Flexural strengths and fibre efficiency of steel-fibre-reinforced, roller-compacted, polymer modified concrete

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Abstract: A new material suitable for the structural repair of concrete pavements has been developed at Coventry University exhibiting high flexural, shear and bond strengths and high resistance to reflection cracking, demonstrating also unique 'placeability' and 'compactability' properties.
This article deals with the standard equivalent flexural strengths evaluated using the identical fibre bridging concept and the size effect. Correlation of flexural strengths for beams of different sizes was achieved and the efficiency of fibre in the mix was scrutinised. It was concluded that the efficiency was much higher in the new steel-fibre reinforced, roller compacted, polymer modified concrete (SFR-RC-PMC) mix than in conventional concrete. The high efficiency revealed by the fibre bridging law is mainly attributed to a lower water to cement ratio. It was also found that the fibre aspect ratio influences significantly the flexural performance of the new material. The very high flexural strength extracted from the SFR-RC-PMC, compared to conventional steel-fibre reinforced concrete is very favourable to worn concrete pavement rehabilitation.

Dear Editor

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Please accept the revised submission of our article with the above title. Revisions were made in accordance with the reviewers' requirements
A Data in Brief article has also been prepared and submitted.

Dr. Yougui Lin is a research assistant at the Department of Civil Engineering Architecture and Building, Faculty of Engineering and Computing, of Coventry University, UK.

Dr. John N Karadelis is senior lecturer, at the Department of Civil Engineering Architecture and Building, Faculty of Engineering and Computing, Coventry University, UK.

Kind regards

John Karadelis and Yougui Lin
28 March 2015

*Detailed Response to Reviewers

LIST OF CHANGES

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	Reviewer's Comments	Author's Response
1	What is the reason for the sharp decrement in flexural strength of PVAPMC in Figure 3?	The reason for the sharp drop of flexural strength of mix PAVPMC1.5%-35 shown in Fig.3 is due to the fact that it exhibited lower flexural toughness than the other mixes. The mix contained 1.5% 35mm-length steel fibre by volume. The flexural performance of the same mix under 3PB shown in Fig.4 also exhibited the same tendency. The article has been amended accordingly (p:5, below Figure 3)
2	In Table 8, how can we use the fibre bridging law in site applications?	The fibre bridging law can serve as an index to evaluate the fibre efficiency for the selection of ingredients during the mix design process in practical (site) applications. For example, mixes SBRPMC1.5%-35 and SBRPMC1.5%-50, in Table 8, are the same (have identical proportions of ingredients), only the former incorporates shorter fibres than the latter. It is apparent from Figure 6 (b) that SBRPMC1.5%-50 is more efficient than SBRPMC1.5%-35 because the fibres of mix -50 provide higher tensile strength than those of -35, for the same crack opening displacement. In this case, the fibre bridging law specified in Table 8, can be used to predict the flexural performance of beams made of the three different mixes. This has been mentioned in the article (p:15, just above the Concluding Remarks)

*Highlights

Flexural Strengths and Fibre Efficiency of Steel-Fibre-Reinforced, Roller-Compacted, Polymer Modified Concrete.

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HIGHLIGHTS:

- Standard equivalent flexural strengths are established for overlay pavement design
- SBRPMC1.5%-35 mix is optimal for flexural and bond strengths and workability
- Lower w/c is the main reason for superior performance of fibre in the SFR-RC-PMC
- The fibre bridging law can be an index of fibre efficiency in a mix design
- The fibre bridging law can be used to predict the flexural performance of beams

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Abstract: A new material suitable for the structural repair of concrete pavements has been developed at Coventry University exhibiting high flexural, shear and bond strengths and high resistance to reflection cracking, demonstrating also unique *placeability* and *compactability* properties.

This article deals with the *standard* equivalent flexural strengths evaluated using the *identical fibre bridging concept* and the size effect. Correlation of flexural strengths for beams of different sizes was achieved and the efficiency of fibre in the mix was scrutinised. It was concluded that the efficiency was much higher in the new steel-fibre reinforced, roller compacted, polymer modified concrete (SFR-RC-PMC) mix than in conventional concrete. The high efficiency revealed by the fibre bridging law is mainly attributed to a lower water to cement ratio. It was also found that the fibre aspect ratio influences significantly the flexural performance of the new material. The very high flexural strength extracted from the SFR-RC-PMC, compared to conventional steel-fibre reinforced concrete is very favourable to worn concrete pavement rehabilitation.

Keywords: steel fibre-reinforced, roller-compacted, polymer-modified, concrete, fibre efficiency.

1. Introduction.

Part of the 'Green Overlays' research lead by the authors for the last four years involved the development of special concrete mixes used as overlay material, fully bonded on worn concrete pavements. This material exhibits high flexural, shear and bond strengths and high resistance to reflection cracking. It also demonstrates unique *placeability* and *compactability* properties, hence it can be placed on the damaged surface by an asphalt paver and compacted by a vibrating roller [1]. The mixes were named steel-fibre-reinforced, roller-compacted, polymer modified concrete (SFR-RC-PMC). The steel fibre in the mix retards and contains reflective cracking, the polymers enhance its strength and achieve good bond with the old

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concrete and the roller compaction ensures quick construction. These types of mixes were different from conventional roller-compacted concrete (RCC). Specifically, the optimal water content of the former determined by the modified-light (M-L) compaction method proposed by the authors [1] was usually around 17kg higher than the latter, designed by the modified Vebe method [2 - 3] for $1m^3$ of concrete, for the same mix proportion [1].

