	T=0, E=0, μ = 0.02 (-0.26 0.27)	T=0, E=0, $\mu = -0.14$ (-0.62 0.4)	T=0, E=0, $\mu = -0.14$ (-0.62 0.4) T=16, E=3, $\mu = -1.06$ (-1.5 -0.61)	T=18, E=3, $\mu = -0.99$ (-1.4 -0.51)

statistics value (degrees of freedom), p-value of the test, Cohen's d effect size or nonparameteric alternative, number of thresholds where significant differences were observed (T), number of epochs where significant differences were **Table A.30:** Results from epoch 3 comparing weighted local vulnerability. The results are reported as follows: (E), group difference estimate (95% CI). Reliable differences (significant in all three epochs) are highlighted with bold text.

	8	θ	σ	β	λ
δ	$U=651, p_{10}.001, d=0.47, T=20, E=0, u=0.85 (0.43, 1.22)$	U=591, p=0.007, d=0.35, T=14 E=1 = 0.71 (0.19, 1.19)	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	t(36.97)=-5.04, pi0.001, d=-1.32, T-15 E-3 = -1 11 (-1 55 -0.67)	U=470, p=0.444, d=0.1, T=0 $E=0$, $u = 0.19$ (-0.33.0.6)
đ	$t(25.91) = 4$, $p_10.001$, $d=1.04$,	t(31.29)=2.94, $p=0.005$, $d=0.78$,	U=270, $p=0.019$, $d=0.31$,	t(33.76) = -3.42, $p = 0.001$, $d = -0.89$,	U=378, $p=0.521$, $d=0.09$,
>	T=19, E=0, $\mu = 0.92 \ (0.46 \ 1.38)$	T=14, E=1, $\mu = 0.73 \ (0.23 \ 1.23)$	T=12, E=0, $\mu = -0.6$ (-0.99 -0.1)	T=16, E=0, $\mu = -0.82$ (-1.3 -0.34)	T=0, E=0, $\mu = -0.13$ (-0.49 0.26)
Ċ	t(28.9)=3.6, p=0.001, d=0.94,	t(36.71)=2.34, $p=0.023$, $d=0.61$,	U=280, p=0.029, d=0.29, d=0.	U=215, $p=0.001$, $d=0.42$,	U=361, p=0.365, d=0.12,
3	T=19, E=0, $\mu = 0.85 \ (0.37 \ 1.32)$	T=13, E=0, $\mu = 0.59 (0.08 \ 1.1)$	T=11, E=0, $\mu = -0.5$ (-0.94 -0.04)	T=15, E=0, $\mu = -0.68$ (-1.03 -0.29)	T=5, E=0, $\mu = -0.16$ (-0.67 0.22)
ø	$t(34.02)=4.25, p_10.001, d=1.11,$	t(34.1)=2.65, p=0.011, d=0.7,	U=320, p=0.122, d=0.2,	U=223, $p=0.002$, $d=0.4$,	U=311, p=0.092, d=0.22,
5	T=18, E=3, $\mu = 0.97$ (0.51 1.43) T=14, E=0, $\mu = 0.67$ (0.16 1.17)	T=14, E=0, $\mu = 0.67 (0.16 \ 1.17)$	T=6, E=0, $\mu = -0.42$ (-0.89 0.11)	T=14, E=0, $\mu = -0.55$ (-0.85 -0.21)	T=9, E=0, $\mu = -0.32$ (-0.77 0.05)
i	t(32.21)=1.26, p=0.213, d=0.33, d=0.	t(35.92)=1.07, p=0.29, d=0.28,	U=493, $p=0.261$, $d=0.15$,	t(37)=-2.64, $p=0.011$, $d=-0.69$,	t(36.16)=-3.28, p=0.002, d=-0.86,
-	T=0, E=0, μ = 0.33 (-0.19 0.84)	T=2, E=0, $\mu = 0.28$ (-0.25 0.81)	T=0, E=0, μ = 0.19 (-0.19 0.44)	T=12, E=3, $\mu = -0.66$ (-1.16 -0.16) T=13, E=3, $\mu = -0.79$ (-1.28 -0.31)	T=13, E=3, $\mu = -0.79$ (-1.28 -0.31)

