Modelling and Motion Analysis of a Pill-Sized Hybrid Capsule Robot

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Abstract

This paper presents a miniature hybrid capsule robot for minimally invasive in-vivo interventions such as capsule endoscopy within the GI (gastrointestinal) tract. It proposes new modes of operation for the hybrid robot namely hybrid mode and anchoring mode. The hybrid mode assists the robot to open an occlusion or to widen a narrowing. The anchoring mode enables the robot to stay in a specific place overcoming external disturbances (e.g. peristalsis) for a better and prolonged observation. The modelling of the legged, hybrid and anchoring modes are presented and analysed. Simulation results show robot propulsions in various modes. The hybrid capsule robot consisting four operating modes is more effective for the locomotion and observation within GI tract when compared to the locomotion consisting a single mean of locomotion as the hybrid robot can switch among the operating modes to suit the situation/task.

Keywords Hybrid capsule robot · Capsule endoscopy · In-vivo diagnosis · Legged mode · Legless mode · Anchoring mode · Modelling · Medical robot

1 Introduction

Miniature robots/robotic assistants show promise for a better and minimally invasive diagnosis and interventions.

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Researches in miniature mobile robots for abdominal cavity interventions and self-propelling capsule endoscope (CE) to diagnose GI (gastrointestinal) tract diseases are rising [1–7]. Currently, available CE is passive and moves by utilising natural GI peristalsis and gravity. It cannot control its movement and orientation, cannot reverse the direction and cannot stop at a certain place for a long and detailed observation. Furthermore, it cannot distend the tissue when it is necessary especially in the colon to have a better view of the interior surface [8]. Thus, the diagnostic outcome of the CE is not fully reliable and it plays a complementary role with traditional probe endoscopy (PE) rather than replacing it. Researches are ongoing to add mobility to CE to increase the reliability, performance and to add functionalities such as biopsy, drug delivery, surgery etc. Mobile robots designed for the abdominal cavity, as well as GI tract, can be divided based on the propulsion mechanism used as 1) external propulsion robot (i. magnetic propulsion [2, 4, 9]) 2) internal propulsion robot (i. wheeled [10, 11] ii. legged [1, 8] iii. internal reaction force propulsion robot [12, 13] iv) vibratory actuation robot [14, 15]) and 3) hybrid propulsion robot [16].

Magnetic propulsion is performed using magnet/ferromagnetic material inside the capsule which is controlled by external magnets or solenoid. The effective control is not possible for this type of propulsion and also it cannot distend the tissue for better view [16]. Moreover the use of large

external magnet makes the system expensive. The sharp edges of legs or wheels of the legged/wheeled robots create the risk to injure the tender GI tract and internal organs. Moreover, a substantial amount of energy is required which is either supplied by batteries or tethered external sources [8, 10, 11]. The internal reaction force propulsion robot utilises the reaction force of an inner mass moving back and forth. It has no external legs or wheels which is a very good feature for in-vivo robots. However, it cannot distend the tissue for better observation [12]. A hybrid locomotion was developed in [16] where internal legged actuation mechanism and external magnetic dragging is combined. Here the legged mechanism is limited. It can lift the tissue in a collapsed region and can move the robot slightly forward. This propulsion mechanism still has the disadvantage of being expensive because of the large external magnet.

This paper is a further development of a hybrid capsule robot based on the idea in [17] which combines both internal reaction propulsion mechanism (capsule/legless propulsion) and legged propulsion mechanism. This paper proposes two new modes of operation namely hybrid mode and anchoring mode. The robot with four modes of operation is more suited for locomotion within a GI tract of the human body when compared to robots having only a single mean for propulsion. The most appropriate mode of operation of the hybrid robot can be selected to minimise/remove the chance of causing harm to the vessels through which the robot passes.

The contributions of this paper are: a) extending the operating modes of hybrid robot of [17] and adding two modes namely hybrid mode and anchoring mode where the existing actuators are utilised for executing the proposed modes b) developing the methods of moving the robot within a tubular environment in legged mode, hybrid mode and anchoring mode c) modelling of the robot in legged mode, hybrid mode and anchoring mode and d) simulation of the robot in legged mode and hybrid mode.

This paper is structured as follows. Section 2 presents the hybrid robot design. The working principles of the robot in various modes are described in Section 3. Section 4 presents the robot modeling in various modes whereas Section 5 presents the robot simulation in various modes. Section 6 presents the rationale of using four operating modes. Finally Section 7 presents the conclusion and future works.

2 Hybrid Robot Design

This paper presents further development based on the idea in [17]. Figure 1a and b show the hybrid capsule robot design and a partially exploded perspective view of the hybrid capsule robot respectively. The hybrid robot has two sets of projecting legs which can be engaged/disengaged with the cylindrical rod of the linear motors by two grippers.

(a)

(b)

(c)
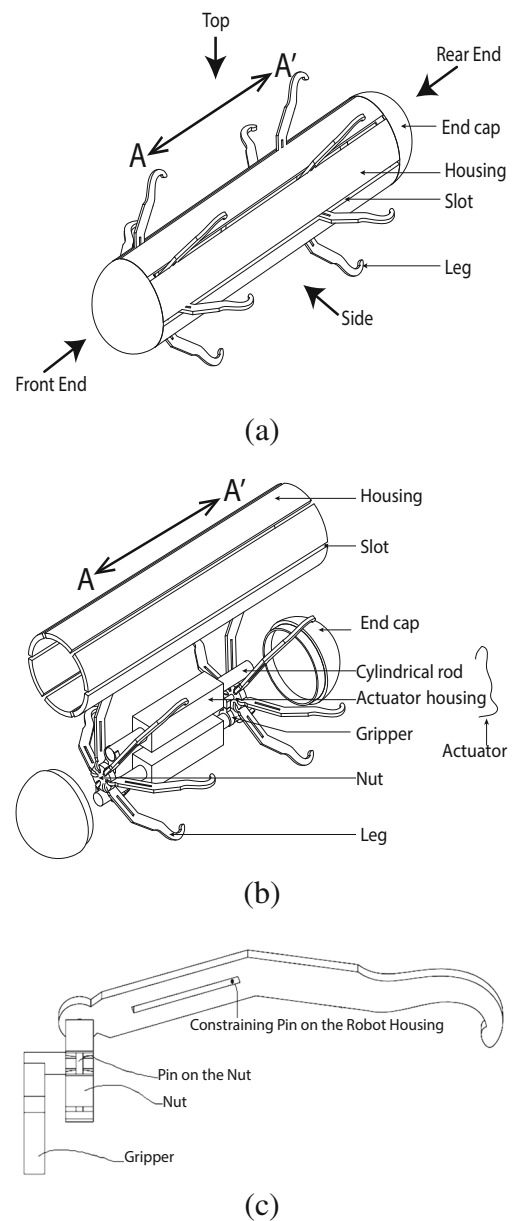
Fig. 1 Hybrid robot design (modified from [17]) **a** A perspective view of the hybrid robot **b** A partially exploded perspective view of the hybrid robot of Fig. 1a where the leg-sets are coupled with the cylinder rods **c** Leg-nut-gripper assembly showing one leg

The legs can be operated (open and close) by controlling the cylindrical rod movement. Figure 1c presents leg-nut-gripper assembly showing one leg.