Flexural strengths of conventional steel fibre reinforced concrete (SFRC) have been investigated since the 1980s [4 - 11]. A vast amount of literature deals with flexural strength, residual flexural strength, toughness, toughness indexes, crack development and propagation, fibre bridging law, fracture energy, and so on. Neocleous at el. [12 - 13] investigated the flexural performance of steel fibre-reinforced RCC for pavements, while the steel fibres were recovered from used tyres, whereas the mix was conventional RCC. Kagaya et al. [14] investigated the mix design method for steel fibre reinforced RCC pavements by employing the modified Proctor compaction method.

It is seen that the mechanical properties of SFR-RC-PMCs have not been investigated to date. In addition, steel fibres in these types of mixes may exhibit a different behaviour to those in conventional SFRCs, due to the fact that the former contains much less cement paste than the conventional concrete, and roller compaction may result in deformation of steel fibres. Furthermore, the flexural performance of PVA (Polyvinyl Alcohol) modified concrete has rarely been investigated. Therefore, it is crucial to investigate the flexural performance of SFR-RC-PMC for overlay pavement design. This article aims to reveal the flexural performance, especially the equivalent flexural strengths of SFR-RC-PMC for overlay pavement design and the efficiency of fibres in RCC.

2. Mix Proportion and Specimen Preparation

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57 The ingredient materials used (apart from the 50mm-long fibre) were presented in ref. [1] in
58 detail. The 50mm-long fibre was the hooked-end type, with an aspect ratio of 80. The test
59 beams of eight mixes are tabulated in Table 1. Two types of polymers, i.e. SBR (Styrene
60 Butadiene Rubber) and PVA (Polyvinyl Alcohol) and two types of steel fibre, i.e. 35 mm-
61 long and 50 mm-long were used. Super-plasticizer was added in the PVA modified concrete
62 to reduce water content and obtain high strength, while the SBR modified concrete did not
63 incorporate any admixtures. Among a total of eight mixes, five mixes, SBRPMC1%-35,
64 SBRPMC1.5%-35, SBRPMC2%-35, PVAPMC1.5% and SBRPMC1.5%-50 (final numbers
65 of mix ID indicate length of fibres), were SFR-RC-PMC, whose water contents were
66 determined using the M-L compaction method [1]. Mix SBRPMC0%, did not contain fibre
67 and was used as the matrix of mixes SBRPMC1.5%-35 and SBRPMC1.5%-50. Also, it was
68 purposely used for the evaluation of the relative toughness of the same mixes. All beams of
69 the six mixes were fabricated in steel moulds using the vibrating compactor shown in Figure 1,
70 which was purposely designed for specimen formation. The dimensions of the beams of the
71 six mixes were 80 (W) x 100 (H) x 500 (L) mm
72 The mixing procedure can be found in ref. [1]. The mix compaction was carried out in two
73 layers. Each layer was about 40 - 50 mm thick. The vibrating compaction lasted 30 - 50
74 seconds per layer for SBRPMC, and 60 - 90 seconds for PVAPMC until mortar formed a ring
75 around the perimeter of the moulds. The surface of each layer was roughened before
76 accepting the next layer of material. The specimens were de-moulded in twenty-four hours.
77 The SBR modified concrete specimens were cured in water for five days whereas the PVA
78 specimens for seven days, followed by air curing until the test day. The ages of the specimens
79 for tests were 28 days – 40 days.
80 The conventional SFRC, i.e. Con.SBRPMC1.5%-35, was intended for comparison with the
81 mix SBRPMC1.5%-35 to reveal the efficiency of fibres. The former had the same ingredients
82 and mix proportion as the latter except for the water content. The mix Con.SBRPMC0% acted

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as the matrix of mix Con.SBRPMC1.5%-35. The slump of the mix Con.SBRPMC1.5%-35 was 130 mm. The dimensions of the beams of both mixes were 100 (W) x 100 (H) x 500 (L) mm, fabricated in steel moulds on the vibrating table. The mixing and curing procedures of both mixes were the same as for mix SBRPMC1.5%-35.

Table 1

Proportion of mixes with optimal water content determined by M-L method (Cem.= Cement, Supe.= Superplasticizer, Ad.water= Added water)

Mix ID	Mix proportion							Fibre by	Wet densi.
	Cem.	Aggr.	Sand	SBR	PVA	Supe.	Ad.water	volume	(Kg/m^3)
SBRPMC1%-35	1	1.266	1.266	0.217	0	0	0.072	1%	2479
SBRPMC1.5%-35	1	1.266	1.266	0.217	0	0	0.095	1.50%	2482
SBRPMC2%-35	1	1.266	1.266	0.217	0	0	0.103	2%	2499
PVAPMC1.5%-35	1	1.266	1.266	0	0.02	0.025	0.228	1.50%	2466
Con.SBRPMC1.5%-35	1	1.266	1.266	0.217	0	0	0.245	1.50%	
SBRPMC1.5%-50	1	1.266	1.266	0.217	0	0	0.095	1.50%	2482
Con.SBRPMC0%	1	1.266	1.266	0.217	0	0	0.245	0%	
SBRPMC0%	1	1.266	1.266	0.217	0	0	0.095	0%	

(a) (b)

Figure 1. (a) Vibrating compactor. (b) Steel plate for compaction.

The beam dimensions recommended by BS [15] are 150 (W) x 150 (H) x 550 (L) mm. The beams used in this study were 80 (W) x 100 (H) x 500 (L), recommended by ASTM [16]. The notches were saw cut to the specified depth by a circular saw one day prior to testing. The width of the notches was 3.5 - 4 mm, complying with BS [15].