Appendix B

Additional results from EEG-based Graph Neural Network Classification: An Empirical Evaluation of Functional Connectivity Methods (Chapter 5)

B.1 Comparison of node features - power spectral density

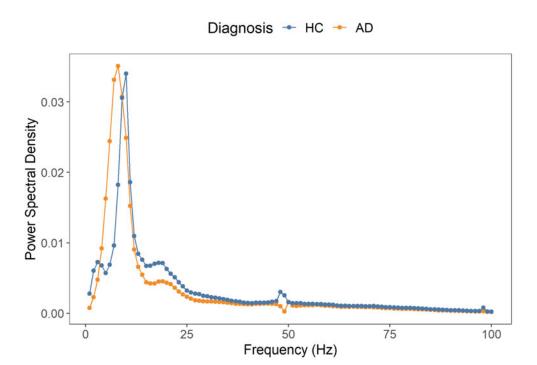
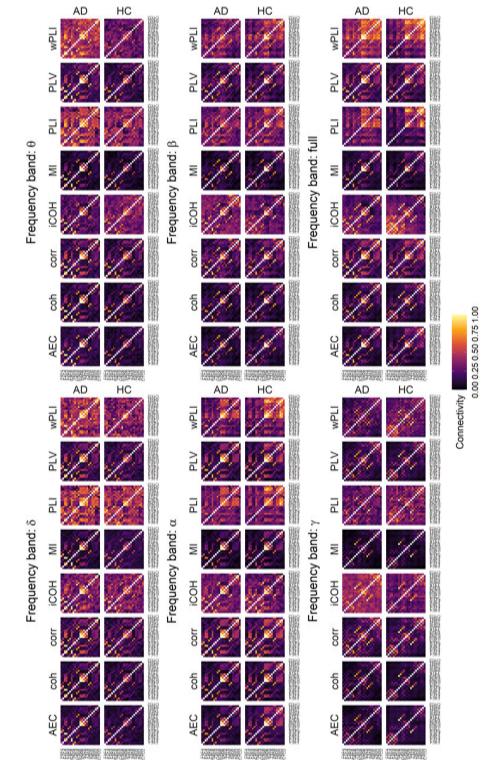


Figure B 1. Averaged node features



Comparison of functional connectivity measures B.2

Figure B.2: Averaged adjacency matrices of AD and HC cases measured with various functional connectivity measures

B.3 Effect of frequency bands on model performance

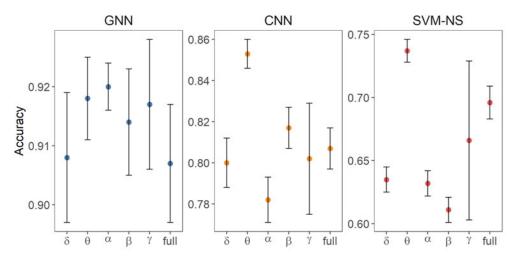


Figure B.3: Effect of frequency band

Table B.1: Performance of the GNN model across five frequency bands and the full frequency range. Values are based on 20-times repeated 20-fold cross-validation. Differences might occur between the main-text results and the supplementary results as the main-text results are based on 50-times repeated 20-fold cross-validation.