3 Working Principle

The hybrid capsule robot has four modes of operation: legless motion mode, legged motion mode, hybrid motion mode and anchoring mode. Same actuators are used to perform the operations in all the modes.

3.1 Legless Mode

This is the primary propulsion mode. In this mode, the cylindrical rods act as inertial masses (IMs) to generate propulsion. The leg-sets are disengaged from the cylindrical rods and retracted inside the robot body. Thus the movement of the cylindrical rod does not cause any movement of the leg-sets. By controlling the acceleration of the cylindrical rods, the robot can i) move forward or backward and ii) rotate clockwise or counterclockwise. In the legless mode, the hybrid robot motion can be compared with the motion of the 2D capsubot described in the paper [18] of the first author. The working principle in legless mode is the same as described in [18]. The mass of the leg-nut-gripper assembly is added to the mass of the robot. The features of legless mode are: i) primary motion mode, ii) moved by the internal reaction force, iii) legs are folded inside the robot body, iv) no external moving parts, v) hermetically sealable, vi) any suitable outer structure is possible, and vii) suitable for applications inside the human body. In the legless mode, the robot is an underactuated system and nonlinear [19, 20] and, a behaviour based control has been presented in [18] to control this nonlinear underactuated system.

3.2 Legged Mode

This is the secondary propulsion mode. This mode is only activated when the robot can not pass a path using legless mode. In the legged mode (Fig. 2a), the leg-sets are connected with cylindrical rods through the gripper-nut assemblies. When the cylindrical rod moves linearly, the corresponding gripper-nut assembly moves linearly with it. However, the legs rotate and slide with respect to the constraining pins which are fixed on the robot cover. The leg-movements (opening and closing) are repeated to enable the robot to move. The legs can be operated (open and close) using the following control sequences so that the robot only moves in the forward direction.

- Cycle 1: At the beginning of the legged locomotion, both the leg-sets remain closed.

    - Step 1: The rear leg-set opens from closed position. During this step, the robot experiences a small backward force from the reaction of the surrounding environment and it moves backward though very small.
    - Step 2: The front leg-set opens from closed position. The robot experiences a small backward force. But as the hook of the rear leg-set locks the robot and opposes any backward movement, the robot remains stand-still.
    - Step 3: The front leg-set closes from opened position. The robot experiences a forward force from the reaction of the surrounding

(a)

(b)

(c)
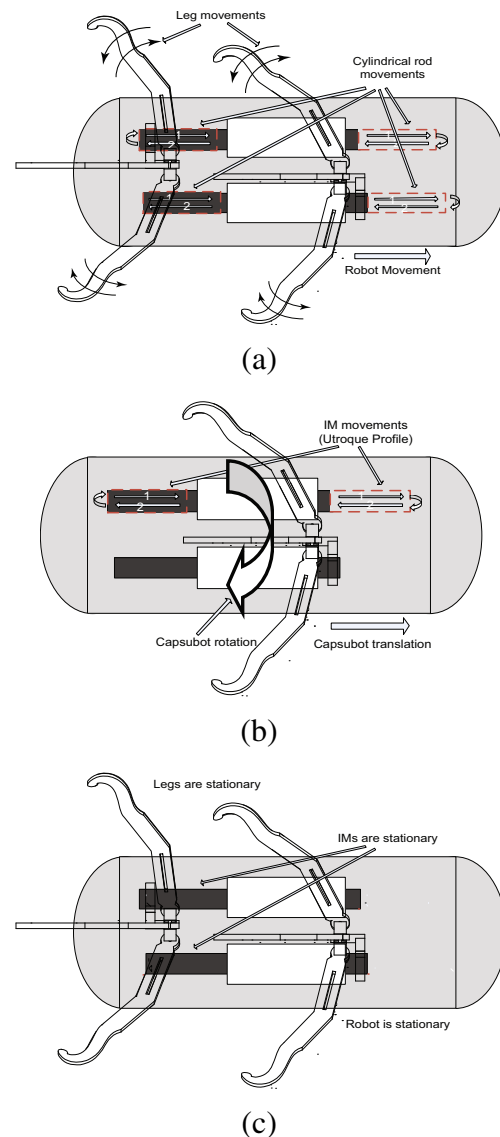
Fig. 2 Legs and cylindrical rods in various modes **a** Legs and cylindrical rods' movements in legged mode **b** Legs and cylindrical rods' movements in hybrid mode (translation-clockwise) **c** Stationary legs and cylindrical rods in anchoring mode

environment and it moves forward. Because of the hook-like structure, the opened rear leg-set creates very low resistance in the forward movement of the robot.

- Repeated cycle: By repeating steps 2 and 3 the robot moves forward.

The features of legged mode are: i) this is a secondary motion mode, ii) the legs come out from the robot body, and iii) the robot can pass occlusions or narrowing using this mode.

3.3 Hybrid Mode

In this mode, one of the leg-sets is kept always open and other leg-set is disengaged from the cylindrical rod

and retracted inside the robot body. The free cylindrical rod is operated in legless mode. In hybrid motion mode, one of the actuators keeps one leg-set open to make a path for the robot and the other actuator works in legless motion mode to provide force to move the robot forward. It provides 'hammer blow - a very hard hit' to the robot and assist it to open an occlusion or to widen a narrowing. Thus, the features of the hybrid mode are: i) secondary motion mode ii) one linear actuator is arranged to keep one leg-set open iii) the other linear actuator of the robot operates in legless propulsion mode iv) legless propulsion is employed to hammer the consequently wedge-shaped robot (because of the opened leg-set) into the occlusion.

The hybrid motion can be divided into two types: 1) Hybrid translation-anti-clockwise rotation, and 2) Hybrid translation-clockwise rotation.

3.3.1 Hybrid translation-anti-clockwise rotation

The first leg-set is kept open and second cylindrical rod (inertial mass/inner mass - IM_2) follows the acceleration profile presented in [18]. The reaction force urges the robot to move forward. Moreover, as the reaction force does not go through the mass centre of the robot, it creates a torque with respect to the mass centre of the robot. The torque urges the robot to rotate counter-clockwise.