3. Flexural Strength of PMC Beams

3.1 Strength under four-point bending (4PB) and three-point bending (3PB)

The representative test methods for steel fibre reinforced concrete currently available are the ASTM [16] and BS [15] methods. The intact beams of the three mixes, SBRPMC1.5%-35, PVAPMC1.5%-35 and Con.SBRPMC1.5%-35, were tested using four point bending (4PB) arrangements. The loading configuration and experimental setups are shown in Figure 2 (a) & (b). The test procedure complied with ASTM [16]. Two LVDTs measuring net deflection were mounted on both sides of the frame. A hydraulic servo-closed loop test facility with a maximum load capacity of 150 KN was used. The loading rate was controlled by a LVDT placed at mid-span. The representative mid-span deflection was the average of the two LVDT readings. The rate of increase of net deflection was 0.0017 mm/s until the LVDT reading reached 0.5 mm; after the 0.5 mm were reached the rate was increased to 0.0033 mm/s. This is within the range specified by ASTM [16]. The load and vertical displacements were continuously recorded at a frequency of 5Hz. The maximum flexural strength, f_p, and the residual flexural strengths, $f_{R,0.5}$ and $f_{R,2}$ were calculated using eqn.(1) in accordance with ASTM [16]:

$$f_j = \frac{300P_j}{Bh^2} \quad (1)$$

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Where: *j= P (for peak),* or *j= R,0.5,* or *j= R,2.*

In this case, *R* denotes residual flexural strength. P_p, is the maximum load. $P_{p,0.5}$ is the load corresponding to mid-span deflection equal to 0.5 mm. $P_{p,2,}$ is the load corresponding to mid-span deflection equal to 2 mm. f_p, is the maximum flexural strength. $f_{R,0.5}$ and $f_{R,2}$ are strengths corresponding to mid-span deflections of 0.5 and 2 mm respectively. *B* and *h* are the breadth and depth of the beam.

The relationships of flexural strength vs. mid-span deflection for the three mixes are presented in Figure 3. The mid-span deflection was recorded and averaged by two LVDT readings. The laboratory tests showed that all the SBRPMC1.5%-35 and PVAPMC1.5%-35 beams failed with multiple cracking under the 4PB test. However, for concrete used as an overlay on worn concrete pavements, a single reflective crack will initiate from the location of an underlying existing crack of the worn pavement. Therefore, the 3PB test arrangement was chosen as more suitable for concrete overlays.

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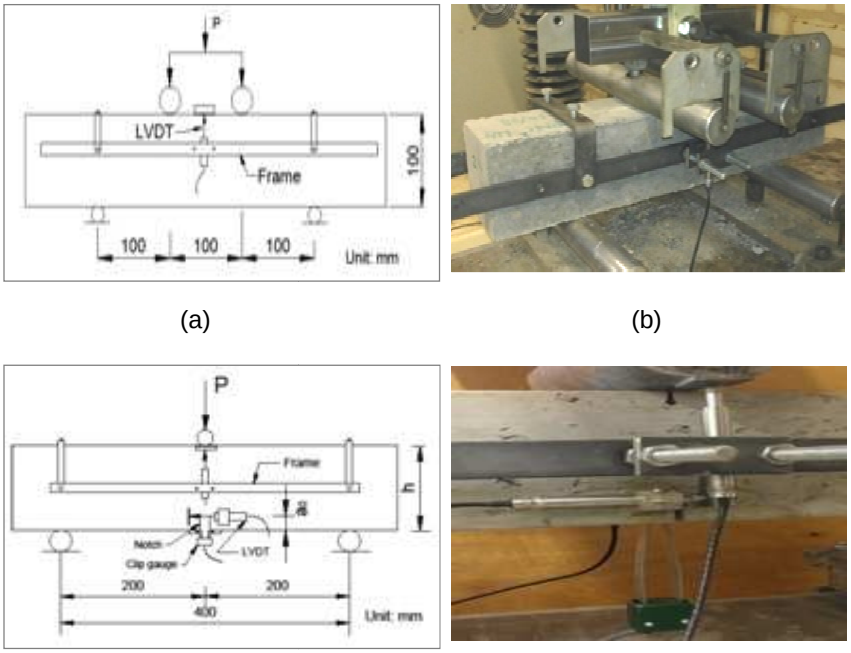

Figure 2. (a) Un-notched beam under 4PB. (b) Experimental setup of 4PB test. (c) Notched beam under 3PB. (d) Close view of clip gauge and LVDTs mounted on the beam under 3PB.

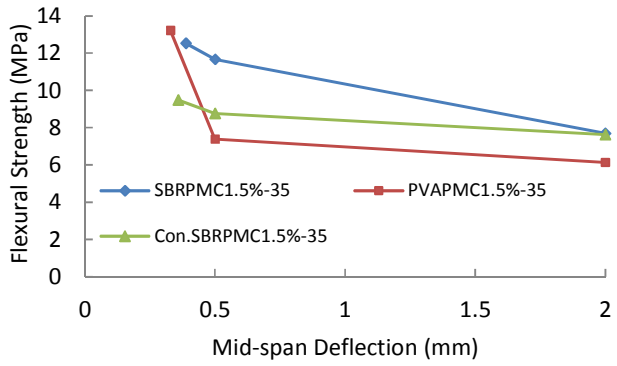

Figure 3. Flexural strengths of un-notched beams for three different mixes under 4PB.

The reason for the sharp drop of the flexural strength of mix PVAPMC1.5%-35 shown in Figure 3 is due to the fact that it exhibited lower flexural toughness than the other two mixes. The flexural performance of the same mix under a 3PB test, shown in Figure 4, shows also the same tendency. The mix contained 1.5%-35mm length steel fibre by volume.