Band-	area-under-curve-(AUC)-		Sensitivity-	
delta-	0.98 0.003-	90.59%-±0.77-	93.43%-±1.65-	87.79%-±2.08-
theta-	0.983 0.003-	90.59% - ± 0.77 -	93.43% - ± 1.65 -	87.79%-±2.08-
alpha-	0.984 0.002-	90.59% - ± 0.77 -	93.43% - ± 1.65 -	87.79%-±2.08-
beta-	0.984 0.003-	90.59% - ± 0.77 -	93.43% - ± 1.65 -	87.79%-±2.08-
gamma-	0.984 0.003-	90.59% - ± 0.77 -	93.43% - ± 1.65 -	87.79%-±2.08-
full-	0.983 0.002-	90.59%-±0.77-	93.43%-±1.65-	87.79%-±2.08-

Table B.2: Performance of the CNN model across five frequency bands and the full frequency range. Values are based on 20-times repeated 20-fold cross-validation. Differences might occur between the main-text results and the supplementary results as the main-text results are based on 50-times repeated 20-fold cross-validation.

Band-	AUC-	Accuracy-	Sensitivity-	Specificity-
theta-	0.937 0.004-	85.51%-±0.6-	82.77%-±1.24-	88.22%-±1.45-
beta-	0.904 0.009-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
full-	0.902 0.005-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
delta-	0.898 0.005-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
gamma-	0.873 0.019-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
alpha-	0.867 0.01-	85.51%-±0.6-	82.77%-±1.24-	88.22%-±1.45-

Table B.3: Performance of the SVM-NS model across five frequency bands and the full frequency range. Values are based on 20-times repeated 20-fold cross-validation. Differences might occur between the main-text results and the supplementary results as the main-text results are based on 50-times repeated 20-fold cross-validation.

Band-	AUC-	Accuracy	Sensitivity-	Specificity-
delta-	0.67 0.017-	63.54% - ± 1.05 -	62.91%-±1.19-	64.22%-±1.02-
theta-	0.801 0.013-	63.54% - ± 1.05 -	62.91% - ± 1.19 -	64.22% - ± 1.02 -
alpha-	0.69 0.042-	63.54% - ± 1.05 -	62.91%-±1.19-	64.22% - ± 1.02 -
beta-	0.725 0.068-	63.54% - ± 1.05 -	62.91% - ± 1.19 -	64.22% - ± 1.02 -
gamma-	0.761 0.056-	63.54% - ± 1.05 -	62.91%-±1.19-	64.22% - ± 1.02 -
full-	0.752 0.037-	63.54% - ± 1.05 -	62.91% - ± 1.19 -	64.22% - ± 1.02 -

B.4 Effect of edge filters on model performance

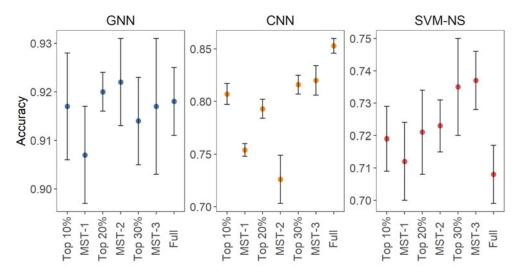


Figure B.4: Effect of edge filters

Table B.4: Performance of the GNN model across the graph filters used. Values are based on 20-times repeated 20-fold cross-validation. Differences might occur between the main-text results and the supplementary results as the main-text results are based on 50-times repeated 20-fold cross-validation.

Edge-Filter-	AUC-	Accuracy-	Sensitivity-	Specificity-
Top-10%-	0.984 0.003-	91.74%-±1.1-	95.13%-±1.31-	88.4%-±2.02-
MST-1-	0.983 0.002-	91.74% - ± 1.1 -	95.13%-±1.31-	88.4%-±2.02-
Top-20%-	0.984 0.002-	91.74% - ± 1.1 -	95.13%-±1.31-	88.4%-±2.02-
MST-2-	0.981 0.004-	91.74%-±1.1-	95.13%-±1.31-	88.4%-±2.02-
Top-30%-	0.984 0.003-	91.74%-±1.1-	95.13%-±1.31-	88.4%-±2.02-
MST-3-	0.981 0.003-	91.74%-±1.1-	95.13%-±1.31-	88.4%-±2.02-
Full-	0.983 0.003-	91.74% - ± 1.1 -	95.13%-±1.31-	88.4%-±2.02-

Table B.5: Performance of the CNN model across the edge filters used. Values are based on 20-times repeated 20-fold cross-validation. Differences might occur between the main-text results and the supplementary results as the main-text results are based on 50-times repeated 20-fold cross-validation.