3.3.2 Hybrid translation-clockwise rotation

The second leg-set is kept open (Fig. 2b) and first cylindrical rod (inertial mass/inner mass - IM_1) follows the acceleration profile presented in [18]. The reaction force urges the robot to move forward. Moreover, as the reaction force does not go through the mass centre of the robot, it creates a torque which urges the robot to rotate clockwise.

3.4 Anchoring mode

In anchoring mode (Fig. 2c), the robot stays in a fixed position to do a certain task (e.g. delivering treatments, taking video for a long time for better observation). The actuators are used to keep both the leg-sets open. The actuators oppose any movement tendency of the leg-sets by any external force such as visceral peristalsis. The features of the anchoring mode are i) the robot does not move and ii) both the leg-sets are kept open to anchor the robot in a fixed position to perform a task (e.g. take video, deliver treatment).

4 Modelling of the Hybrid Robot

4.1 Modelling of the Legless Mode

The legless mode of the hybrid robot can be compared with the 2D capsubot presented in the paper [18] of the first author. The reader is referred to [18] for the modelling of the legless mode.

4.2 Modelling of the Legged Mode

By controlling the movements of the cylindrical rods the leg-sets can be opened and closed. The leg has a good contact with the surrounding environment (colon wall of GI tract) while the leg-opening is between $140° - 110°$ [21]. Thus, the working angle is kept between $140°$ - $110°$ in this paper. The closing is defined as moving the leg-set from leg-opening $140°$ to $110°$ as shown in Fig. 3a and b. The opening is defined as moving the leg-set from leg-opening $110°$ to $140°$ as shown in Fig. 3a. In one cycle the leg performs closing and opening i.e. moves from $140°$ to $110°$ and then returns to $140°$ from $110°$. To help the reader to follow the modelling of the legged mode a notation list is provided in Table 1.

4.2.1 When the leg-set is closing from 140° to 110° and leg-tips have no contact

Figure 3a shows the scenario where the leg-set is closing from $140°$ to $110°$ and leg-tips have no contact with the surrounding. Here the cylindrical rod moves towards left from A' to A" position, θ changes from $140°$ to $110°$, the leg moves from red dotted to blue solid position and the leg-tip moves from C' to C" position. The position of leg-tip for Fig. 3a:

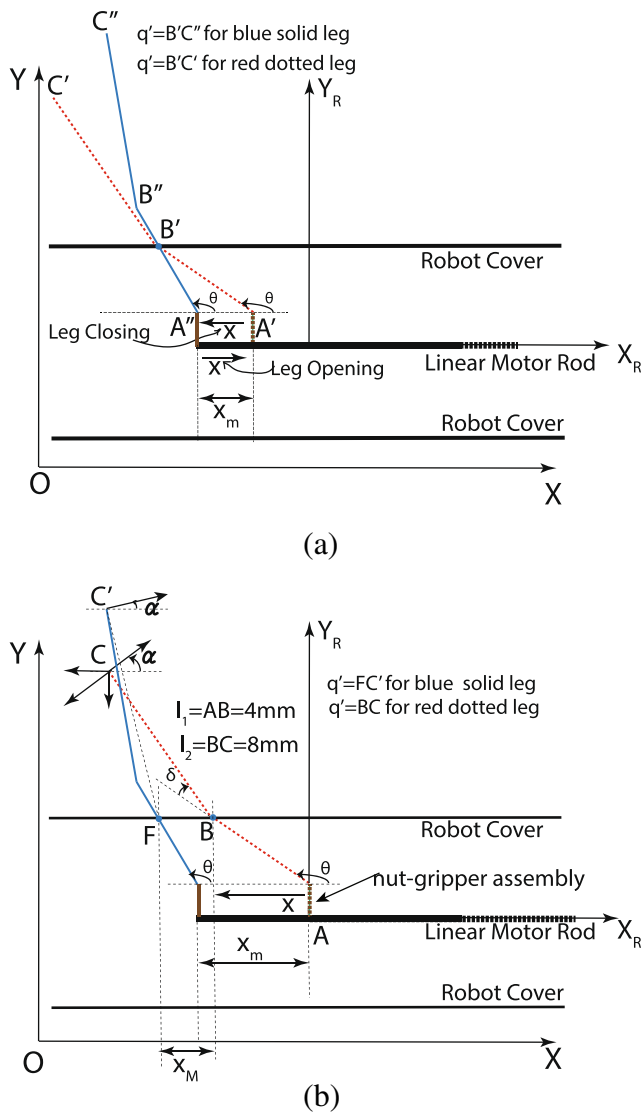$$x_{leg-tip} = l_1 \cos(\theta) + l_2 \cos(\theta + \delta) + x_m, \tag{1}$$

$$y_{leg-tip} = l_1 \sin(\theta) + l_2 \sin(\theta + \delta) + y_m, \tag{2}$$

where $\delta = constant = -15°$, $l_1 = 4mm$ and $l_2 = 8mm$.

$$\theta(x_m) = \tan^{-1} \frac{l_1 \sin(\theta_M)}{l_1 \cos(\theta_M) - x_m}, \tag{3}$$

$$x_M = 0. \tag{4}$$

- From Eqs. 1 and 3 if $\theta = \theta_M$ then $x_m = 0$ and $x_{leg-tip} = -7.6528mm$.
- Similarly from Eqs. 1 and 3 if $\theta = \theta_m$ then $x_m = -2.1284mm$ and $x_{leg-tip} = -4.1937mm$.

Fig. 3 **a** Leg closing and opening when the leg is not facing any obstacle - the robot does not move **b** Leg closing: the leg (red dotted and blue solid) in two positions (140° and 110°) when the robot moves

4.2.2 When the Leg-Set Closes and the Leg-Tips have Contact with the Surrounding

This section presents the modelling of the legged mode when the leg-set closes from 140 degrees to 110 degrees and the leg-tips have contact with the cylindrical surrounding such as colon wall. Figure 4a shows the force balance. The linear motor housing applies F_{act} force on the cylindrical rod and tries to move it towards left. f_m is the friction which opposes this movement tendency. Through lever action (pin on the slot of the robot cover of each leg works as a fulcrum and forms a lever) each leg-tip applies F_{leg} force on the colon wall. The reaction by the colon wall on the leg-tip is $R_{colon} = -F_{leg}$. The rod applies " $-F_{act}$ " reaction force on the linear motor housing which is attached to the outer