151 The three-point bending (3PB) test, recommended by BS [15], was employed to measure the
152 flexural performance. The experimental setup is shown in Figure 2, (c) & (d). Six mixes
153 shown in Figure 4 were tested under 3PB complying with the BS [15]. The beams measured
154 80 (W) x 100 (H) x 500 (L) mm, spanning 400 mm with a mid-span notch of 20 mm depth.
155 They were loaded at mid-span. It should be pointed out that the dimensions of the beams used
156 in this study were different from those proposed by BS [15], which are 150 (W) x 150 (H) x
157 550 (L) mm, with span of 500 mm, centrally loaded and notched to the depth of 25 mm.
158 The loading machine was the same as the one used in the 4PB test. One LVDT was fixed on
159 the frame for measuring mid-span (point-load) deflection. The other, for measuring notch tip
160 opening displacement (CTOD), was secured on the beam surface, while the clip gauge was
161 mounted on the underside to measure the crack mouth opening displacement (CMOD) and
162 control the loading rate. Test data were automatically recorded by a computer at the frequency
163 of 5 Hz. The loading rate procedure, controlled by CMOD, was as follows: 0.0001 mm/s until
164 CMOD reached 0.2 mm; 0.0033 mm/s until CMOD reached 3 mm; then 0.005 mm/s until
165 failure of the specimen. The rate of increase CMOD used was much lower than that proposed
166 in the BS [15], which is 0.00083 mm/s until CMOD= 0.1 mm; after that 0.0033 mm/s. All
167 tests were accurately controlled; no abrupt failures occurred and suitable load-CMOD, load-
168 CTOD, and load - load point deflection curves were obtained. These results were used to
169 evaluate the maximum flexural strength, residual flexural strength, equivalent flexural
170 strength, relative toughness index, and total fracture energy and size effects.
171 The flexural strengths were evaluated according to BS [15], using eqns. (2) – (4):
172

173 $$f_{ct,L}^{f} = \frac{3SP_L}{2Bh_{sp}^2} \quad (2)$$

174 $$f_{\mathrm{R,j}} = \frac{3\mathrm{SP_j}}{2\mathrm{Bh_{sp}^2}} \quad (3)$$

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$$f_{\mathrm{P}} = \frac{3\mathrm{SP_P}}{2\mathrm{Bh_{sp}^2}} \quad (4)$$

Where: $f_{\mathrm{ct,L}}^{\mathrm{f}}$ is the limit of proportionality (LOP) in MPa. P_L is the load corresponding to LOP (N). S is the span (mm). B is the breadth (width) of the specimen (mm). h is the depth (height) of the beam (mm). a_0 is the depth of notch (mm). h_{sp} is the distance between the tip of the notch and the top of the specimen (mm). $f_{\mathrm{R,j}}$ is the residual flexural tensile strength. CMOD= j, j= 0.5, 1.5, 2.5, & 3.5 mm, respectively. P_j is the load corresponding to CMOD= j, (N); f_P is the maximum flexural tensile strength (MPa). P_P is the peak load (N).

The flexural strength-CMOD relationships are plotted in Figure 4. The compressive strengths of blocks saw-cut from the tested beams are listed in

Table **2**, while the interfacial fracture toughness and splitting tensile bond strength of composite specimens are shown in Table 3. The details for testing interfacial fracture toughness can be found in ref. [17]. It is seen that:

a. Compared to conventional SFRC, SFR-RC-PMC exhibited very high flexural strengths, which are desired for worn concrete pavement rehabilitation;
b. Compared to the strengths measured under 4PB for the same mix, the obtained strengths under 3PB are remarkably higher.

However, the flexural strengths cannot be directly used for overlay pavement design. The design method for SFRC pavements proposed by Altoubat et al [18], requires the flexural strengths to be converted into equivalent flexural strengths.

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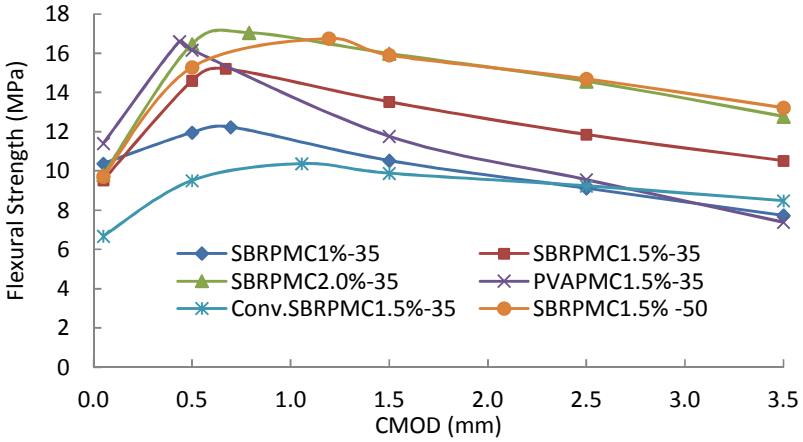

Figure 4. Flexural strengths of six 20mm-notched PMC beams under 3PB

Table 2

Compressive strengths of blocks saw-cut from tested beams

Mix ID	Num. of block	Compres. strength (MPa)	
		Average	STDEV
SBRPMC 1%-35	3	83.91	6.69
SBRPMC 1.5%-35	4	79.61	1.48
SBRPMC 2%-35	3	84.76	0.27
Con. SBRPMC 1.5%-35	8	68.18	2.82
PVAPMC 1.5%-35	6	105.87	3.78

Table 3

Mechanical properties of interface of SBRPMC1.5%-35, PVAPMC1.5%-35 and OPCC to OPCC composite specimens.