Edge-Filter-	AUC-	Accuracy-	Sensitivity-	Specificity-
Full-	0.937 0.004-	85.51%-±0.6-	82.77%-±1.24-	88.22%-±1.45-
MST-3-	0.911 - 0.004	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
Top-10%-	0.902 0.005-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
Top-30%-	0.896 0.005-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
MST-2-	0.887 0.004-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
MST-1-	0.88 0.004-	85.51% - ± 0.6 -	82.77%-±1.24-	88.22%-±1.45-
Top-20%-	0.872 0.006-	85.51%-±0.6-	82.77%-±1.24-	88.22%-±1.45-

Table B.6: Performance of the SVM-NS model across the edge filters used. Values are based on 20-times repeated 20-fold cross-validation. Differences might occur between the main-text results and the supplementary results as the main-text results are based on 50-times repeated 20-fold cross-validation.

Edge-Filter-	AUC-	Accuracy-	Sensitivity-	Specificity-
Top-10%-	0.77 0.011-	71.86%-±1.05-	72.21%-±1.06-	71.55%-±1.22-
MST-1-	0.772 0.013-	71.86% - ± 1.05 -	72.21%-±1.06-	71.55%-±1.22-
Top-20%-	0.772 0.03-	71.86%-±1.05-	72.21%-±1.06-	71.55% - ± 1.22 -
MST-2-	0.785 0.014-	71.86%-±1.05-	72.21%-±1.06-	71.55% - ± 1.22 -
Top-30%-	0.779 0.014-	71.86% - ± 1.05 -	72.21%-±1.06-	71.55%-±1.22-
MST-3-	0.801 - 0.013	71.86%-±1.05-	72.21%-±1.06-	71.55%-±1.22-
Full-	0.759 0.008-	71.86% - ± 1.05 -	72.21%-±1.06-	71.55%-±1.22-

Appendix C

Additional results from Adaptive Gated Graph Convolutional Network for Explainable Diagnosis (Chapter 6)

C.1 Hyperparameters of proposed model

The optimised and allowed values of the various hyperparameters of the proposed AGGCN are reported in Tables C.1 and C.2, respectively.

L_{CNN}	kernel-size-	CNN-filters-	h_{CNN}	$drop_{CNN}$	k_{KNN}
1-	4-	84-	403-	0.024-	16-
R	h_{GNN}	activation-	aggregation-	$drop_{GNN}$	
4-	372-	Tanh-	mean-	0.9-	
k_{pool}	$drop_{pool}$	negative-slope-	L_{MLP}	h_{MLP}	$drop_{MLP}$
3-	0.75-	0.085-	3-	16-	0-
learning-rate-	momentum-	weight-decay-	γ	σ	p_{noise}
0.063-	0.859-	0.076-	0.896-	0.346-	0.1-

Table C.1: Hyper-parameter values of the optimised model

Hyperparameter-	Values-
L_{CNN}	$[1,\ldots,4]$ -
kernel-size-	$[2,\ldots,4]$ -
CNN-filters-	$[16, \ldots, 100]$ -
h_{CNN}	$[16, \ldots, 1024]$ -
$drop_{CNN}$	[0, 0.9]-
k_{KNN}	$[1,\ldots,23]$ -
R	$[1,\ldots,10]$ -
h_{GNN}	$[16, \ldots, 1024]$ -
activation-	ReLU, Tanh, ELU, LeakyReLU
aggregation-	add, mean, max
$drop_{GNN}$	[0, 0.9]-
k_{pool}	$[1,\ldots,23]$ -
$drop_{pool}$	[0, 0.9]-
negative-slope-	[0, 0.5]-
L_{MLP}	$[1,\ldots,5]$ -
h_{MLP}	$[16, \ldots, 2048]$ -
$drop_{MLP}$	[0, 0.9]-
learning-rate-	[0.001, 0.1]-
momentum-	[0, 0.9]-
weight-decay-	[0, 0.1]-
γ	[0.8, 0.95]-
σ	[0, 0.5]-
p_{noise}	[0, 0.6]-