Table 1 Description of the notations used

Notation	Description
F_{act}	Force on the cylindrical rod by the Motor housing
F_{leg}	Force on the colon wall of the GI tract by the leg-tip
n	Number of legs in each leg-set
l_1	Length of the first link of the leg
l_2	Length of the second link of the leg
θ	Angle between the first link and the robot body
θ_M	Maximum leg-opening, 140°
θ_m	Minimum leg-opening, 110°
δ	Angle between the first and second links (constant)
p'	Straight line distance between the constraining pins (on the cover and on the nut)
q'	Straight-line distance between the constraining pin on the cover and leg-tip (contact point with the surrounding)
$x_{leg-tip}$	Horizontal position of the leg-tip
$y_{leg-tip}$	Vertical position of the leg-tip
(x_F, y_F)	Position of the pin on the robot cover, F
(x_m, y_m)	Position of the cylindrical rod (inertial mass)
(x_M, y_M)	Position of the robot

cover of the robot. The rod and the robot are still stationary. The force on the colon wall by the leg-tip is given by:

$$F_{leg} = -\frac{1}{n}(F_{act} - f_m)\sin(\theta)\frac{p'}{q'}, \tag{5}$$

where,

$$f_m = \sin(\dot{x}_m)\mu_m mg,$$
$$p' = \frac{p}{\sin(\theta)},$$
$$q' = \sqrt{(y_{leg-tip} - y_F)^2 + (x_{leg-tip} - x_F)^2}.$$

When all the components of the robot and the robot are stationary, there is a force balance. The vertical component of the reaction force of the surrounding environment such as colon wall on each leg is given by the following equation.

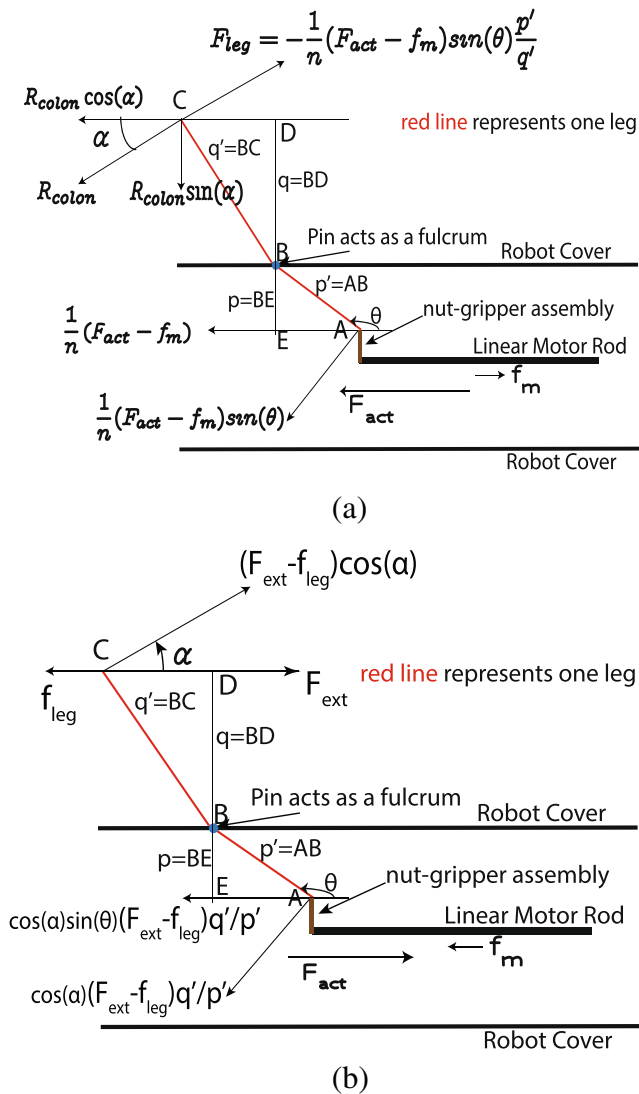$$F_V = R_{colon}\sin(\alpha).$$

There are three pairs of legs in each leg-set. As each pair cancels each others vertical component of reaction forces, the vertical components do not have any impact on the robot movement. Horizontal forces contributes to the robot movement. Following two forces are acting on the leg horizontally (towards left in Fig. 4a). Horizontal force on the leg by the rod (F_{H1}) and by the surrounding such as colon wall (F_{H2}) are given by the following equations respectively.

$$F_{H1} = \frac{1}{n}(F_{act} - f_m),$$
$$F_{H2} = R_{colon}cos(\alpha).$$

As the leg is stationary, the pin on the robot cover (fulcrum of the lever) must apply a horizontal force (F_H)

$$F_{leg} = -\frac{1}{n}(F_{act} - f_m)sin(\theta)\frac{p'}{q'}$$

$R_{colon}\cos(\alpha)$ C

α D $q'=BC$

R_{colon} $R_{colon}\sin(\alpha)$ $q=BD$

red line represents one leg

Pin acts as a fulcrum Robot Cover

$p'=AB$

$p=BE$ nut-gripper assembly

$\frac{1}{n}(F_{act} - f_m)$ E A θ Linear Motor Rod

$\longrightarrow f_m$

$\frac{1}{n}(F_{act} - f_m)sin(\theta)$ F_{act}

Robot Cover

(a)

$(F_{ext} - f_{leg})\cos(\alpha)$

C α D F_{ext} red line represents one leg

f_{leg} $q'=BC$

$q=BD$

Pin acts as a fulcrum Robot Cover

$p=BE$ $p'=AB$

E nut-gripper assembly

$\cos(\alpha)\sin(\theta)(F_{ext} - f_{leg})q'/p'$ A θ Linear Motor Rod

$\longleftarrow f_m$

$\cos(\alpha)(F_{ext} - f_{leg})q'/p'$ F_{act}

Robot Cover

(b)

Fig. 4 Acting forces for one leg **a** Acting forces in the legged mode when the robot is stationary **b** Acting forces for one leg when F_{ext} exceeds the limiting value of f_{leg} (applicable to both hybrid and anchoring mode)

(towards right in Fig. 4a) force on each leg given by the following equation.

$$F_H = \frac{1}{n}(F_{act} - f_m) + R_{colon}cos(\alpha).$$

Each leg applies F_H reaction force (towards left in Fig. 4a) on the pin on the robot cover (fulcrum). As the pin on each slot of the leg are fixed to the robot cover, the force applied on the robot/robot cover by all the legs is nF_H. This force tries to move the robot. The cylindrical rod also applies nF_{H1} force (towards right in Fig. 4a) on the robot. The total horizontal force ($F_{H_{robot}}$) acting on the

robot (towards left in Fig. 4a) is given by the following equation.