Interfacial fracture toughness (J/m^2)	SBRPMC1.5%-35 on-OPCC	Roughened interface	52.0
		Smooth interface	22.6
Splitting tensile bond strength (MPa)	SBRPMC1.5%-35 on-OPCC	Roughened interface	2.96
		Smooth interface	1.8
	PVAPMC1.5%-35 on-OPCC	Roughened interface	3.7
	OPCC-on-OPCC	Roughened interface	2.68

3.2 Size Effect on Flexural Strength

There are two major approaches to explaining the effect of size on the strength of a material: the statistical and deterministic approaches. A representative statistical approach is Weibull's theory [19], while the classic deterministic approach is by Bazant [20 - 21], based on fracture mechanics. According to Weibull's theory [19], a larger specimen has a weaker strength because it has a higher probability of having larger and more severe flaws or defects in it. Table 4, Figures 3 & 4 indicate that for the same mix, the measured flexural strength under 4PB is higher than that under 3PB. The reason for this can be explained by Weibull's theory. As has been presented earlier, the tested beams in this study were of dimensions 80 (W) x 100 (H) x 400 (S) mm. The beams for 3PB were saw-cut a central notch of 20 mm prior to testing, while the beams for 4PB were intact. In order to use the equivalent concept (presented later), proposed by the Japan Society of Civil Engineers (JSCE-SF4) [22], the flexural strength obtained using 3PB test has to be converted to that by 4PB test.

It is seen from Figure 4 that the flexural strength-CMOD curves for all mixes are basically parallel to each other except for the mix PVAPMC1.5%-35. This indicates that all mixes have

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the same scale factor for equivalent strength conversion. The conversion factor (β_1) can be taken as the ratio of maximum flexural strength under 3PB to that under 4PB. It is used for converting the strength of the small volume to the large volume, which can be explained by Weibull's theory [19].

The maximum flexural strengths tested under the 3PB and 4PB are listed in Table 4. The conversion factor, β_1 can be easily obtained by simply comparing the f_p in the 4PB to the 3PB, using eqn. (5). The calculated β_1 is listed in Table 4.

$$\beta_1 = \frac{f_P \ \ (in\ 4PB)}{f_P \ \ (in\ 3PB)} \tag{5}$$

In this study [23], the flexural strength affected by the height of beams was experimentally investigated. For this purpose, the SBRPMC1.5%-35 beams with the dimensions of 80 (W) x 100 (H) x 400 (S) mm and 100 (W) x 150 (H) x 500 (S) mm and with different notch lengths, were tested under 3PB to investigate the size effect on maximum flexural strengths. The size effect law proposed by Bazant [21] was employed. The splitting tensile strength taken from three cylinders with the dimensions Φ100 x 170 mm was 9.88 MPa. Consequently, the size effect law obtained using regression analysis for maximum flexural strength of mix SBRPMC1.5%-35 is [23]:

$$f_p = \frac{80.42}{\sqrt{\frac{h_{sp}}{2.7}-1}} \tag{6}$$

Where: f_p is the maximum flexural strength (MPa). h_{sp} is as per Eqns. (3) & (4).

Eqn. (6) will be used to determine the standard equivalent flexural strength later.

3.3 Equivalent Flexural Strength.

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Altoubat et al. [18] tested an actual size SFRC slab on an elastic foundation, and related the load carrying capacity to the equivalent flexural strength proposed by the Japan Society of Civil Engineers (JSCE-SF4) [22]. He then proposed a simple design method for SFRC pavements. The equivalent flexural strength, $f_{e,3}$ proposed by JSCE-SF4 [22] was measured by conducting a 4PB test. The test beam was 150 (W) x 150 (H) x 450 (S) mm. The equivalent flexural strength was calculated using the area enveloped by load-central deflection curve, and is evaluated by eqn. (7).

$$f_{e,3} = \frac{S.A_{3mm}}{2Bh^2} \quad (7)$$

Where: A_{3mm} is the ratio of the area enveloped under the load-midspan deflection curve, from the origin to the load at deflection equal to 3 mm. *S* is the span. *B* and *h* are the breadth (width) and height of beam, respectively.

However, the beams used in this study were centrally notched, had dimensions of 80 (W) x 100 (H) x 400 (S) mm and were tested under the 3PB. In order to use the equivalent flexural strength concept, which is defined at the specified deflection of 3 mm, it is necessary to correlate the two different test methods via the relationship between deflection and CMOD. In the post-peak region of a 3PB test, a hinge forms at the top of the beam, hence the residual flexural strength is only dependent on the fibre reactions. For different dimensional beams under bending test, the fibre effect can be regarded as similar if the crack lengths and crack opening displacements of the two beams are identical. In order to compare the residual strengths in the post-peak region measured from different geometrical beams, Giaccio et al.

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[24] proposed an approach to determine the deflection limits of small beams to obtain design parameters of fibre-reinforced concrete.

Consider the two types of beams with different dimensions under 4PB and 3PB shown in Figure 5. Beam one is the standard un-notched beam with the dimensions S_1 and h_1 under 4PB, while beam two is a centrally-notched beam with dimensions S_2 and h_2 and initial notch a_0 under 3PB. In order to obtain identical fibre bridging effect, $CMOD_1$ should be equal to $CTOD_2$.