Table C.2: Hyper-parameter value ranges allowed during optimisation

C.2 Parameter sensitivity experiments

Multiple- parameter- sensitivity- experiments- were- performed- to- test- the- influence- ofthe-selected-crucial-hyperparameters- of-AGGCN.- The- results- of- these- experimentsare-reported-in-Figures-C.1,-C.2,-C.3- and-C.4-for-the-number-of-GGCN-iterations,-Knearest-neighbour-edges-kept-in-the-sparse-learned-graph-structure,-size-of-the-coarsened-(pooled)-graph-and-aggregation-function,-respectively.-

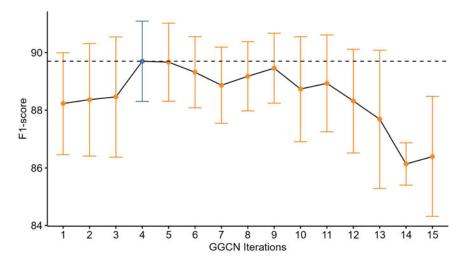


Figure C.1: Sensitivity of the proposed model to the number of iterations of the GGCN encoder. The error bars show the standard deviation of accuracies measured across ten repetitions. The optimal value is shown in blue.

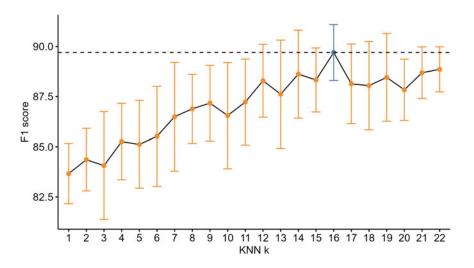


Figure C.2: Sensitivity of the proposed model to the k-nearest-neighbour edges kept in the learned graph structure. The error bars show the standard deviation of accuracies measured across ten repetitions. The optimal value is shown in blue.

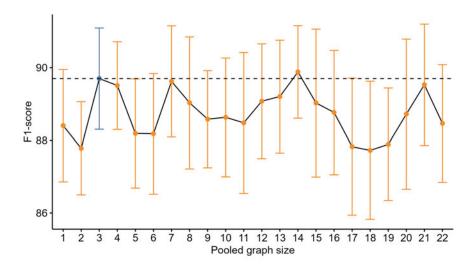


Figure C.3: Sensitivity of the proposed model to the size of the pooled graph. The error bars show the standard deviation of accuracies measured across ten repetitions. The optimal value is shown in blue.

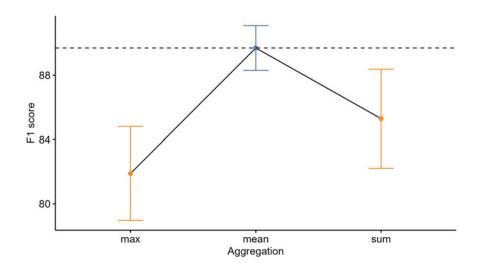


Figure C.4: Sensitivity of the proposed model to the choice of the aggregation function. The error bars show the standard deviation of accuracies measured across ten repetitions. The optimal value is shown in blue.

C.3 Explainability of AGGCN: Adjacency-based visualisations

The main-manuscript shows the AGGCN-learned graphs and the node pooling patterns as a graph. In order to facilitate a different view of the same results, we report the averaged adjacency matrices in Figure C.5 that correspond to Figure 6.3 in the main text. Similarly, we report the differences between the learned graphs together with effect sizes (Wilcox permutation effect size) to quantify the strength of these differences (Figure C.6, corresponding to Figure 6.4 in the main text). Finally, we report an adjacency-like view of the node pooling attention scores (Figure C.7) corresponding to Figure 6.8 in the main text.