$$\begin{aligned} F_{H_{robot}} &= nF_H - nF_{H1}, \\ \implies F_{H_{robot}} &= (F_{act} - f_m) + nR_{colon}\cos(\alpha) \\ &\quad -(F_{act} - f_m), \\ \implies F_{H_{robot}} &= nR_{colon}\cos(\alpha), \\ \implies F_{H_{robot}} &= -nF_{leg}, \\ \implies F_{H_{robot}} &= (F_{act} - f_m)\sin(\theta)\cos(\alpha)\frac{p'}{q'}. \quad (6) \end{aligned}$$

The dynamic equation of the robot can be written as:

$$F_{H_{robot}} = f_M + M\ddot{x}_M, \quad (7)$$

$$M\ddot{x}_M = (F_{act} - f_m - m\ddot{x}_m)\cos(\alpha)\frac{p}{q'} - f_M. \quad (8)$$

where

$$f_M = sgn(\dot{x}_M)\mu_M F_{NM}, \quad F_{NM} = Mg.$$

$F_{H_{robot}}$ contributes to the robot movement. The robot moves when F_{act} is large enough so that $F_{H_{robot}}$ exceeds the friction ($|f_M|$) of the robot. To maintain this force, the leg-tips need to have contact with the colon-wall all the time. To fulfil this constraint: both the robot and the rod moves left which causes the leg-tip to stay in the same horizontal position but leg-tip vertical position changes. In one closing cycle, the rod moves left so that the angle θ changes from 140° to 110° and to keep the leg-tip in the same horizontal position the distance travelled by the robot in one cycle is (from Fig. 3b):

$$\begin{aligned} x_M = & (l_1\cos(\theta) + l_2\cos(\theta + \delta) + x_m) \; for \; \theta_M \\ & -(l_1\cos(\theta) + l_2\cos(\theta + \delta) + x_m) \; for \; \theta_m. \quad (9) \end{aligned}$$

When both the rod and robot move, $\theta(x_m, x_M)$ is given by:

$$\theta(x_m, x_M) = \tan^{-1}\frac{l_1\sin(\theta_M)}{l_1\cos(\theta_M) - x_m + x_M}, \quad (10)$$

and the leg-tip position is given by:

$$x_{leg-tip} = l_1\cos(\theta) + l_2\cos(\theta + \delta) + x_m, \quad (11)$$

$$y_{leg-tip} = l_1\sin(\theta) + l_2\sin(\theta + \delta) + y_m. \quad (12)$$

- From Eqs. 10 and 11 if $x_{leg-tip} = -7.6528mm$ and $\theta = 140°$ then $x_m = 0$ and $x_M = 0$.
- From Eqs. 10 and 11 if $x_{leg-tip} = -7.6528mm$ and $\theta = 110°$ then $x_m = -5.5875$ and $x_M = -3.4591$.

In one closing cycle, the rod moves from $x_m = 0$ position to $x_m = -5.5875mm$ position; the angle changes from $\theta = 140°$ to $\theta = 110°$; the robot moves from $x_M = 0$ to $x_M = -3.4591mm$. However, the horizontal position of the leg-tip remains unchanged i.e. $x_{leg-tip} = -7.6528mm$.

4.2.3 When the Leg-Set Opens from 110° to 140°

At the end of the closing cycle, the robot is stationary, front leg-set is partially open (110°) and rear leg-set is fully open (140°). The rear leg-set maintains its open position. The rod associated with the front leg-set tries to move to open the leg from 110° to 140° . Here the forces are same as forces during leg closing (Fig. 4a) but opposite in direction. Unlike leg closing, here the leg faces little resistance while trying to move and, thus the reaction force is also small. The force $nR_{colon}\cos(\alpha)$ is not enough to move the robot and the robot remains stationary when the leg opens from 110° to 140° (Fig. 3a).

4.2.4 Repeated Cycle

To keep the robot moving the rear leg-set is kept open and, the front leg-set opens and closes repetitively. The robot moves in the 'closing cycle' and remains stationary in the 'opening cycle'.

4.3 Modelling of the Hybrid Mode

In this mode, the robot performs a hybrid translation-rotation because of the reaction force from the IM (cylindrical rod) that moves using the acceleration profile presented in the paper [18] of the first author. As the robot moves, the legs experience an external force. The actuator that is used to keep the leg-set open, has to apply a force to balance the external force so that the leg-set remains open. Let us consider the external force on each leg is F_{ext} and limiting friction of each leg is f_{leg}. Figure 4b shows the acting forces for one leg in hybrid mode. From Fig. 4b, the required force of the actuator is given by:

$$F_{act} = -n\cos\alpha\sin\theta(F_{ext} - f_{leg})\frac{q'}{p'} + f_m. \tag{13}$$

The dynamic model of the robot and the IM (cylindrical rod) which works in legless mode is as follows [18]:

$$F_{m_i} - f_{m_i} = m_i\ddot{x}_{mi} \quad i = 1, \ 2, \tag{14}$$
$$M\ddot{x} = (-F_{m_i} + f_{m_i} - f_M)\cos(\phi) \quad i = 1, \ 2, \tag{15}$$
$$M\ddot{y} = (-F_{m_i} + f_{m_i} - f_M)\sin(\phi) \quad i = 1, \ 2, \tag{16}$$
$$I\ddot{\phi} = (-1)^i[(-F_{m_i} + f_{m_i})d_i - M_f] \quad i = 1, \ 2, \tag{17}$$

where x, y and ϕ are generalised coordinates of the robot with respect to a fixed frame; m_i and M are the IM_i (cylindrical rod) mass and the robot mass respectively; d_i is the perpendicular distance of the direction of forces F_{m_i} and f_{m_i} and, the axis of rotation; f_M is the friction force on the

robot; M_f is the frictional moment of the robot about z-axis through the mass centre of the capsule robot.

The models for both the hybrid motions (1) Hybrid translation-anti-clockwise rotation and 2) Hybrid translation-clockwise rotation) are given below:

4.3.1 Hybrid Translation-Anti-Clockwise Rotation

Here the robot moves forward and rotates anti-clockwise. The first cylindrical rod is used to keep open the first leg-set. The cylindrical rod will oppose any radial movement of the leg-sets. However, the robot as a whole can move forward. The extended leg will increase the friction. Here IM_2 (second cylindrical rod) is disengaged from the leg-set to perform the legless motion. IM_2 (second cylindrical rod) follows the utroque acceleration profile presented in [18]. Equations 14–17 become:

$$F_{m_2} - f_{m_2} = m_2\ddot{x}_2, \tag{18}$$
$$M\ddot{x} = -F_{m_2} + f_{m_2} - f_M, \tag{19}$$
$$I\ddot{\phi} = (-F_{m_2} + f_{m_2})d_2 - M_f. \tag{20}$$