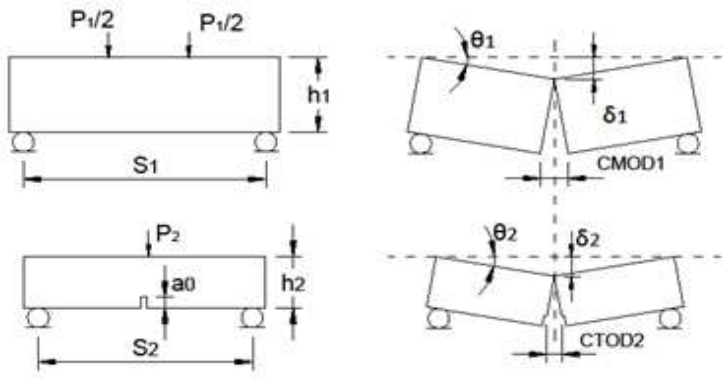

Figure 5. Correlation of δ_1 and δ_2 of two beams with different dimensions

In the post-peak region, the relationships between deflection and the rotation angle and crack opening is as follows:

$$\delta_1 = \theta_1 s_1/2 \tag{8}$$

$$\delta_2 = \theta_2 s_2/2 \tag{9}$$

$$CMOD_1 = 2h_1\theta_1 \tag{10}$$

$$CTOD_2 = 2(h_2 - a_0)\theta_2 \tag{11}$$

From the equations above and the condition of $\mathrm{CMOD}_1 = \mathrm{CTOD}_2$, the following equation is obtained:

$$\frac{\delta_1}{\delta_2} = \frac{s_1(h_2 - a_0)}{s_2 h_1} \quad (12)$$

The standard beam for testing equivalent flexural strength is 150 (W) x 150 (H) x 450 (S) mm, and the specified deflection, δ_1 = 3mm. The beams used in this study were 80 (W) x 100 (H) x 400 (S) mm with an initial notch of 20 mm. Hence, substitution of these dimensions into eqn. (12) results in:

$$\delta_2 = 1.67\delta_1 \quad (13)$$

Thus, the corresponding deflection limit, δ_2, determined using eqn. (13) is 5 mm. Hereafter, the equivalent strength for the deflection limit of 5 mm is denoted as $f_{e,5.}$ The equivalent flexural strengths $f_{e,5}$ are listed in Table 4.

3.4 Standard Equivalent Flexural Strength, $f_{e,3}$

However, the equivalent flexural strength, $f_{e,5}$, cannot be used directly for the design of the SFRC overlay pavement proposed by Altoubat et al.[18], because specimen sizes affect the flexural strength significantly. As has been presented earlier, the tested beams in this study were of dimensions 80 (W) x 100 (H) x 400 (S) mm with a central notch of 20 mm, quite different from the standard beam for testing equivalent flexural strength proposed by JSCE-

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SF4 [22], which is of the dimensions 150 (W) x 150 (H) x 450 (S) mm. Therefore, the $f_{e,5}$ above needs to be converted by taking the size effect into account.

It is seen from Figure 4 that the flexural strength-CMOD curves for all mixes are basically parallel to each other except for the mix PVAPMC1.5%-35. This indicates that all mixes have the same scale factor for equivalent strength conversion. In order to use the SFRC pavement design method proposed by Altoubat et al. [18], the $f_{e,5}$ has to be converted twice to obtain the standard equivalent flexural strength, $f_{e,3}$.

First, it has to be converted from the 3PB to 4PB. Its conversion factor (β_1) has been determined previously. Second, it has to be converted from a 4PB test with the beam of 100 mm height to a 4PB test with the standard beam of 150 mm height, via the conversion factor (β_2) that can be determined using the size effect equation (6) for mix SBRPMC1.5%-35.

Both conversion factors are attributed to the size effect. Factor β_2 is for converting the strength of the 'short' beam to that of the 'tall' beam, explained thoroughly by Bazant's theory [21]. The second conversion factor, β_2, is calculated in the following way:

$$\beta_2 = \frac{f_P \quad (in\ 150mm{-}height\ beam)}{f_P \quad (in\ 100mm{-}height\ beam)} = \frac{\sqrt{\frac{100}{2.7}-1}}{\sqrt{\frac{150}{2.7}-1}} = 0.813 \tag{14}$$

$$\beta = \beta_1 \cdot \beta_2 \tag{15}$$

The process of calculating the total conversion factor β and the standard equivalent flexural strength, $f_{e,3}$, are tabulated in Table 4. It is seen from Table 4 that the mix PVAPMC1.5%-35 developed the lowest standard equivalent flexural strength, although it exhibited very high maximum flexural strength. The standard equivalent flexural strength, $f_{e,3}$ can be used for SFR-RC-PMC overlay pavement design.

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346

347 **Table 4**

348 Calculation of standard equivalent flexural strength $f_{3,e}$

Mix ID	$f_{e,5}$ (MPa)	f_P in 3PB (MPa)	f_p in 4PB (MPa)	First convers. factor β_1	Second convers. factor β_2	$f_{e,3}$ (MPa)
SBRPMC1%-35	8.87	12.24	N/A	0.823	0.813	5.93
SBRPMC1.5%-35	10.86	15.22	12.53	0.823	0.813	7.27
SBRPMC2%-35	14.05	17.05	N/A	0.823	0.813	9.4
Con.SBRPMC1.5%-35	9.13	10.37	9.49	0.915	0.813	6.79
SBRPMC1.5%-50	14.24	16.76	N/A	0.823	0.813	9.53
PVAPMC1.5%-35	10.05	16.6	13.2	0.795	0.813	6.49