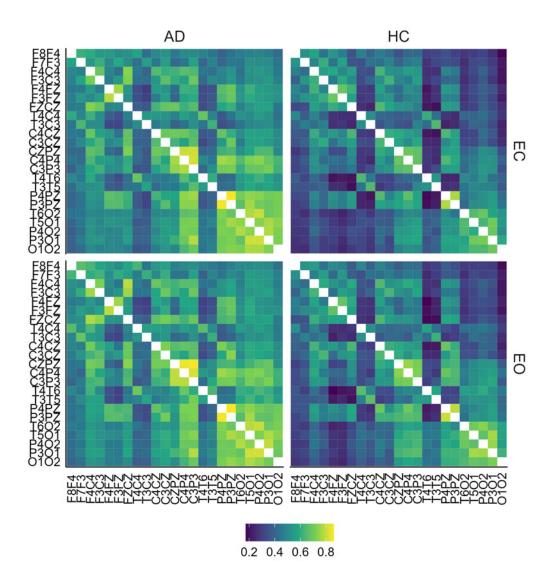


Figure C.5: Average adjacency matrix of learned graphs of AD and HC cases in EC and EO conditions.

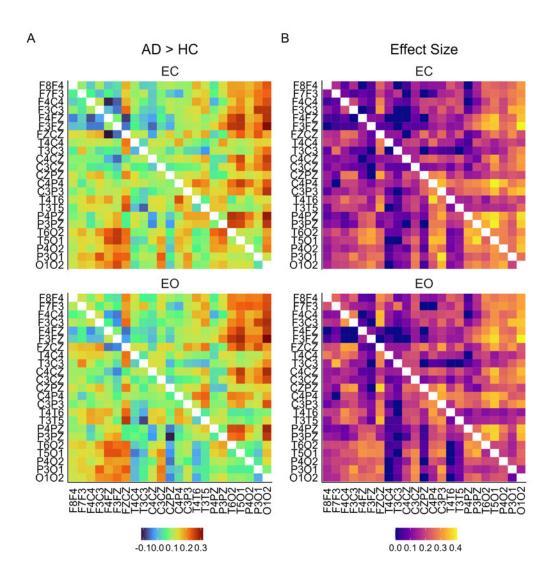


Figure C.6: Difference of averaged adjacency matrices of learned graphs of AD and HC cases (AD – HC) in EC and EO conditions (A). (B)-The effect-size-for-the-non-parametric-Mann-Whitney-U-tests-comparing-AD-and-HC-with-values-set-to-0-where-p-value>> 0.05,-

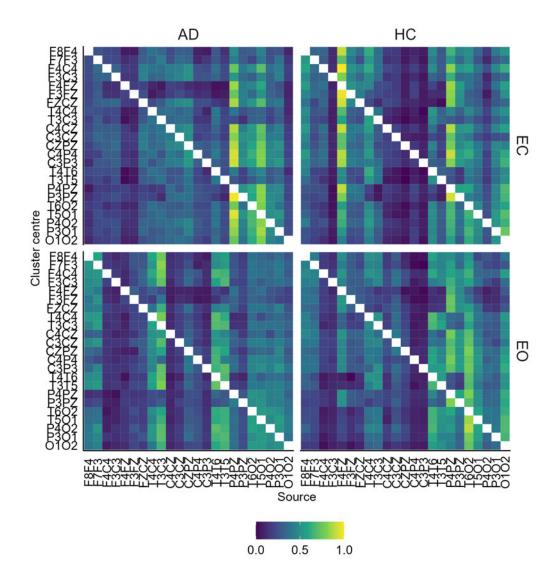


Figure C.7: Average adjacency matrix of attention scores obtained by the node pooling module for AD and HC cases across EC and EO conditions.