4.3.2 Hybrid translation-Clockwise Rotation

Here the robot moves forward and rotates clockwise. The second cylindrical rod is used to keep open the second leg-set. Here IM_1 (first cylindrical rod) is dis-engaged from the leg-set to perform legless motion. IM_1 (first cylindrical rod) follows the utroque acceleration profile presented in [18]. Equations 14–17 become:

$$F_{m_1} - f_{m_1} = m_1\ddot{x}_1, \tag{21}$$
$$M\ddot{x} = -F_{m_1} + f_{m_1} - f_M, \tag{22}$$
$$I\ddot{\phi} = -(-F_{m_1} + f_{m_1})d_1 + M_f. \tag{23}$$

4.4 Modelling of the Anchoring Mode

In this mode, each of the leg-set is engaged with the corresponding cylindrical rod by the gripper and the leg-set is kept wide open all the time. If any external force (e.g. peristalsis) tries to move the robot, the friction of the legs will stop the robot from moving. The external force is assumed to be acting uniformly on all the legs. If F_{ext} is working on each leg and f_{leg} is the limiting friction of each leg then:

$$F_{ext} \leq f_{leg}. \tag{24}$$

If the external force exceeds the limiting friction force of the leg i.e. when $F_{ext} > f_{leg}$, the actuators need to provide force to stop the robot from moving. Figure 4b shows the

Table 2 Parameters for hybrid robot

n	g	δ	l_1	l_2	m
6	9.8	$-15°$	$4mm$	$8mm$	$25gm$
M	μ_m	μ_M	θ_m	θ_M	
$100gm$	0.2	0.3	$110°$	$140°$	

acting forces for one leg in anchoring mode. From Fig. 4b, the required actuator force:

$$F_{act} = -n \cos \alpha \sin \theta (F_{ext} - f_{leg}) \frac{q'}{p'} + f_m. \quad (25)$$

5 Simulation Results and Discussion

The simulation is performed in the Matlab/Simulink environment where a Ode45 (Dormand-Prince) solver is used with a variable step. The equations developed in the modelling section (Section 4) are applied in the simulation. The values for various parameters used in the simulation are listed in Table 2.

5.1 Legless Mode

The simulation for legless motion is similar to the simulation results presented in the paper [18] of the first author.

5.2 Legged Mode

Figure 5 shows the simulation results for the legged motion for one closing cycle. The dynamic Eqs. 7 and 8 presented in the Section 4.2 are applied to perform simulation. Figure 5a shows the force on the IM (cylindrical rod) required to generate robot movement in legged mode while the legs are closing. It shows that the force required to generate the motion is high which ranges from -12.5N to -21N. Various parameters of the robot design can be modified to improve the force requirement. One scope of improvement is the ratio q'/p. From Eq. 8, it can be concluded that by reducing this ratio, the required force can be reduced.

Figure 5b shows the angle of the leg with the robot body while the robot and the IM (cylindrical rod) are moving. The angle decreases from 140° to 110°. From Fig. 5a and b it can be concluded that as the leg closes the required force increases and reaches to maximum when the leg-closing, θ is 110°. From the Figs. 3 and 4, it can be seen that as the leg-closing (θ) decreases α and q'/p increase. From Eq. 8, it can be concluded when α and q'/p increase the required force will increase as well.

Figure 5c and d show the IM (cylindrical rod) and the robot translation respectively. In one closing cycle, the IM
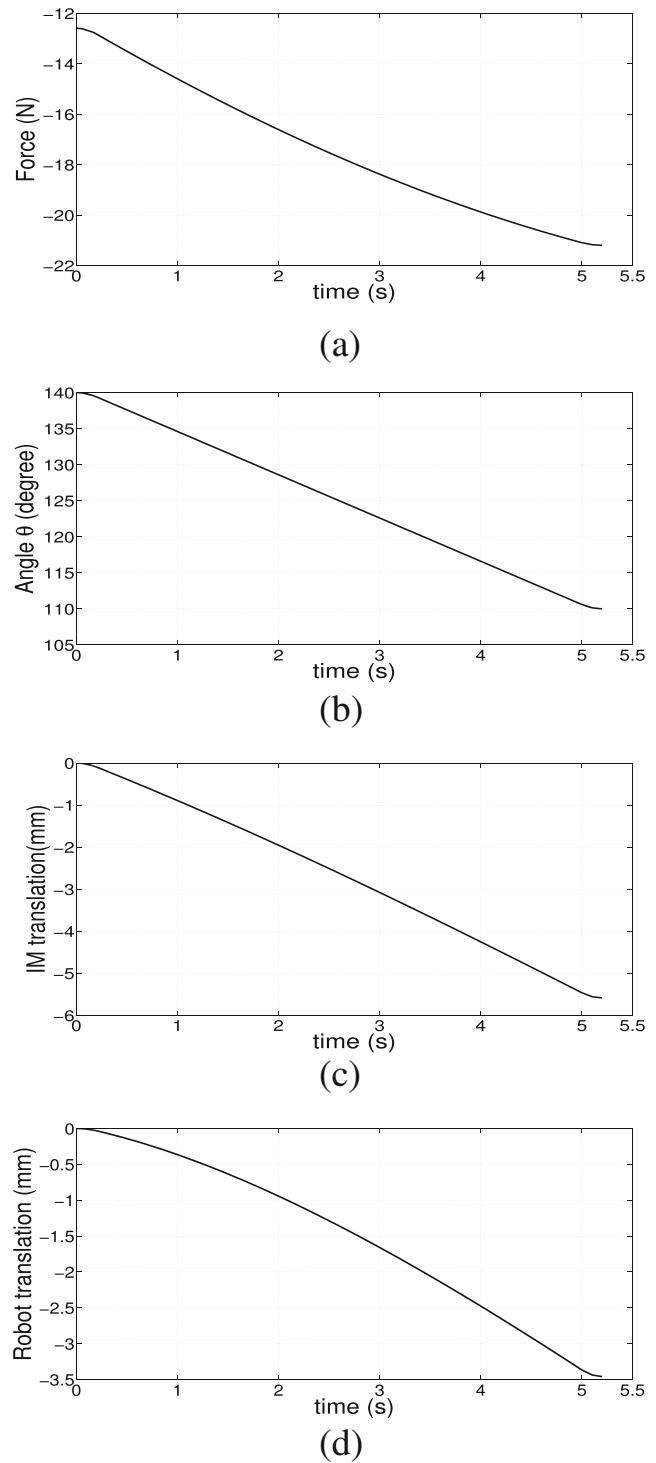
Fig. 5 Simulation results for legged movement in one closing cycle **a** Force applied on the IM (cylindrical rod) **b** Angle in the legged mode **c** IM (cylindrical rod) translation in the legged mode **d** Robot translation in the legged mode

(cylindrical rod) travels $-5.5mm$ whereas the robot travels $-3.4mm$. It can be seen from the Fig. 5c and d that the IM (cylindrical rod) moves faster than the robot so that there

is always contact between the leg-tip and the surrounding environment.