349

350 **3.5 Verification.**

351

352 The experimental results of SBRPMC1.5%-35 beams with different notch lengths and beam
353 depths, which were previously used for establishing the size effect law, were reanalysed to
354 verify the method for calculating the equivalent flexural strength, $f_{e,3,}$ which should be
355 theoretically identical. Two types of beams, i.e. three 80 (W) x 100 (H) x 400 (S) mm with 40
356 mm-long notch and two 100 (W) x 150 (H) x 500 (S) mm beams with 25 mm-long notch were
357 analysed. The deflection limit for the former, determined using eqn. (11), was 6.8 mm, while
358 that of the latter was 4 mm. The equivalent flexural strengths $f_{e,5}$, $f_{e,6.8}$ and $f_{e,4}$ corresponding
359 to the deflection limits of 5, 6.8 and 4 mm, and their conversion factors are tabulated in Table
360 5. It is seen that the standard equivalent flexural strengths, $f_{e,3}$, determined using the method
361 proposed are approximately identical. This validates the method for calculating the standard
362 equivalent flexural strength, $f_{e,3}$, for overlay pavement design.

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Table 5

Standard equivalent flexural strength determined using experimental results of beams with different notch length and beam depth (a_0=notch length, h=height of beam)

Mix ID	a_0/h (mm/mm)	$f_{e,5}$ /$f_{e,6.8}$/$f_{e,4}$ (MPa)	f_P in 3PB (MPa)	f_p in 4PB (MPa)	β_1	β_2	$f_{e,3}$ (MPa)
SBRPMC1.5%-35	20/100	10.86	15.22	12.53	0.823	0.813	7.27
	40/100	13.31	16.85	12.53	0.743	0.813	8.04
	25/150	8.89	11.94	N/A	0.823	1.00	7.32

4. Efficiency of Steel Fibre in Roller–Compacted Concrete.

Compared to conventional SFRCs, the SFR-RC-PMC has more air voids and relatively less cement paste (Table 6), hence this may lead to:

a. The steel fibres may not be fully bonded by cement paste;
b. The steel fibres may be deformed during specimen formation due to compaction by the vibrating compactor.

The two factors may consequently lead to poor steel fibre efficiency. In addition, the efficiency of 50mm-long fibres also need to be quantitatively investigated by comparison with 35mm-long fibres. Steel fibres have been successfully used in conventional concrete to improve the performance of concrete for several decades. The conventional concrete containing the same steel fibre type and fibre content, can be a reliable benchmark for the investigation of the fibre efficiency in SFR-RC-SBRPMC.

Table 6 Table 6 shows the main physical parameters of the three mixes SBRPMC1.5%-35, SBRPMC1.5%-50 and Con.SBRPMC1.5%-35. The mix Con.SBRPMC1.5%-35 was conventional concrete, its slump of fresh mix was measured to be 130mm. The three mixes

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contained the same fibre content and the beams were of the same dimensions to avoid any size effect.

Table **6** 6 clearly indicates that the water to cement ratios and cement paste contents of mixes SBRPMC1.5%-35 and SBRPMC1.5%-50 are much lower than those of the conventional Con.SBRPMC1.5%-35. Also, the former have higher air content than the latter.

Table 6

Comparison of physical properties of five mixes

Mix ID	Workability of fresh mixes	W/C	Cem. paste by volume (%)	Air content (%)
SBRPMC1.5%-35	Dry, non-slump	0.206	37.94	2.94
SBRPMC1.5%-50	Dry, non-slump	0.206	37.94	2.94
Con.SBRPMC1.5%-35	Wet, slump of 130mm	0.355	42.3	1.2
SBRPMC0%	Dry, non-slump	0.206	N/A	N/A
Con.SBRPMC0%	Wet, slump > 130mm	0.355	N/A	N/A

Note: the water for determining water to cement ratio and cement paste fraction included also the water contained in SBR but excluded the water absorbed by the coarse aggregate.

The beam dimensions and test procedures for the three mixes SBRPMC1.5%-35, SBRPMC1.5%-50 and Con.SBRPMC1.5%-35 have been presented in Section 2 and Section 3.1. The three mixes were tested under 3PB, and the experimental data have been analysed to evaluate maximum flexural strength, f_p, equivalent flexural strength, $f_{e,3,}$ relative toughness index, I_t, defined as the ratio of fracture energy of SFRC to that of unreinforced concrete [27] and total fracture energy, G_F [23]. These mechanical parameters are rearranged to study the fibre efficiency in the following:

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The total fracture energy was evaluated using the method recommended by the RILEM code [25], i.e. it is equal to the work done by the externally applied load divided by the area of fractured section of the beam.

The beams of mixes SBRPMC0% and Con.SBRPMC0% had midspan saw-cut notches to the depth of 33 mm made prior to the test. The 3PB test was conducted to measure fracture energy. The specimen dimensions and test procedure complied with the code of RILEM Report 5 1991 [26]. However, the much lower than the recommended by the same code CMOD - control loading rate was 0.0001 mm/s, in an effort to obtain stable load-deflection curves. The test for each beam lasted about 30 minutes, longer than that recommended by the RILEM code [26]. It is seen from Table 7 that:

a. The fibre in mix SBRPMC1.5%-35 exhibited much higher efficiency than the mix Con.SBRPMC1.5%-35, indicating that the efficiency of fibres in these mixes is much higher than that in conventional concrete.
b. The efficiency of fibres with aspect ratio of 80 in mix SBRPMC1.5%-50 was much higher than the fibres with aspect ratio of 60 in SBRPMC1.5%-35, indicating the fibre aspect ratio has remarkable influence on the flexural performance.