5.3 Hybrid Mode

The dynamic equations presented in the Section 4.3 are applied to perform simulation in this section.

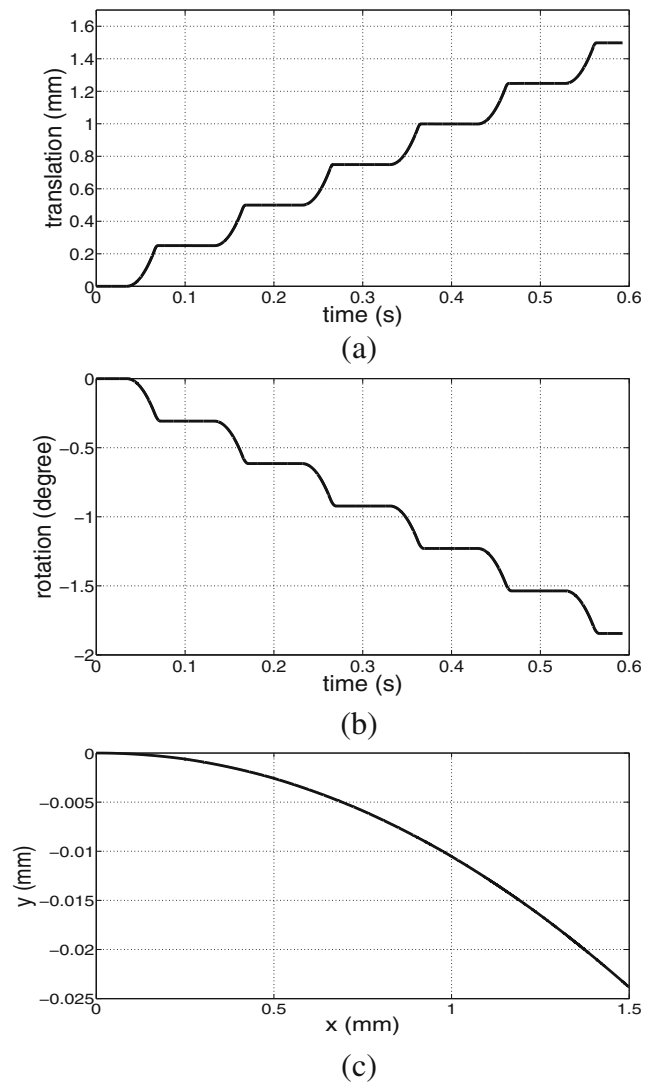#### 5.3.1 Hybrid Translation-Clockwise Rotation

The simulation results for hybrid translation-clockwise rotation are shown in Fig. 6. Figure 6a and b show the translation and the rotation of the hybrid robot respectively. The figures show the step-wise movement of the robot i.e. the robot moves for part of each cycle and remains stationary for the rest of the cycle. It is because of the four-step acceleration profile [18] which the IM (cylindrical rod) follows. Figure 6c shows the hybrid translation-clockwise rotation in the x-y plane. It is also seen that the rotation performed by the robot is small and it is less than $-2°$ in one cycle. It can be concluded from Eq. 23 that robot clockwise rotation will increase if d_2 is increased. In Fig. 6c, the translation along the y-axis is negligible compared to the translation along the x-axis.

5.3.2 Hybrid Translation-Anti-Clockwise Rotation

The simulation results for hybrid translation-anti-clockwise rotation are shown in Fig. 7. The figures are similar to that of Fig. 6 except that the robot rotates anti-clockwise. It can be concluded from Eq. 20 that robot clockwise rotation will increase if d_1 is increased. Similar to Fig. 6c, in Fig. 7c the translation along the y-axis is negligible compared to the translation along the x-axis.

6 Rationale of Four Modes

The hybrid capsule robot has three motion modes (legless, legged and hybrid) and one anchoring mode. Same actuators are used for all the operating modes. The legless motion mode is the primary motion mode whereas the remaining modes are secondary. The leg-sets are disengaged from the cylindrical rods and retracted inside the robot body in the legless mode and the robot has minimal chance of causing harm to internal soft tissue. The legged mode is only activated when the robot can not pass a difficult path using legless mode. The robot returns to the legless mode once the robot passes that difficult path. The anchoring mode is activated when the robot requires to stay in a fixed position to perform a task such as delivering treatments, recording video for a long time for a detailed observation. The actuators are used to keep both the leg-sets wide open to

Fig. 6 Simulation results for hybrid translation-clockwise rotation **a** Forward translation **b** Clockwise rotation **c** Hybrid translation-clockwise rotation

anchor the robot and resists the robot movement due to any external force such as peristalsis. The hybrid mode mode is activated when the robot needs to open an occlusion or to widen a narrowing. One actuator keeps one leg-set open to make a path for the robot and the other actuator works in the legless motion mode to provide force to move the robot forward to open an occlusion or to widen a narrowing. The robot can move minimally invasively in legless mode, can pass a difficult path in legged mode, can open an occlusion in hybrid mode and can stay in a fixed location overcoming external forces in anchoring mode. All these features are not available together in a robot which has only one mode. The hybrid robot is more effective for the locomotion and observation within GI tract when compared to robot with a single mode as the hybrid robot can switch among the modes to suit the situation/task.
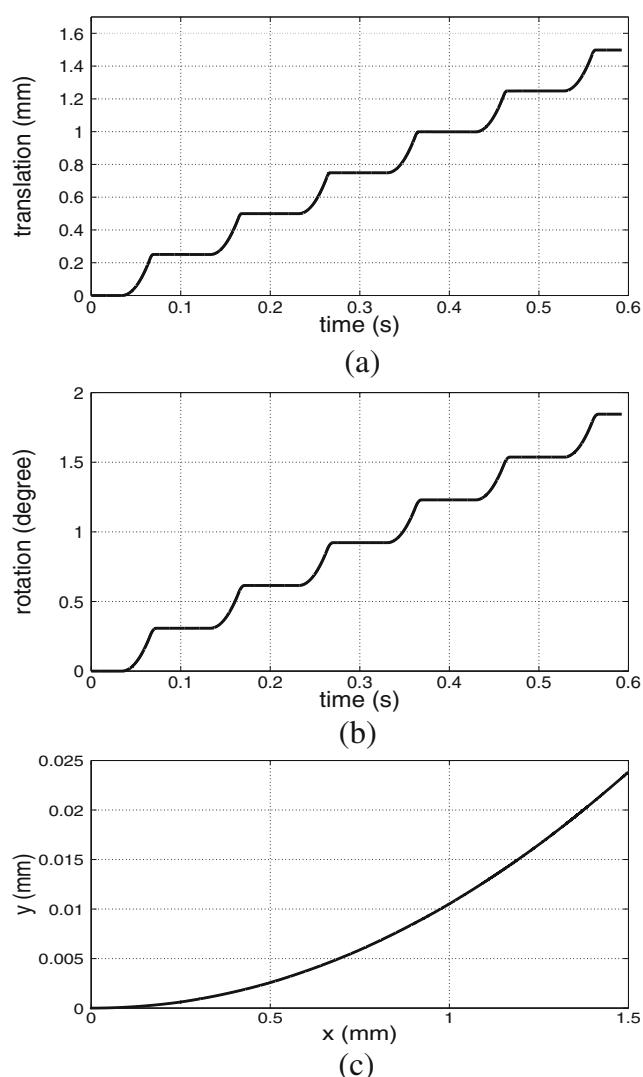
Fig. 7 Simulation results for hybrid translation-anticlockwise rotation **a** Forward translation **b** Anticlockwise rotation **c** Hybrid translation-anti-clockwise rotation

7 Conclusions and Future Works

The hybrid robot is an effective solution for the in-vivo active locomotion for diagnostic purposes. Introduction of two more modes means the robot can perform four modes of operation with a set of actuators. An appropriate operating mode can be selected based on the situation/task to reduce/remove the chance of causing harm to internal tissues. The modelling of the robot for various operating modes are performed. The simulation results show the feasibility of the design and propulsion principles. In our future research we would like to optimise the robot design, in particular, we want to optimise various parameters of the leg. We also would like to develop a hybrid robot prototype and perform ex-vivo and in-vivo experimentations.

References

1. Gao, J., Yan, G.: Locomotion analysis of an inchworm-like capsule robot in the intestinal tract. IEEE Trans. Biomed. Eng. **63**(2), 300–310 (2016)
2. Natali, C.D., Beccani, M., Simaan, N., Valdastri, P.: Jacobian-based iterative method for magnetic localization in robotic capsule endoscopy. IEEE Trans. Robot. **32**(2), 327–338 (2016)
3. Liu, L., Towfighian, S., Hila, A.: A review of locomotion systems for capsule endoscopy. IEEE Rev. Biomed. Eng. **8**, 138–151 (2015)
4. Son, D., Yim, S., Sitti, M.: A 5-D localization method for a magnetically manipulated untethered robot using a 2-D array of hall-effect sensors. IEEE/ASME Trans. Mech. **21**(2), 708–716 (2016)
5. Bao, G., Pahlavan, K., Mi, L.: Hybrid Localization of Micro-robotic Endoscopic Capsule Inside Small Intestine by Data Fusion of Vision and RF Sensors. IEEE Sensors J. **15**(5), 2669–2678 (2015)
6. Hawks, J., Kunowski, J., Platt, S.: In vivo demonstration of surgical task assistance using miniature robots. IEEE Trans. Biomed. Eng. **59**(10), 2866–2873 (2012)
7. Sun, Z.J., Ye, B., Qiu, Y., Cheng, X.G., Zhang, H.H., Liu, S.: Preliminary study of a legged capsule robot actuated wirelessly by magnetic torque. IEEE Trans. Magn. **50**(8), 1–6 (2014)
8. Valdastri, P., Webster, R.J., Quaglia, C., Quirini, M., Menciassi, A., Dario, P.: A new mechanism for mesoscale legged locomotion in compliant tubular environments. IEEE Trans. Robot. **25**(5), 1047–1057 (2009)
9. Munoz, F., Alici, G., Zhou, H., Li, W., Sitti, M.: Analysis of magnetic interaction in remotely controlled magnetic devices and its application to a capsule robot for drug delivery. IEEE/ASME Trans. Mech. **23**(1), 298–310 (2018)
10. Prendergast, J.M., Formosa, G.A., Rentschler, M.E.: A platform for developing robotic navigation strategies in a deformable, dynamic environment. IEEE Robot. Auto. Lett. **3**(3), 2670–2677 (2018)
11. Platt, S., Hawks, J., Rentschler, M.: Vision and task assistance using modular wireless in vivo surgical robots. IEEE Trans. Biomed. Eng. **56**(6), 1700–1710 (2009)
12. Yu, H., Huda M.N., Wane S.O.: A novel acceleration profile for the motion control of capsubots. In: IEEE international conference on robotics and automation (ICRA), pp. 2437–2442 (2011)
13. Huda, M.N., Yu, H., Goodwin, M.J.: Experimental study of a capsubot for two dimensional movements. In: UKACC international conference on control, pp. 108–113. Best student paper (2012)
14. Liu, P., Yu, H., Cang, S.: Optimized adaptive tracking control for an underactuated vibro-driven capsule system. Nonlinear Dyn **94**, 1–15 (2018)

15. Carta, R., Sfakiotakis, M., Pateromichelakis, N., Thoné, J., Tsakiris, D., Puers, R.: A multi-coil inductive powering system for an endoscopic capsule with vibratory actuation. Sens. Actuator A Phys. **172**(1), 253–258 (2011)
16. Simi, M., Valdastri, P., Quaglia, C., Menciassi, A., Dario, P.: Design, fabrication, and testing of a capsule with hybrid locomotion for gastrointestinal tract exploration. IEEE/ASME Trans. Mech. **15**(2), 170–180 (2010)
17. Yu, H., Huda, M.N., Liu, Y., Wane, S.O.: Travelling capsule with two drive mechanisms (2013)
18. Huda, M.N., Yu, H., Cang, S.: Behaviour-based control approach for the trajectory tracking of an underactuated planar capsule robot. IET Control Theory Appl. **9**(2), 163–175 (2014)
19. Sun, K., Mou, S., Qiu, J., Wang, T., Gao, H.: Adaptive fuzzy control for non-triangular structural stochastic switched nonlinear systems with full state constraints. IEEE Trans. Fuzzy Syst. **27**(8), 1587–1601 (2018)
20. Qiu, J., Sun, K., Wang, T., Gao, H.: Observer-based fuzzy adaptive event-triggered control for pure-feedback nonlinear systems with prescribed performance. IEEE Trans. Fuzzy Syst. **27**(11), 2152–2162 (2019)
21. Quirini, M., Menciassi, A., Scapellato, S., Dario, P., Rieber, F., Ho, C.N., et al.: Feasibility proof of a legged locomotion capsule for the gi tract. Gastrointestinal Endoscopy **67**(7), 1153–1158 (2008)

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