Table 7

Comparison of macro-mechanical properties of three mixes

Mix ID	f_p (MPa)	$f_{e,3}$ (MPa)	G_F (J/m^2)	I_t
SBRPMC1.5%-35	15.22	7.27	18580	221
SBRPMC1.5%-50	16.76	9.53	28300	337
Con.SBRPMC1.5%-35	10.37	6.79	15650	103

5. Mechanism of Fibre Efficiency.

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Observations on SFRC beam under 3PB test indicated that the crack initiated from the notch tip, and extended monotonically with load increments. The crack continued to extend but the applied load begun to fall after the peak load was reached and a hinge formed beneath the top of the beam. The complete process of failure of SFRC beam in flexure consisted of two stages: At stage I, prior to hinge formation, the flexural performance mainly depends on the interaction of matrix and fibres. At stage II, after the hinge formation, the flexural behaviour depends mainly on the resistance induced by fibre traction. Therefore, it is reasonable to use the relationship of fibre tensile stress and crack face opening displacement (fibre bridging law) at stage-II to reveal the reasons why the efficiency of fibre in RCC was much higher than that in conventional concrete. The fibre bridging at stage-II serves also as the fibre pull-out test. Table 8 presents the fibre bridging law, for stage-II, for three mixes, established by using inverse analysis presented in ref. [28] in detail. Figure 6 (b) provides a graphical representation of the law for the same three mixes.

Table 8

Fibre bridging law for stage-II under 3BP [Units: σ (MPa), and w (mm)]

Mix ID	Fibre bridging law for stage-II under flexure
SBRPMC1.5%-35	$\sigma_{II}(w) = -0.0056w^3+0.1612w^2-1.5044w+5.9306$
	$0.958 \le w \le 12.45$
Con.SBRPMC1.5%-35	$\sigma_{II}(w) = 0.0012w^3 - 0.025w^2 - 0.0461w + 2.4392$
	$0.907 \le w \le 12.64$
SBRPMC1.5%-50	$\sigma_{II}(w) = -0.0012w^3 + 0.0654w^2 - 0.9482w + 5.9164$
	$1.063 \le w \le 12.99$

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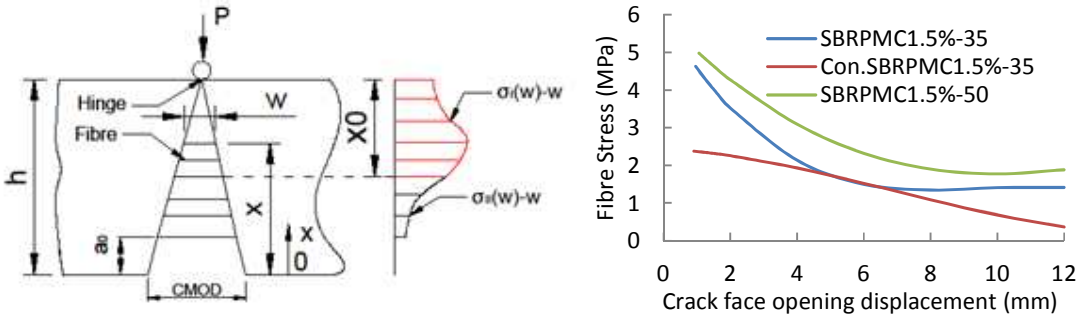

(a) (b)

Figure. 6 (a) Fibre tensile stress after a hinge formation beneath the point load (a_0=notch depth).

(b) Plots of fibre bridging laws in polynomial form as listed in Table 8

It is seen from Figure 6 (b) that both mixes SBRPMC1.5%-35 and Con.SBRPMC1.5%-35 contained the same amount and type of fibre, however the former exhibited higher tensile strength than the latter, for a given face opening displacement. It is clear that the main mechanism for the RCC having higher fibre efficiency than conventional concrete is attributed to a lower water to cement ratio, resulting in higher friction between fibre and mortar, although the air content of the former was higher than the latter. In addition, the curve of fibre bridging law of SBRPMC1.5%-50 is above the curve of SBRPMC1.5%-35 at all crack face opening displacements, implying that the former provided higher fibre traction. The fibre bridging law can serve as an index to evaluate the fibre efficiency for the selection of ingredients during the mix design process in practical (site) applications. For example, mixes SBRPMC1.5%-35 and SBRPMC1.5%-50, in Table 8, are the same (have identical proportions of ingredients), only the former incorporates shorter fibres than the latter. It is apparent from Figure 6 (b) that SBRPMC1.5%-50 is more efficient than SBRPMC1.5%-35 because the fibres of mix -50 provide higher tensile strength than those of -35, for the same crack opening displacement. In this case, the fibre bridging law specified in Table 8, can be used to predict the flexural performance of beams made of the three different mixes.

6. Concluding Remarks.

1. Compared to conventional steel fibre-reinforced concrete, steel fibre- reinforced roller-compacted polymer modified concrete developed very high flexural strength. This is very favourable to worn concrete pavement rehabilitation.
2. The standard equivalent flexural strengths evaluated using the method proposed by this study are listed in Table 4, and can be directly used for overlay pavement design. The method, using the identical fibre bridging concept and size effect, has been verified successfully.
3. Mix SBRPMC1.5%-35 is deemed to be optimum for both, strength and workability. Mix PVAPMC1.5%-35 exhibited higher flexural and bond strength with the old concrete than mix SBRPMC1.5%-35 but unfortunately low equivalent flexural strength which is the basis of overlay design and thus is not a suitable mix for worn concrete pavement rehabilitation.
4. The fibres in SFR-RC-PMC exhibited much higher efficiency than in conventional SFRC (consolidated by vibrating table). This is mainly attributed to a lower water to cement ratio. This indicates that these mixes are economically viable.

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